

Mach number! -

$$M = \frac{V}{c} = \frac{\text{velocity at a point in a fluid}}{\text{velocity of sound at that point at a given instant of time}}$$

For -  $M < 0.3$  — incompressible.

$0.3 < M < 0.8$  → Subsonic flow

$0.8 < M < 1.2$  — transonic [infact  $M=1$  — sonic flow].

$1.2 < M < 5$  — Supersonic flow

$5 < M < 11$  — hypersonic flow

$M > 11$  — hypervelocity flow.

i)  $M < 1$  ( $v < c$ ) — subsonic.

ii)  $M = 1$  ( $v = c$ ) — sonic.

iii)  $M > 1$  ( $v > c$ ) — supersonic

Mach Cone :- when the point source moves with a velocity  $(v)$  greater than sound speed, it will move ahead of the disturbance. The wave front in such case form a conical surface tangential to wavefronts. Known as Mach cone.

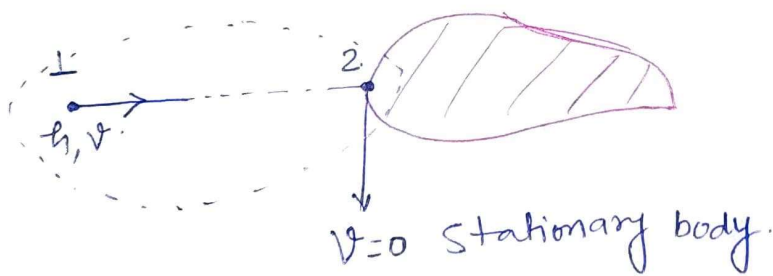
The half angle of the mach cone is known as mach angle.

$$\sin \alpha = \frac{ct}{vt} = \frac{c}{v} = \frac{1}{M}$$

The region inside the mach cone is known as zone of action, whereas the region outside is termed as zone of silence.

**Stagnation Properties!** The point on a immersed body, where the velocity is zero is called stagnation point. The value of pressure, temp, density at stagnation point are called stagnation properties.

- no heat interaction
- no work interaction



$$h_1 = h, \quad v_1 = v, \quad z_1 = z, \quad h_2 = h_0, \quad v_2 = 0, \quad z_2 = z$$

According to S.F.E.E.

$$h + \frac{v^2}{2} + \Delta ke + \Delta pe + \Delta h$$

$$\Delta h + \Delta K.E. = 0$$

$$h_0 = h + \frac{v^2}{2}$$

↑  
Stagnation enthalpy (SP.)

adiabatic flow

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Stagnation temp.

$$h_0 = h + \frac{v^2}{2} \Rightarrow \underline{h_0 - h} = \frac{v^2}{2}$$

For perfect gas -  $\Delta h = C_p \cdot \Delta T$

$$C_p (T_0 - T) = \frac{v^2}{2}$$

$$C_p = \frac{R \cdot \gamma}{\gamma - 1}$$

$$\frac{R \cdot \gamma}{(\gamma - 1)} (T_0 - T) = \frac{v^2}{2}$$

$$C_v = \frac{R}{\gamma - 1}$$

$$\frac{R \cdot \gamma \cdot T}{(\gamma - 1)} \left( \frac{T_0}{T} - 1 \right) = \frac{v^2}{2}$$

$$c = \sqrt{\gamma \cdot R T}$$

$$c^2 = \gamma \cdot R T$$

$$\frac{c^2}{(\gamma - 1)} \left( \frac{T_0}{T} - 1 \right) = \frac{v^2}{2}$$

$$\left( \frac{T_0}{T} - 1 \right) = \frac{\gamma - 1}{c^2} \cdot \frac{v^2}{2}$$

$$M = \frac{v}{c}$$

$$\frac{T_0}{T} - 1 = \frac{\gamma - 1}{2} \cdot M^2$$

$$\frac{T_0}{T} = 1 + \frac{\gamma - 1}{2} M^2 \quad (*)$$

$$\boxed{T_0 = T \left[ 1 + \frac{\gamma - 1}{2} M^2 \right]}$$