

The *pn* junction excited by a constantcurrent source supplying a current Iin the forward direction.

The depletion layer narrows and the barrier voltage decreases by V volts, which appears as an external voltage in the forward direction.



Minority-carrier distribution in a forward-biased *pn* junction. It is assumed that the *p* region is more heavily doped than the *n* region;  $N_A \gg N_D$ .

Excess minority carrier concentration:

$$p_n(x_n) = p_{n0} e^{\frac{v}{V_T}}$$

$$n_p(-x_p) = n_{p0} e^{\frac{v}{V_T}}$$

> Exponential relationship

Small voltage incremental give rise to great incremental of excess minority carrier concentration.

Distribution of excess minority concentration:

$$p_{n}(x) = p_{n0} + [p_{n}(x_{n}) - p_{n0}]e^{-(x - x_{n})/L_{p}}$$
$$n_{p}(x) = n_{p0} + [n_{p}(-x_{p}) - n_{p0}]e^{(x + x_{p})/L_{n}}$$

Where

$$L_{p} = \sqrt{D_{p}\tau_{p}}$$
$$L_{n} = \sqrt{D_{n}\tau_{n}}$$

are called excess-minority-carrier lifetime.  $\tau_n, \tau_p$ 

The total current can be obtained by the diffusion current of majority carriers.

$$I = I_{pD} + I_{nD}$$
  
=  $A (J_{pD} + J_{nD})$   
=  $A (-q \frac{dp(x)}{dx} \Big|_{x=x_n} + q \frac{dn(x)}{dx} \Big|_{x=-x_p})$   
=  $Aq (\frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n})(e^{V_{vT}} - 1)$ 

The saturation current is given by :

$$I_{s} = qA(\frac{D_{p}p_{n0}}{L_{p}} + \frac{D_{n}n_{p0}}{L_{n}})$$
$$= qAn_{i}^{2}(\frac{D_{p}}{L_{p}n_{D}} + \frac{D_{n}}{L_{n}n_{A}})$$

I-V characteristic equation:

$$i = I_s(e^{\frac{v}{nV_T}} - 1)$$

- Exponential relationship, nonlinear.
- I<sub>s</sub> is called saturation current, strongly depends on temperature.
- $V_T$  is thermal voltage.

assuming  $V_1$  at  $I_1$  and  $V_2$  at  $I_2$  then:

$$V_2 - V_1 = nV_T \ln \frac{I_2}{I_1} = 2.3nV_T \log \frac{I_2}{I_1}$$

\* For a decade changes in current, the diode voltage drop changes by 60mv (for n=1) or 120mv (for n=2).

Turn-on voltage

A conduction diode has approximately a constant voltage drop across it. It's called turn-on voltage.

$$V_{D(on)} = 0.7V$$
 For silicon  
 $V_{D(on)} = 0.25V$  For germanium

- Diodes with different current rating will exhibit the turn-on lacksquarevoltage at different currents.  $TC = -2mv / {}^{\circ}C$
- Negative TC,

# The pn Junction Under Reverse-Bias Conditions



The *pn* junction excited by a constant-current source *I* in the reverse direction.

To avoid breakdown, *I* is kept smaller than  $I_S$ .

Note that the depletion layer widens and the barrier voltage increases by  $V_R$  volts, which appears between the terminals as a reverse voltage.

### The pn Junction Under Reverse-Bias Conditions

I-V characteristic equation:

 $i = I_s$  Independent of voltage.

Where  $I_s$  is the saturation current, it is proportional to  $n_i^2$  which is a strong function of temperature.

$$I_{s} = qA(\frac{D_{p}p_{n0}}{L_{p}} + \frac{D_{n}n_{p0}}{L_{n}})$$
$$= qAn_{i}^{2}(\frac{D_{p}}{L_{p}n_{D}} + \frac{D_{n}}{L_{n}n_{A}})$$

# The pn Junction Under Reverse-Bias Conditions



The *pn* junction excited by a reverse-current source *I*, where  $I > I_S$ . The junction breaks down, and a voltage  $V_Z$ , with the polarity indicated, develops across the junction.

# **I-V** Characteristics



The diode *i–v* relationship with some scales expanded and others compressed in order to reveal details