

**.For B.M diagram:**  
If we just take the moments to the left of the cross-section,

$$B.M_{x-x} = \frac{W}{2} x \text{ for } x \text{ lies between } 0 \text{ and } l/2$$

$$B.M_{\text{at } x = l/2} = \frac{W}{2} \cdot \frac{l}{2} \text{ i.e. } B.M \text{ at } x = 0$$

$$= \frac{Wl}{4}$$

$$B.M_{y-y} = \frac{W}{2} x - W \left( x - \frac{l}{2} \right)$$

Again

$$= \frac{W}{2} x - Wx + \frac{Wl}{2}$$

$$= -\frac{W}{2} x + \frac{Wl}{2}$$

$$B.M_{\text{at } x=l} = -\frac{Wl}{2} + \frac{Wl}{2}$$

$$= 0$$

Which when plotted will give a straight relation i.e.

A cantilever beam subjected to U.d.L, draw S.F and B.M diagram.

Here the cantilever beam is subjected to a uniformly distributed load whose intensity is given  $w / \text{length}$ .  
Consider any cross-section XX which is at a distance of  $x$  from the free end. If we just take the resultant of all the forces on the left of the X-section, then

$S.F_{xx} = -Wx$  for all values of 'x'. ----- (1)

$S.F_{xx} = 0$

$S.F_{xx \text{ at } x=l} = -Wl$

So if we just plot the equation No. (1), then it will give a straight line relation. Bending Moment at X-X is obtained by treating the load to the left of X-X as a concentrated load of the same value acting through the centre of gravity.

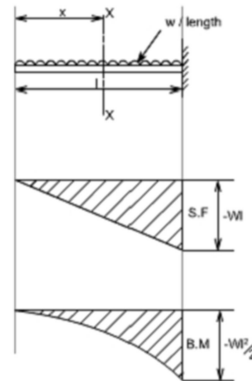
Therefore, the bending moment at any cross-section X-X is

$$\begin{aligned} B.M_{x-x} &= - W \times \frac{x}{2} \\ &= - W \frac{x^2}{2} \end{aligned}$$

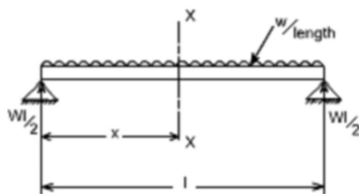
The above equation is a quadratic in x, when B.M is plotted against x this will produce a parabolic variation.

The extreme values of this would be at  $x = 0$  and  $x = l$

$$\begin{aligned} B.M_{at\ x=l} &= - \frac{Wl^2}{2} \\ &= \frac{Wl}{2} - Wx \end{aligned}$$



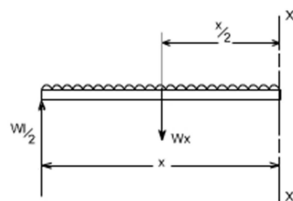
### Simply supported beam subjected to a uniformly distributed load U.D.L

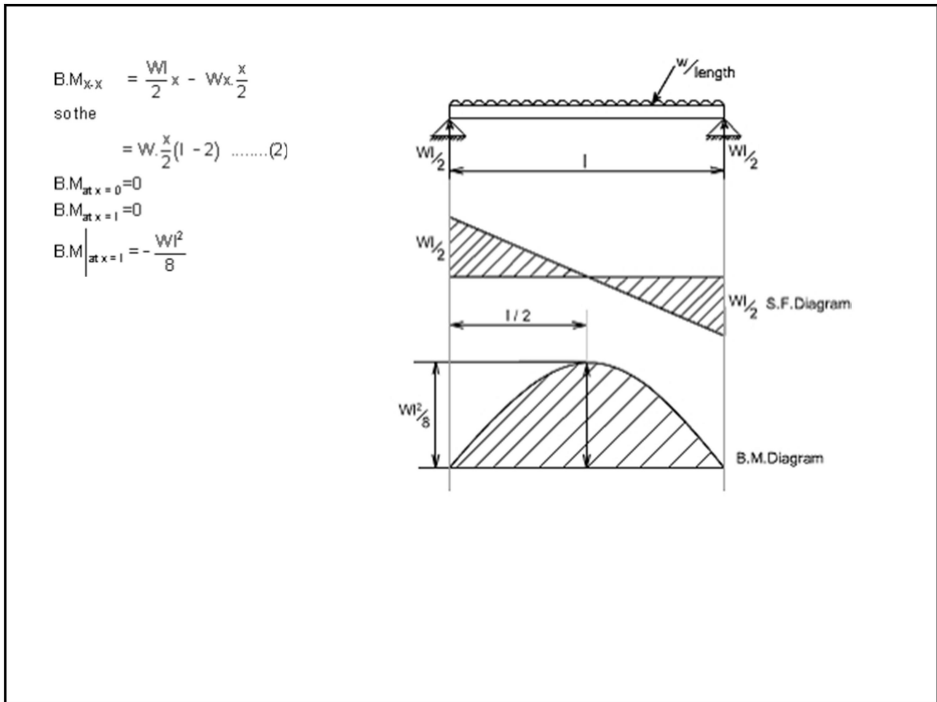


S.F at any X-section X-X is

$$\begin{aligned} &= \frac{Wl}{2} - Wx \\ &= W \left( \frac{l}{2} - x \right) \end{aligned}$$

The bending moment at the section x is found by treating the distributed load as acting at its centre of gravity, which is at a distance of  $x/2$  from the section





**An I - section girder, 200mm wide by 300 mm depth flange and web of thickness is 20 mm is used as simply supported beam for a span of 7 m. The girder carries a distributed**

**load of 5 KN/m and a concentrated load of 20 KN at mid-span.**

**Determine the**

**(i). The second moment of area of the cross-section of the girder**

**(ii). The maximum stress set up.**

**Solution:**

The second moment of area of the cross-section can be determined as follows :

For sections with symmetry about the neutral axis, use can be made of standard I value for a rectangle about an axis through centroid i.e.  $(b.d^3)/12$ . The section can thus be divided into convenient rectangles for each of which the neutral axis passes through the centroid.

Example in the case enclosing the girder by a rectangle

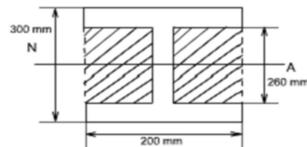
$$\begin{aligned}
 I_{girder} &= I_{rectangle} - I_{shaded\ portion} \\
 &= \left[ \frac{200 \times 300^3}{12} \right] 10^{-12} - 2 \left[ \frac{90 \times 260^3}{12} \right] 10^{-12} \\
 &= (4.5 - 2.64) 10^{-4} \\
 &= 1.86 \times 10^{-4} \text{ m}^4
 \end{aligned}$$

The maximum stress may be found from the simple bending theory by equation

$$\frac{\sigma}{y} = \frac{M}{I} = \frac{E}{R}$$

i.e.

$$\sigma_{max} = \frac{M_{max}}{I} y_{max}$$



### Calculations of Beam Reactions

Ex3:

$$\rightarrow \sum F_x = 0 \quad \text{--- (1)}$$
$$\underline{R_{Ax}} = 0$$

$$\curvearrow + \sum M_{@A} = 0 \quad \text{--- (2)}$$

$$250 + 80 \times 2.5 + 80 \times 3.75 - R_B \times 5 = 0$$

$$\therefore R_{By} = +135 \text{ N} \quad \uparrow$$

$$\uparrow \sum F_y = 0 \quad \text{--- (3)}$$

$$\underline{R_{Ay}} = -5 \text{ N} \quad \uparrow \quad \Rightarrow \quad \underline{R_{Ay}} = 5 \text{ N} \quad \downarrow$$

