PRIMARY SENSING ELEMENT III

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- The bellows element is a thin walled cylindrical cup-like structure with a number of folds for its cylindrical surface along the axis of the cup as shown in Fig.
- The fold are known as corrugations or convolutions .The formation of the convolution for a thin walled seamless tubing or cup is complex process, an hence welded bellows are manufactured by welding separately stamped annular diaphragms with a large hole at the center as shown in Fig.
- Precision bellows are normally of special metallic alloy used for generating much larger displacement with pressure than the other elastic elements.
- They are also made from plastic material and rubber for use at much lower pressure, and do not require much precision.
- Bellows are axially stretched or compressed by forces developed due to the difference in pressure between the inside and outside of the element.
- Bellows differing widely in their sizes are available for a variety of applications in instrumentation.

- The diameter of the bellows ranges from 7mm to 150mm ,while the wall thickness ranges fro 0.08 mm to 0.3mm.
- The merits of a bellow element are its low spring rate, low flexural rigidity, and a near-linear characteristics between pressure and displacement.
- But the limitation in their application to measurement is due to their lack of zero stability. To some extent, this difficulty is minimized by using it in conjunction with a high quality helical spring at the cost of its spring rate.
- Sensitivity of the bellow depends on various parameters such as the fold angle α , ratio m of the radius of curvature of the fold, R to internal radius Ri, and the ratio, c of the external radius Re to Ri.
- However, the axial deflection



However, the axial deflection y_m for the case with $\alpha = 0$ is given by

$$y_{m} = \pi R_{m}^{2} \Delta P \frac{1 - \mu^{2}}{Et} \frac{n}{A_{0} + B_{0} \frac{t^{2}}{R_{i}^{2}}}$$
(5.16)

where,

n = No. of convolutions

 $R_m = \text{mean radius } \frac{R_e + R_i}{2} \text{ m}$

 $P = \text{pressure difference N/m}^2$

 μ = Poisson's ratio of the material

E =Young's modulus N/m²

t =thickness of walls m

 R_i = internal radius m

 A_0, B_0 = constants depending on *m* and *c*

- Bourdon tube is the most favoured mechanical elements for the measurement of pressure and constitute an important group of primary transducer for converting pressure into linear and angular displacements.
- The simplest and the best form of bourdon tube element consist of thin-walled tube of an oval and flat sided cross-section, bent into circular arc of central angle ranging from 200 to 270 degree (hence known as C-type bourdon tube)
- One end is connected to rigid base to communicate with the source of pressure, while other end is closed and sealed having freedom of movement
- Due to pressure difference between inside and outside of the tube, the cross-section of the tube is deformed and the tube bent to circular cross section, the resulting effect being the displacement of the free tip

- The initial coiling angle ψ o decreases to ψ as shown and the difference of these two angles $\Delta \psi$ and the consequent displacement of the free tip y is linearly related to the pressure difference ΔP .
- The net displacement is 3-4mm for tube of 10cm diameter with $\Delta \psi$ of 10 degree.
- Thin walled tube have the ratio of t/b of less than 0.6, where t is thickness of the wall and b half breadth of the tube are used for the pressure up to 35kN/m2
- Thick walled tube with higher ratio above 0.6 is used to handle higher pressure.
- Expressions for $\Delta \psi$ and y for thin walled tube is given as follows



$$\frac{\Delta \Psi}{\Psi_0} = \Delta P \left[\frac{1 - \mu^2}{Ebt} R_0^2 \right] \left(1 - \frac{b^2}{a^2} \right) \left(\frac{\alpha}{\beta + \chi} \right)$$
(5.17)

(5.18)

(5.19)

(5.20)

$$y_{\text{radial}} = \frac{\Delta \psi}{\psi_0} R_0 (1 - \cos \psi_0)$$

$$y_{\text{tangential}} = \frac{\Delta \psi}{\psi_0} R_0 (\psi_0 - \sin \psi_0)$$

$$y = \sqrt{(y_{\rm rad}^2 + y_{\rm tan}^2)}$$

where

- ΔP = pressure difference, N/m²
- R_0 = radius of the arc, m
- μ = Poisson's ratio of the material
- E = Young's modulus of the material, N/m²
- a = semi-major axis of the tube, m
- b = semi-minor axis of the tube, m
- t = thickness of walls of tube, m
- $\chi = R_0 t/a^2$, a dimensionless constant
- α , β = dimensionless constants obtained from Table 5.5

 $\Delta \psi$, ψ_0 = angles, radians