

# UNIT 2

# Oscillators

# Introduction to Feedback:

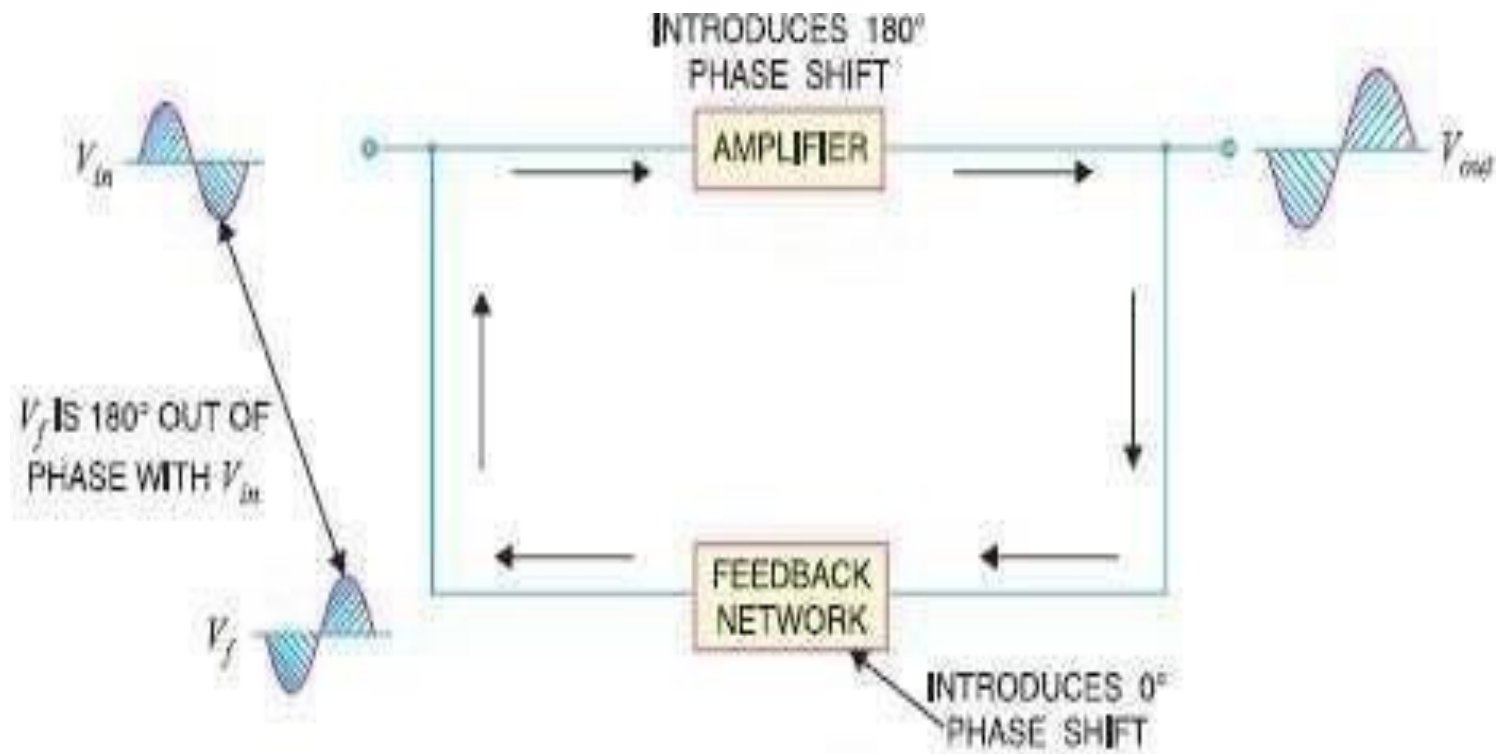
The phenomenon of feeding a portion of the output signal back to the input circuit is known as feedback. The effect results in a dependence between the output and the input and an effective control can be obtained in the working of the circuit. Feedback is of two types.

- Negative Feedback
- Positive Feedback

## Negative or Degenerate feedback:

- In negative feedback, the feedback energy (voltage or current), is out of phase with the input signal and thus opposes it.
- Negative feedback reduces gain of the amplifier. It also reduce distortion, noise and instability.
- This feedback increases bandwidth and improves input and output impedances.
- Due to these advantages, the negative feedback is frequently used in amplifiers.

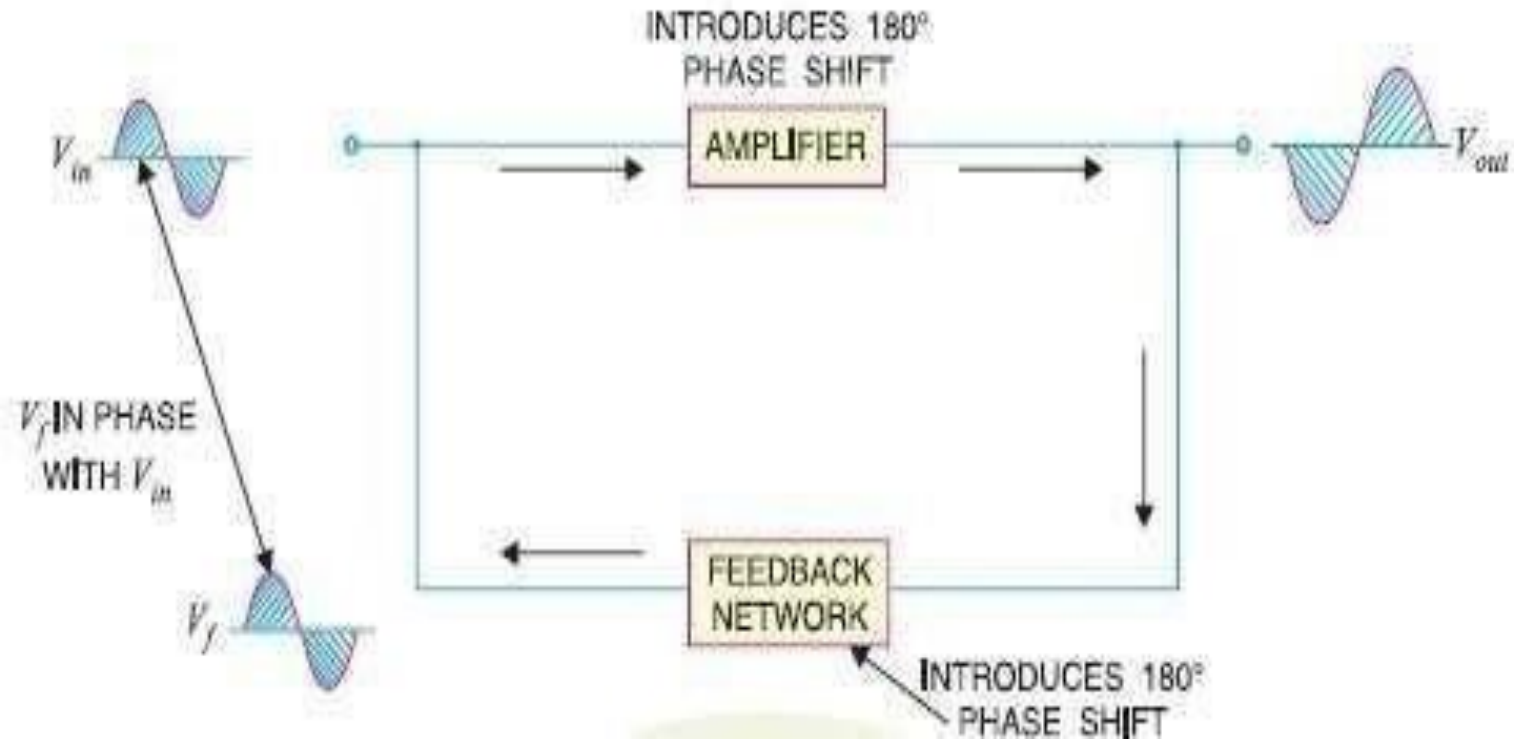
# Negative Feedback



## Positive or regenerate feedback:

- In positive feedback, the feedback energy (voltage or currents), is in phase with the input signal and thus aids it. Positive feedback increases gain of the amplifier also increases distortion, noise and instability.
- Because of these disadvantages, positive feedback is seldom employed in amplifiers. But the positive feedback is used in oscillators.

# Positive Feedback



In the above figure, the gain of the amplifier is represented as  $A$ . The gain of the amplifier is the ratio of output voltage  $V_o$  to the input voltage  $V_i$ . The feedback network extracts a voltage  $V_f = \beta V_o$  from the output  $V_o$  of the amplifier.

This voltage is subtracted for negative feedback, from the signal voltage  $V_s$ . Now,

$$\mathbf{V_i = V_s + V_f = V_s + \beta V_o}$$

The quantity  $\beta = V_f/V_o$  is called as feedback ratio or feedback fraction.



The output  $V_o$  must be equal to the input voltage  $(V_s + \beta V_o)$  multiplied by the gain  $A$  of the amplifier.

Hence,

$$(V_s + \beta V_o)A = V_o$$

$$AV_s + A\beta V_o = V_o$$

$$AV_s = V_o(1 - A\beta)$$

$$V_o/V_s = A/(1 - A\beta)$$

Therefore, the gain of the amplifier with feedback is given by

$$A_f = A/(1 - A\beta)$$

# Comparison Between Positive and Negative Feed Back:

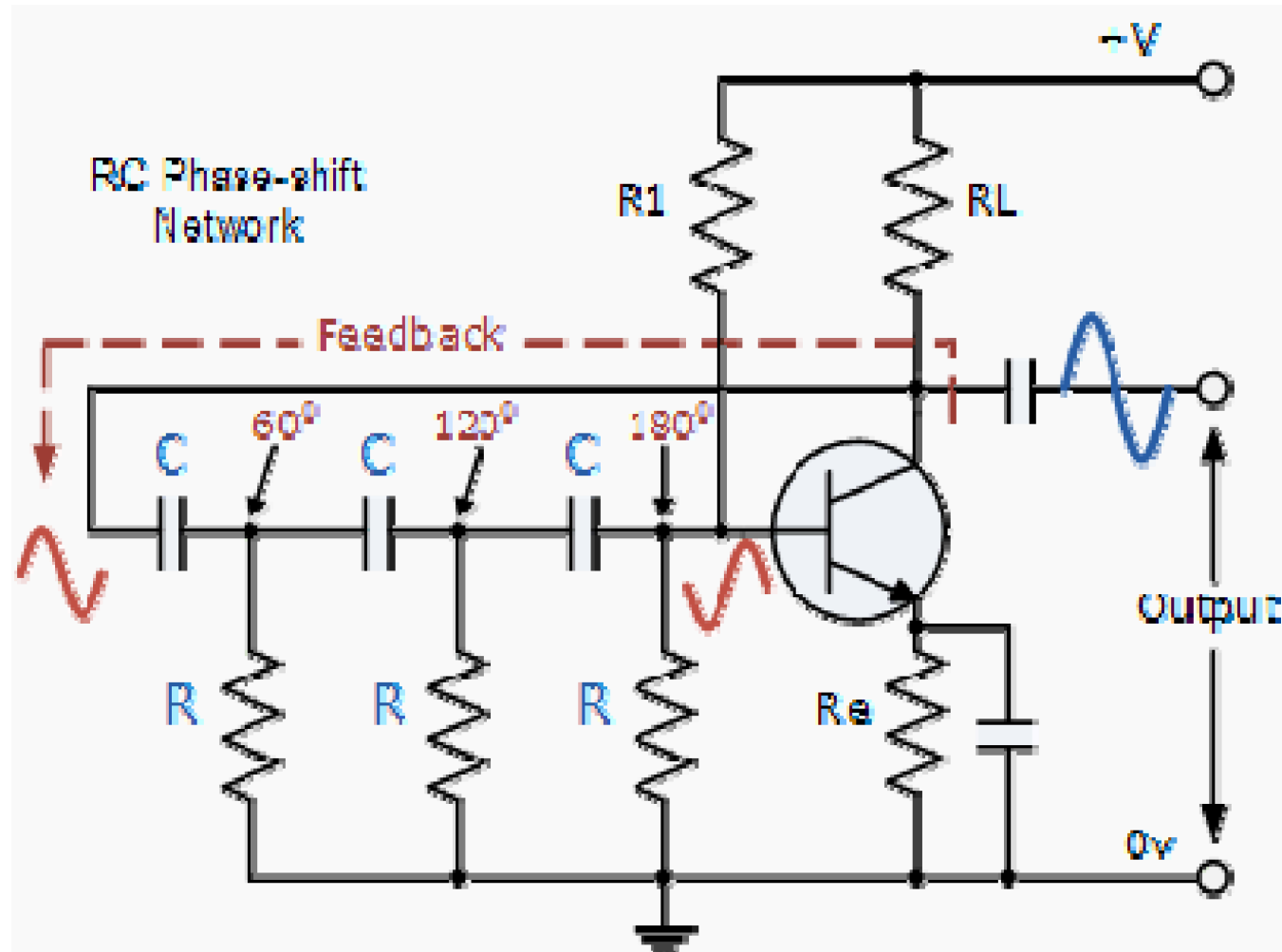
S.No.	Negative Feedback	Positive Feedback
1.	Feedback energy is out phase with their input signal	Feedback energy is in phase with the input signal.
2.	Gain of the amplifier	Gain of the amplifier increases
3.	decreases	Gain stability decreases
4.	Gain stability increases	Noise and distribution increases.
5.	Noise and distortion	Decreases bandwidth
6.	decreases.	Used in Oscillators
	Increase the band width	

Used in amplifiers

# Barkhausen Criteria:

- The condition  $A\beta=1$  is known as Barkhausen criteria. It implies
  - (1) Magnitude of the loop gain  $A\beta = 1$
  - (2) Phase shift over the loop = 0 or 360 degrees.
- Frequency of the noise in the amplifier for which this criteria are satisfied, is the frequency of oscillations.
- By applying this criteria, we can even find the values of transistor parameters, like gain, required for setting in oscillations.

# Basic RC Phase Shift Oscillator:



The **RC Oscillator** which is also called a **Phase Shift Oscillator**, produces a sine wave output signal using regenerative feedback from the resistor-capacitor combination. This regenerative feedback from the RC network is due to the ability of the capacitor to store an electric charge, (similar to the LC tank circuit). This resistor-capacitor feedback network can be connected as shown above to produce a leading phase shift (phase advance network) or interchanged to produce a lagging phase shift (phase retard network) the outcome is still the same as the sine wave oscillations only occur at the frequency at which the overall phase-shift is  $360^\circ$ . By varying one or more of the resistors or capacitors in the phase-shift network, the frequency can be varied and generally this is done using a 3-ganged variable capacitor.

If all the resistors, R and the capacitors, C in the phase shift network are equal in value, then the frequency of oscillations produced by the RC oscillator is given as:

$$f_r = \frac{1}{2\pi RC\sqrt{2N}}$$

Where:

$f$  is the Output Frequency in Hertz

R is the Resistance in Ohms

C is the Capacitance in Farads

N is the number of RC stages. (in our example  $N = 3$ )

Since the resistor-capacitor combination in the **RC Oscillator** circuit also acts as an attenuator producing an attenuation of  $-1/29^{\text{th}}$  ( $V_o/V_i = \beta$ ) per stage, the gain of the amplifier must be sufficient to overcome the losses and in our three mesh network above the **amplifier gain must be greater than 29**. The loading effect of the amplifier on the feedback network has an effect on the frequency of oscillations and can cause the oscillator frequency to be up to 25% higher than calculated. Then the feedback network should be driven from a high impedance output source and fed into a low impedance load such as a common emitter transistor amplifier but better still is to use an Operational Amplifier as it satisfies these conditions perfectly.



## Type of Oscillator:

There are many types of oscillators, but can broadly be classified into two main categories – **Harmonic Oscillators** (also known as Linear Oscillators) and **Relaxation Oscillators**.

In a harmonic oscillator, the energy flow is always from the active components to the passive components and the frequency of oscillations is decided by the feedback path.

Whereas in a relaxation oscillator, the energy is exchanged between the active and the passive components and the frequency of oscillations is determined by the charging and discharging time-constants involved in the process. Further, **harmonic oscillators produce low-distorted sine-wave outputs while the relaxation oscillators generate non-sinusoidal (saw-tooth, triangular or square) wave-forms.**

## **The main types of Oscillators include:**

### **RC Oscillators**

- Wien Bridge Oscillator
- RC Phase Shift Oscillator

### **LC Oscillators**

- Hartley Oscillator
- Colpitts Oscillator
- Clapp Oscillator

### **Crystal Oscillators**

# Wien Bridge Oscillator:

A Wien-Bridge **Oscillator** is a type of phase-shift oscillator which is based upon a Wien-Bridge network comprising of four arms connected in a bridge fashion. Here two arms are purely resistive while the other two arms are a combination of resistors and capacitors. In particular, one arm has resistor and capacitor connected in series ( $R_1$  and  $C_1$ ) while the other has them in parallel ( $R_2$  and  $C_2$ ). This indicates that these two arms of the network behave identical to that of high pass filter or low pass filter, mimicking the behavior of the circuit shown by Figure.

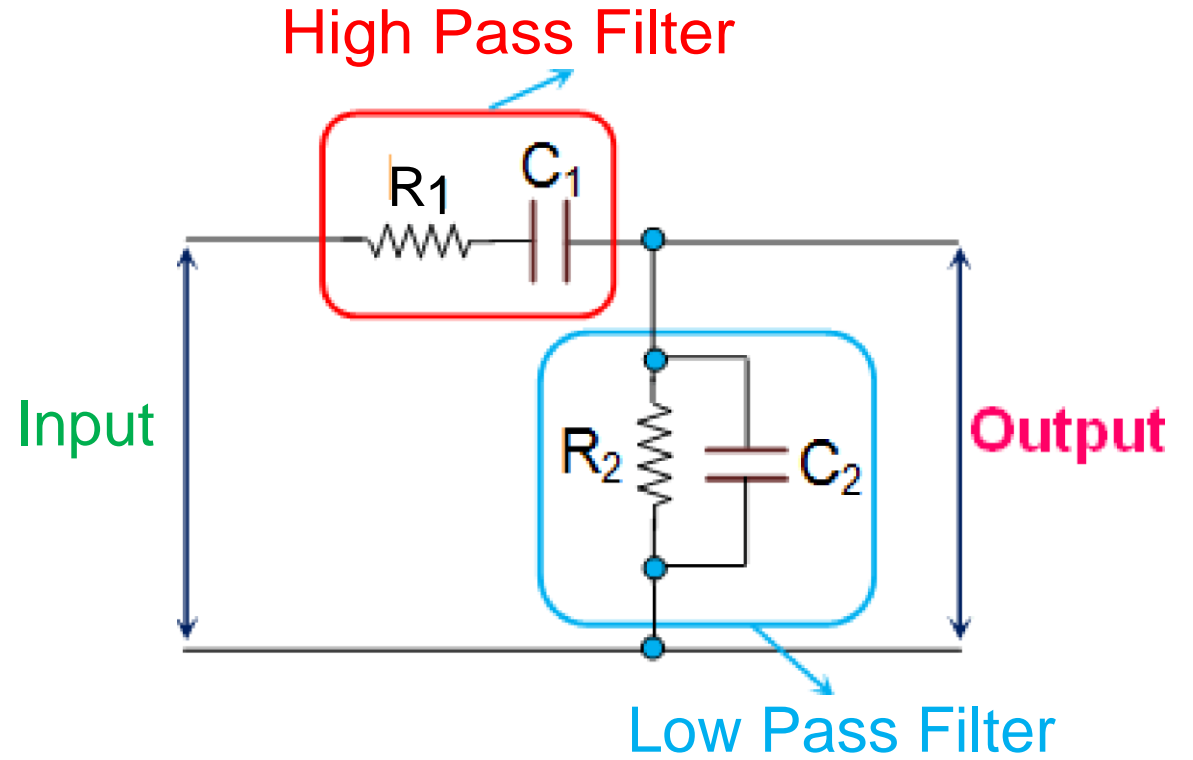
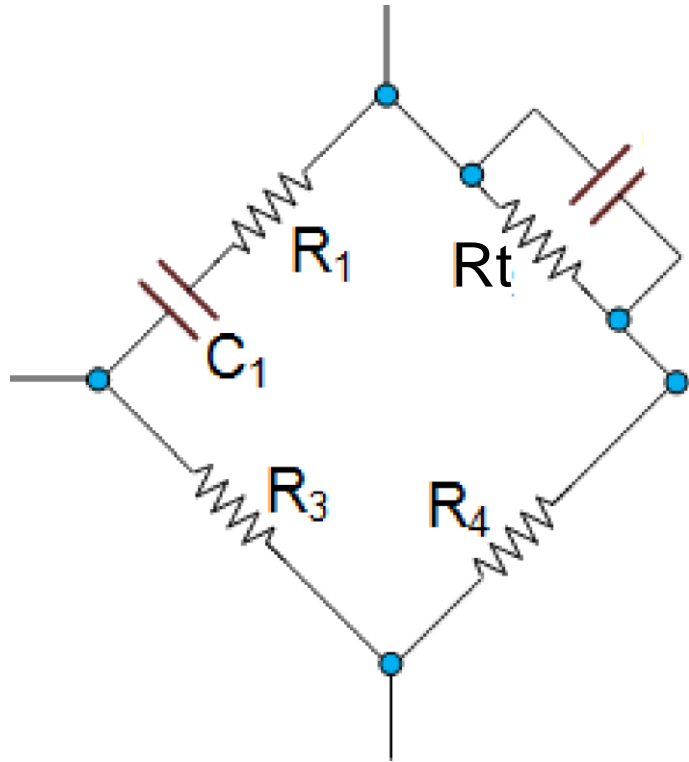


Figure 1 (a) Wien-Bridge Network (b) Two arms of the Wien-Bridge Network

In this circuit, at high frequencies, the reactance of the capacitors  $C_1$  and  $C_2$  will be much less due to which the voltage  $V_0$  will become zero as  $R_2$  will be shorted. Next, at low frequencies, the reactance of the capacitors  $C_1$  and  $C_2$  will become very high.

However even in this case, the output voltage  $V_0$  will remain at zero only, as the capacitor  $C_1$  would be acting as an open circuit. This kind of behavior exhibited by the Wien-Bridge network makes it a lead-lag circuit in the case of low and high frequencies, respectively.

## Wien Bridge Oscillator Frequency Calculation:

Nevertheless, amidst these two high and low frequencies, there exists a particular frequency at which the values of the resistance and the capacitive reactance will become equal to each other, producing the maximum output voltage. This frequency is referred to as resonant frequency. The resonant frequency for a Wein Bridge Oscillator is calculated using the following formul:

$$f_r = \frac{1}{2\pi\sqrt{R_1C_1R_2C_2}}$$

$$\text{if } R_1 = R_2 = R \text{ and } C_1 = C_2 = C$$

$$\text{then } f_r = \frac{1}{2\pi RC}$$

Further, at this frequency, the phase-shift between the input and the output will become zero and the magnitude of the output voltage will become equal to one-third of the input value. In addition, it is seen that the Wien-Bridge will be balanced only at this particular frequency.

In the case of **Wien-Bridge oscillator**, the Wien-Bridge network of Figure 1 will be used in the feedback path as shown in Figure 2. The circuit diagram for a Wien Oscillator using a BJT ([Bipolar Junction Transistor](#)) is shown below:

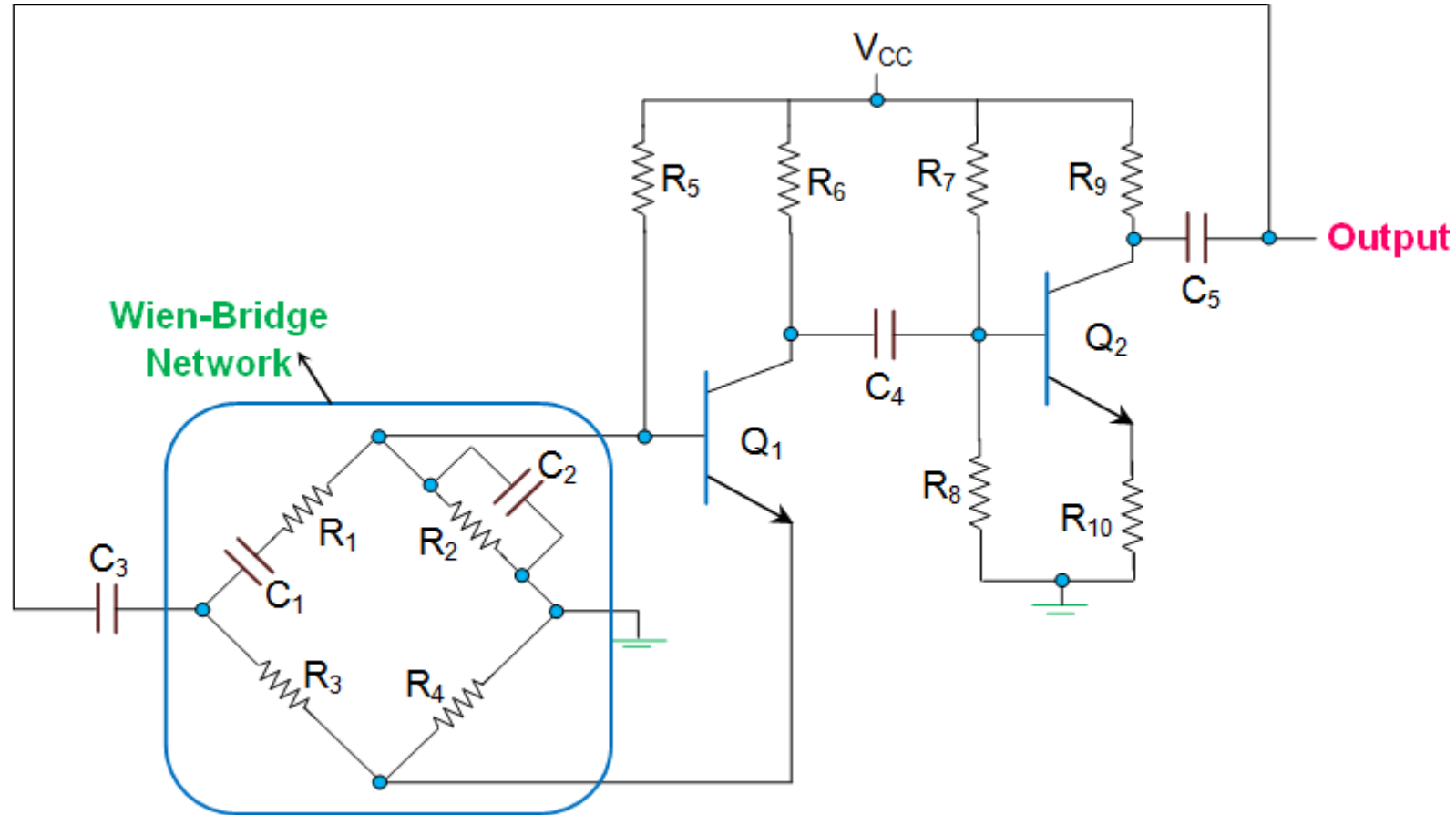


Figure 2 Wien-Bridge Oscillator Using BJT



In these oscillators, the amplifier section will comprise of two-stage amplifier formed by the transistors,  $Q_1$  and  $Q_2$ , wherein the output of  $Q_2$  is back-fed as an input to  $Q_1$  via Wien-Bridge network (shown within the blue enclosure in the figure). Here, the noise inherent in the circuit will cause a change in the base current of  $Q_1$  which will appear at its collector point after being amplified with a phase-shift of  $180^\circ$ .

This is fed as an input to  $Q_2$  via  $C_4$  and gets further amplified and appears with an additional phase-shift of  $180^\circ$ . This makes the net phase-difference of the signal fed back to the Wien-Bridge network to be  $360^\circ$ , satisfying phase-shift criterion to obtain sustained oscillations.

However, this condition will be satisfied only in the case of resonant frequency, due to which the Wien-Bridge oscillators will be highly selective in terms of frequency, leading to a frequency-stabilized design.

Wien-bridge oscillators can even be designed using Op-Amps as a part of their amplifier section, as shown by Figure 3. However it is to be noted that, here, the Op-Amp is required to act as a non-inverting amplifier as the Wien-Bridge network offers zero phase-shift. Further, from the circuit, it is evident that the output voltage is fed back to both inverting and non-inverting input terminals.

At resonant frequency, the voltages applied to the inverting and non-inverting terminals will be equal and in-phase with each other. However, even here, the voltage gain of the amplifier needs to be greater than 3 to start oscillations and equal to 3 to sustain them. In general, these kind of Op-Amp-based **Wien Bridge Oscillators** cannot operate above **1 MHz** due to the limitations imposed on them by their open-loop gain.

Wien-Bridge  
Network

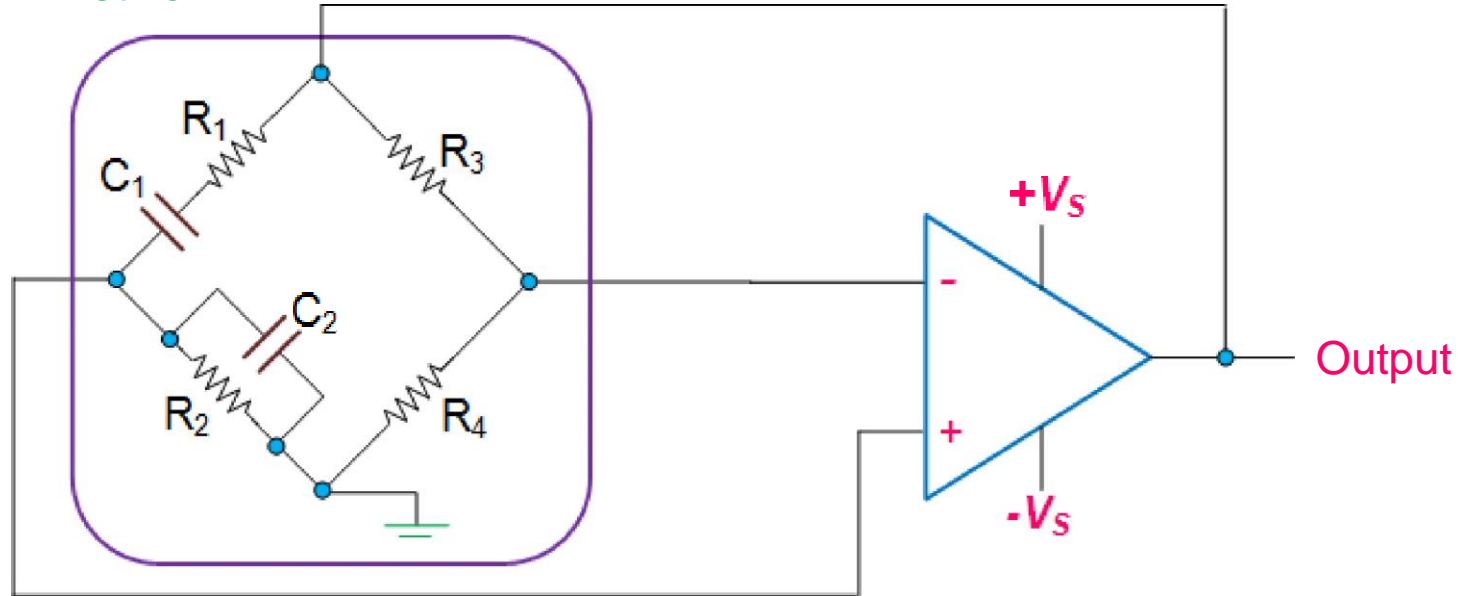


Figure 3 Wien-Bridge Oscillator Using an Op-Amp

Wien-Bridge networks are low frequency oscillators which are used to generate audio and sub-audio frequencies ranging between 20 Hz to 20 KHz. Further, they provide stabilized, low distorted sinusoidal output over a wide range of frequency which can be selected using decade resistance boxes. In addition, the oscillation frequency in this kind of circuit can be varied quite easily as it just needs variation of the capacitors  $C_1$  and  $C_2$ . However these oscillators require large number of circuit components and can be operated up to a certain maximum frequency only.

## RC Phase Shift Oscillator:

*RC phase-shift oscillators* use resistor-capacitor (RC) network (Figure 1) to provide the phase-shift required by the feedback signal. They have excellent frequency stability and can yield a pure sine wave for a wide range of loads.

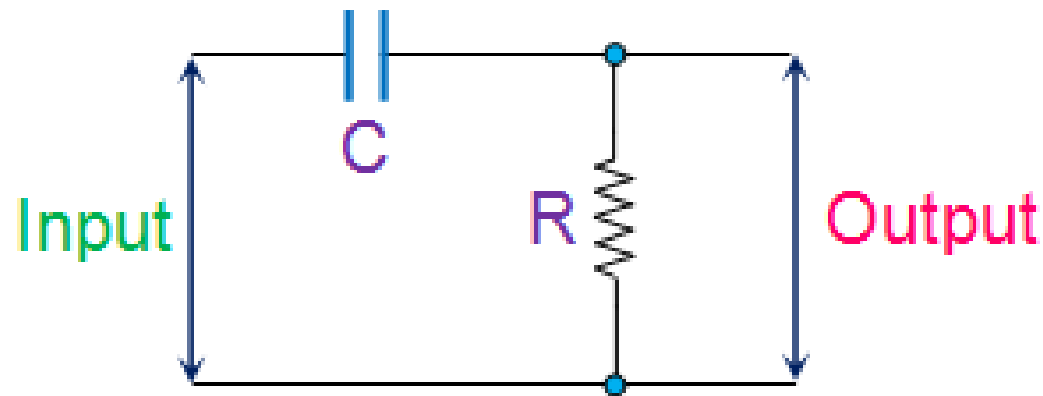


Figure 1 RC Phase-Shift Network

Ideally a simple RC network is expected to have an output which leads the input by 90°. However, in reality, the phase-difference will be less than this as the [capacitor](#) used in the circuit cannot be ideal. Mathematically the phase angle of the RC network is expressed as

$$\varphi = \tan^{-1} \frac{X_C}{R}$$

Where,  $X_C = 1/(2\pi fC)$  is the reactance of the capacitor C and R is the [resistor](#). In [oscillators](#), these kind of RC phase-shift networks, each offering a definite phase-shift can be cascaded so as to satisfy the phase-shift condition led by the Barkhausen Criterion.

One such example is the case in which **RC phase-shift oscillator** is formed by cascading three RC phase-shift networks, each offering a phase-shift of  $60^\circ$ , as shown by Figure 2.

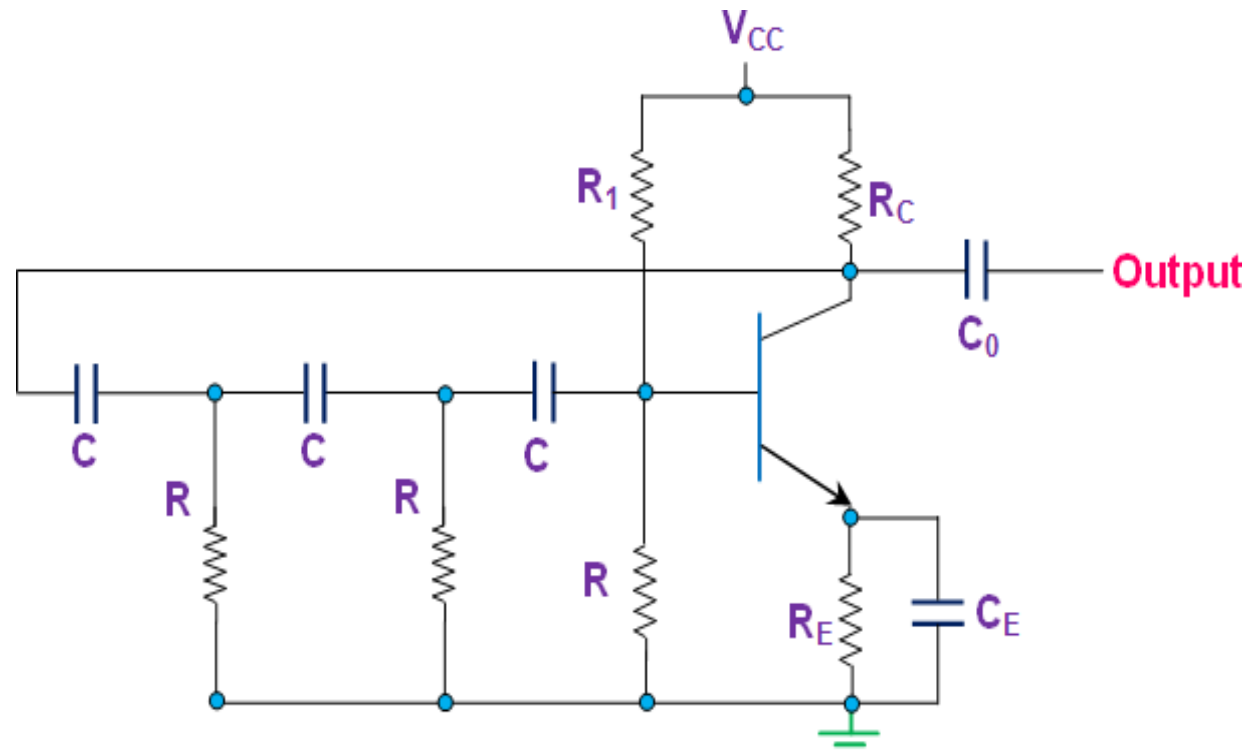


Figure 2 RC Phase-Shift Oscillator Using BJT

Here the collector resistor  $R_c$  limits the collector current of the transistor, resistors  $R_1$  and  $R$  (nearest to the transistor) form the voltage divider network while the emitter resistor  $R_E$  improves the stability. Next, the capacitors  $C_E$  and  $C_o$  are the emitter bypass capacitor and the output DC decoupling capacitor, respectively. Further, the circuit also shows three RC networks employed in the feedback path.

This arrangement causes the output waveform to shift by  $180^\circ$  during its course of travel from output terminal to the base of the transistor. Next, this signal will be shifted again by  $180^\circ$  by the transistor in the circuit due to the fact that the phase-difference between the input and the output will be  $180^\circ$  in the case of common emitter configuration. This makes the net phase-difference to be  $360^\circ$ , satisfying the phase-difference condition.



One more way of satisfying the phase-difference condition is to use four RC networks, each offering a phase-shift of 45°. Hence it can be concluded that the **RC phase-shift oscillators** can be designed in many ways as the number of RC networks in them is not fixed. However it is to be noted that, although an increase in the number of stages increases the frequency stability of the circuit, it also adversely affects the output frequency of the oscillator due to the loading effect.

The generalized expression for the frequency of oscillations produced by a **RC phase-shift oscillator** is given by

$$f = \frac{1}{2\pi RC\sqrt{2N}}$$

Where, N is the number of RC stages formed by the resistors R and the capacitors C.

Further, as is the case for most type of oscillators, even the RC phase-shift oscillators can be designed using an OpAmp as its part of the amplifier section (Figure 3). Nevertheless, the mode of working remains the same while it is to be noted that, here, the required phase-shift of  $360^\circ$  is offered collectively by the RC phase-shift networks and the Op-Amp working in inverted configuration.

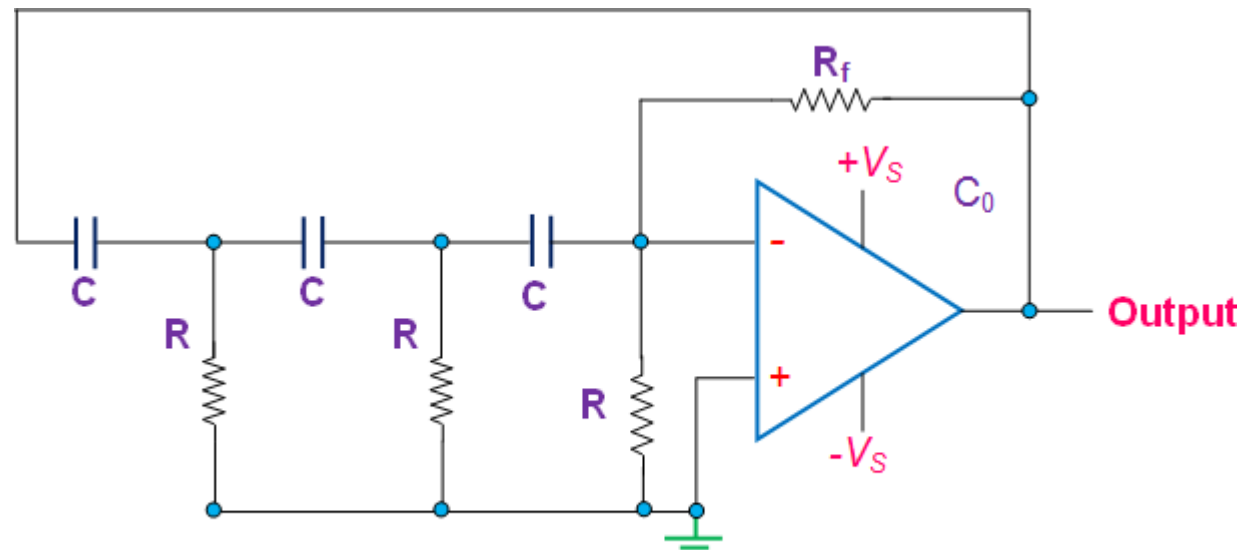


Figure 3 RC Phase-Shift Oscillator Using an Op-Amp

Further, it is to be noted that the frequency of the RC phase-shift oscillators can be varied by changing either the resistors or the [capacitors](#). However, in general, the [resistors](#) are kept constant while the capacitors are gang-tuned. Next, by comparing the **RC phase-shift oscillators** with LC oscillators, one can note that, the former uses more number of circuit components than the latter one. Thus, **the output frequency produced from the RC oscillators can deviate much from the calculated value rather than in the case of LC oscillators.** Nevertheless, they are used as local oscillators for synchronous receivers, musical instruments and as low and/or audio-frequency generators.

# LC- Oscillators

LC Oscillator	Z1	Z2	Z3
Hartley Oscillator	L	L	C
Colpitts Oscillator	C	C	L
Clapp Oscillator	C	C	L-C

# Hartley Oscillator:

**Hartley Oscillator** is a type of harmonic [oscillator](#) which was invented by Ralph Hartley in 1915. These are the Tuned Circuit Oscillators which are used to produce the waves in the range of **radio frequency and hence are also referred to as RF Oscillators**. Its frequency of oscillation is decided by its tank circuit which has a [capacitor](#) connected in parallel with the two serially connected [inductors](#), as shown by Figure 1.

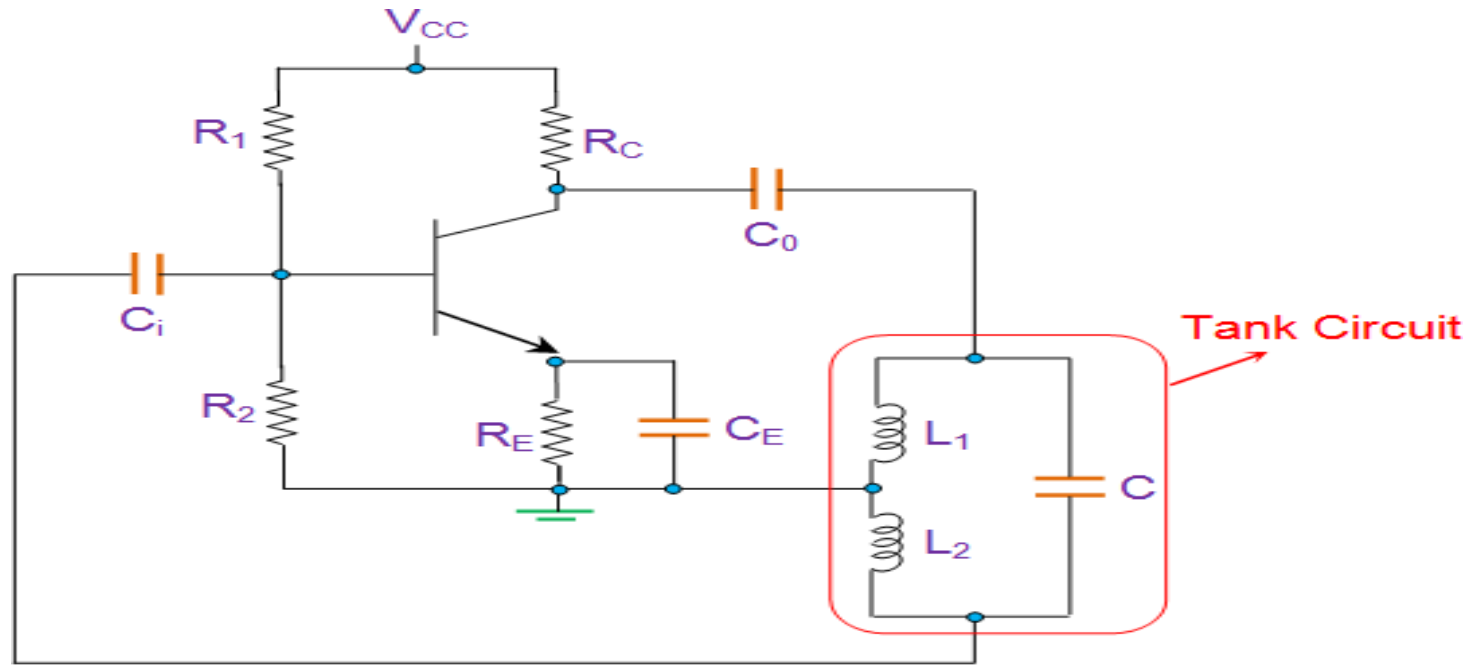


Figure 1 Hartley Oscillator

Here the  $R_C$  is the collector resistor while the emitter [resistor](#)  $R_E$  forms the stabilizing network. Further the resistors  $R_1$  and  $R_2$  form the [voltage divider](#) bias network for the [transistor](#) in common-emitter CE configuration. Next, the capacitors  $C_i$  and  $C_o$  are the input and output decoupling capacitors while the emitter capacitor  $C_E$  is the bypass capacitor used to bypass the amplified AC signals. All these components are identical to those present in the case of a [common-emitter amplifier](#) which is biased using a voltage divider network. However, Figure 1 also shows one more set of components viz., the inductors  $L_1$  and  $L_2$  and the [capacitor](#)  $C$  which form the tank circuit (shown in red enclosure).

On switching ON the power supply, the transistor starts to conduct, leading to an increase in the collector current,  $I_C$  which charges the capacitor C. On acquiring the maximum charge feasible, C starts to discharge via the inductors  $L_1$  and  $L_2$ . This charging and discharging cycles result in the damped oscillations in the tank circuit. The oscillation current in the tank circuit produces an AC voltage across the inductors  $L_1$  and  $L_2$  which are out of phase by  $180^\circ$  as their point of contact is grounded.

Further from the figure, it is evident that the output of the amplifier is applied across the inductor  $L_1$  while the feedback voltage drawn across  $L_2$  is applied to the base of the transistor. Thus one can conclude that the output of the amplifier is in-phase with the tank circuit's voltage and supplies back the energy lost by it while the energy fed back to amplifier circuit will be out-of-phase by  $180^\circ$ . The feedback voltage which is already  $180^\circ$  out-of-phase with the transistor is provided by an additional  $180^\circ$  phase-shift due to the transistor action. Hence the signal which appears at the transistor's output will be amplified and will have a net phase-shift of  $360^\circ$ .

At this state, if one makes the gain of the circuit to be slightly greater than the feedback ratio given by

$$\beta = \frac{L_1}{L_2}; \text{ if the coils are wound on different cores}$$

$$\beta = \frac{L_1 + M}{L_2 + M}$$

(if the coils are wound on the same core with M indicating the [mutual inductance](#))

then the circuit generates the oscillations which can be sustained by maintaining the gain of the circuit to be equal to that of the feedback ratio. This causes the circuit in Figure 1 to act as an oscillator as it would then satisfy both the conditions of the Barkhausen criteria.

The frequency of such an [oscillator](#) is given as

$$F = \frac{1}{2\pi\sqrt{L_{eff}C}}$$

Where,  $L_{eff}$  is the effective series inductance which is expressed as

$$L_{eff} = L_1 + L_2; \text{ if the coils are wound on different cores}$$

$$L_{eff} = L_1 + L_2 + 2M; \text{ if the coils are wound on the same core}$$



**Hartley oscillators** are available in many different configurations including series-or shunt-fed, common-emitter or common-base configured, and [BJT](#) (Bipolar Junction Transistor) or [FET](#) (Field Effect Transistor) amplifier based. Further it is to be noted that the transistor-based amplifier section of Figure 1 can even be replaced by an amplifier of any other kind like that of an [inverting amplifier](#) formed by an [Op-Amp](#) as shown by Figure 2. The working of this kind of oscillator is similar to that of the one shown earlier. However, here, the gain of the oscillator can be individually adjusted using the feedback [resistor](#)  $R_f$  due to the fact that the gain of the inverting amplifier is given as  $-R_f / R_1$ . From this, it can be noted that, in this case, the gain of the circuit is less dependent on the circuit elements of the tank circuit. This increases the stability of the oscillator in terms of its frequency.

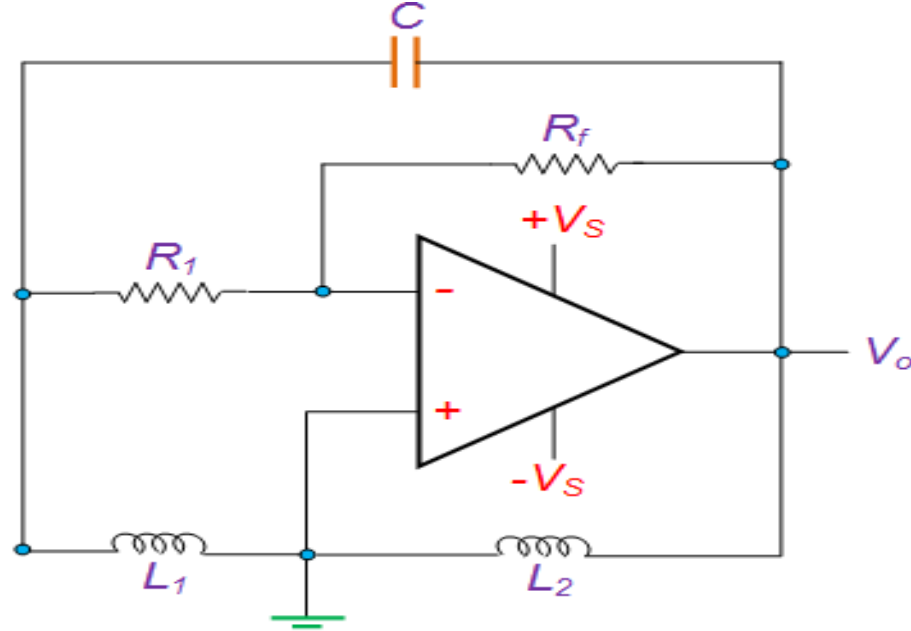


Figure 2 Hartley Oscillator Using an Op-Amp

**Hartley Oscillators** are advantageous as **they are easy-tunable circuits** with a very few components including a [capacitor](#) and either two [inductors](#) or a tapped coil. This results in a constant amplitude output throughout its wide operational frequency range which typically **ranges from 20 KHz to 30 MHz**. However, this kind of oscillator is **not suitable for low frequency** as it would result in a **large-sized inductor which makes the circuit bulky**. Further, the output of **Hartley Oscillator** has high content of [harmonics](#) in it and hence does not suit for the applications which require pure sine wave.

## Colpitts Oscillator:

**Colpitts Oscillator** is a type of LC oscillator which falls under the category of Harmonic Oscillator and was invented by Edwin Colpitts in 1918. Figure 1 shows a typical Colpitts oscillator with a tank circuit in which an inductor  $L$  is connected in parallel to the serial combination of capacitors  $C_1$  and  $C_2$  (shown by the red enclosure).

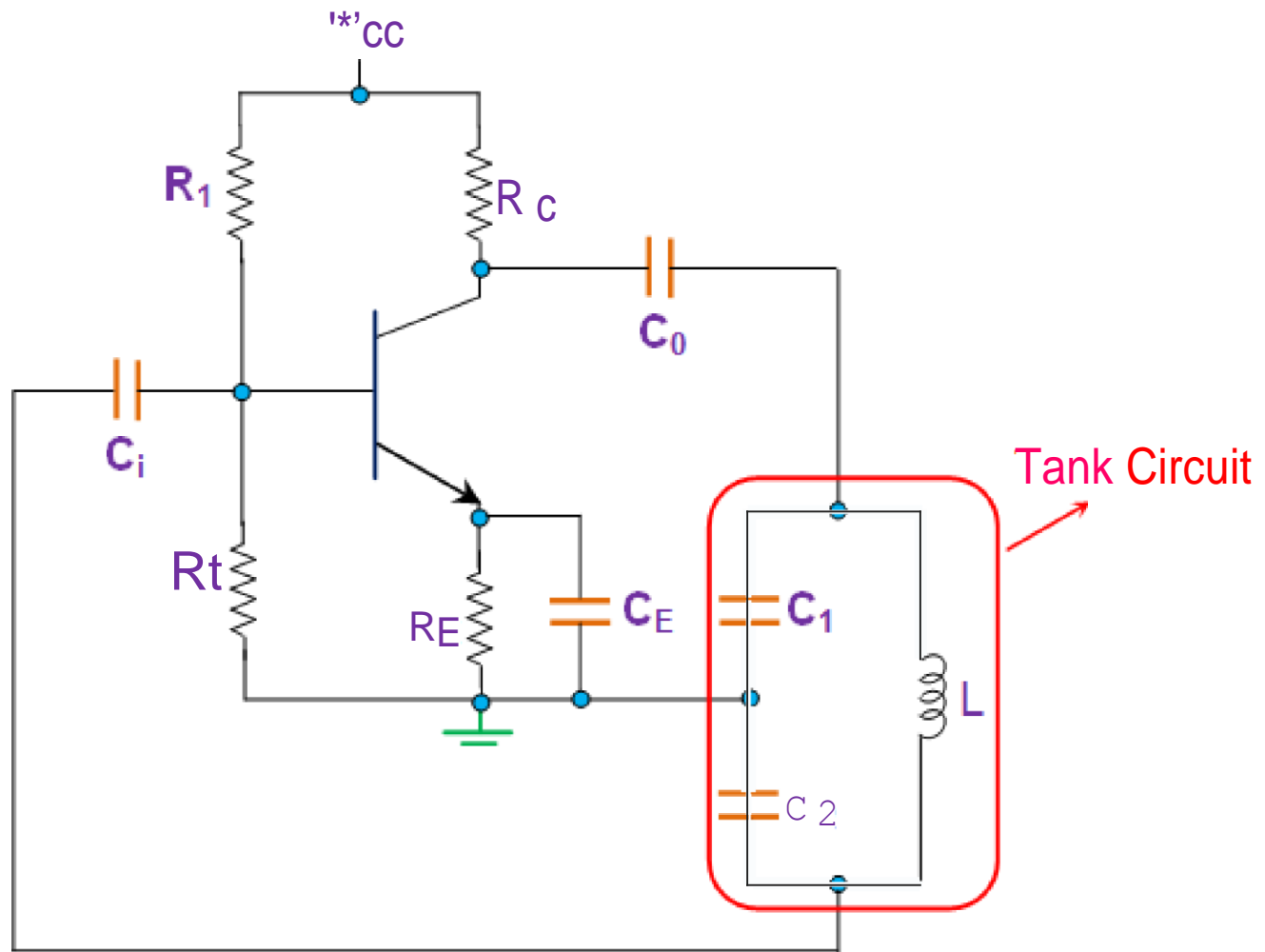


Figure 1 Colpitts Oscillator

Other components in the circuit are the same as that found in the case of common-emitter CE which is biased using a voltage divider network i.e.  $R_C$  is the collector resistor,  $R_E$  is the emitter resistor which is used to stabilize the circuit and the resistors  $R_1$  and  $R_2$  form the voltage divider bias network. Further, the capacitors  $C_i$  and  $C_o$  are the input and output decoupling capacitors while the emitter capacitor  $C_E$  is the bypass capacitor used to bypass the amplified AC signals.

Here, as the power supply is switched ON, the transistor starts to conduct, increasing the collector current  $I_C$  due to which the capacitors  $C_1$  and  $C_2$  get charged. On acquiring the maximum charge feasible, they start to discharge via the inductor  $L$ . During this process, the electrostatic energy stored in the capacitor gets converted into magnetic flux which in turn is stored within the inductor in the form of electromagnetic energy. Next, the inductor starts to discharge which charges the capacitors once again. Likewise, the cycle continues which gives rise to the oscillations in the tank circuit.

Further the figure shows that the output of the amplifier appears across  $C_1$  and thus is in-phase with the tank circuit's voltage and makes-up for the energy lost by re-supplying it. On the other hand, the voltage feedback to the transistor is the one obtained across the capacitor  $C_2$ , which means the feedback signal is out-of-phase with the voltage at the transistor by  $180^\circ$ . This is due to the fact that the voltages developed across the capacitors  $C_1$  and  $C_2$  are opposite in polarity as the point where they join is grounded. Further, this signal is provided with an additional phase-shift of  $180^\circ$  by the transistor which results in a net phase-shift of  $360^\circ$  around the loop, satisfying the phase-shift criterion of Barkhausen principle.

At this state, the circuit can effectively act as an [oscillator](#) producing sustained oscillations by carefully monitoring the **feedback ratio given by  $(C_1 / C_2)$** . The frequency of such a **Colpitts Oscillator** depends on the components in its tank circuit and is given by

$$F = \frac{1}{2\pi\sqrt{LC_{eff}}}$$

Where, the  $C_{eff}$  is the effective capacitance of the capacitors expressed as

$$\frac{C_1 C_2}{C_1 + C_2}$$

As a result, these oscillators can be tuned either by varying their [inductance](#) or the [capacitance](#). However the variation of L does not yield a smooth variation. Hence they are usually tuned by varying the capacitances which are generally ganged, due to which a change in any one of them changes both of them. Nevertheless, the process is tedious and requires special large-valued capacitor. Thus, the Colpitts oscillators are seldom preferred in the applications where in the frequency varies but are more popular as fixed frequency oscillators due to their simple design. Further they offer better stability in comparison with the [Hartley Oscillators](#) as they are exempted from the [mutual inductance](#) effect present in-between the two inductors of the latter case.



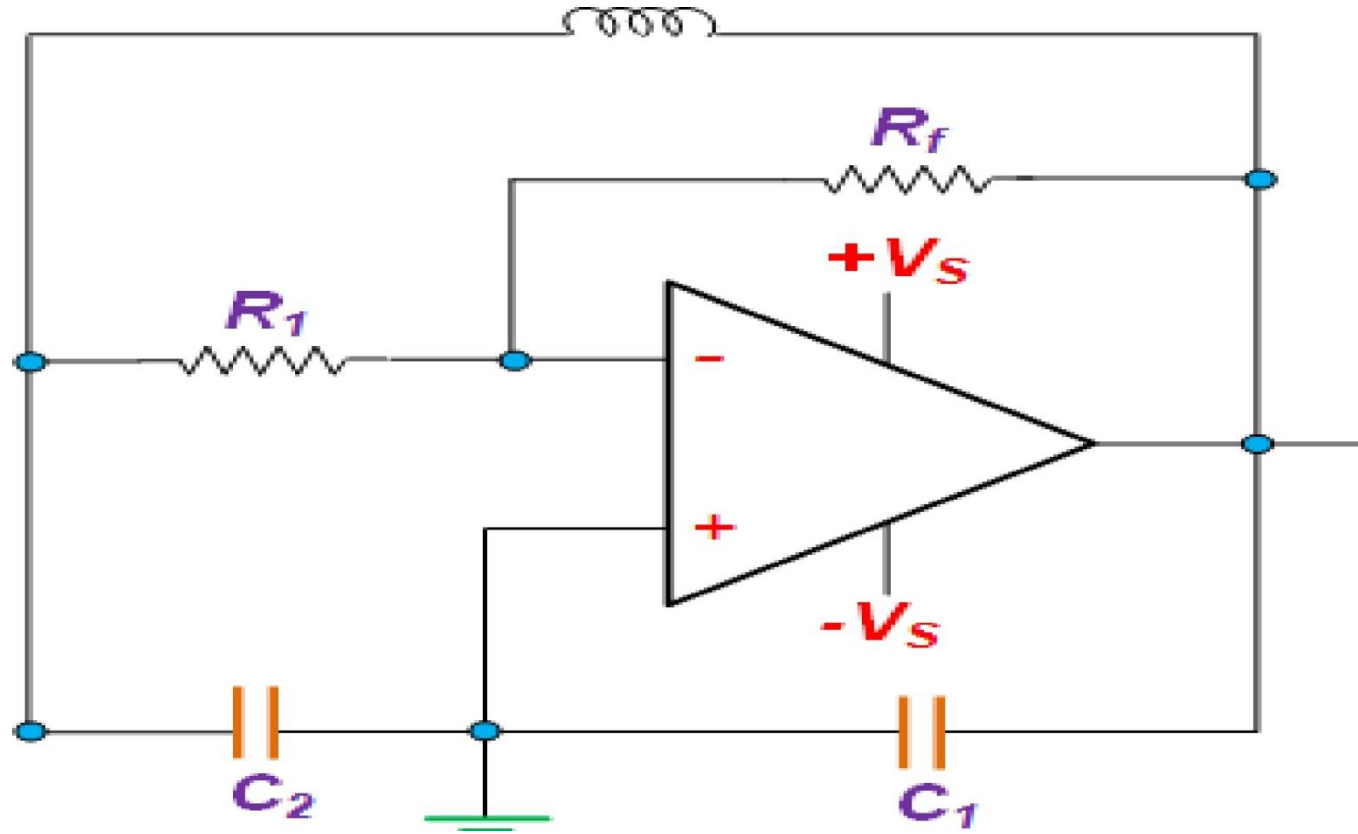


Figure 2 Colpitts Oscillator Using an op-Amp

Apart from the [BJT](#)-based Colpitts Oscillator shown, they are also realizable using valves or [FET](#) (Field Effect Transistor) or Op-Amp. Figure 2 shows such a **Colpitts oscillator** which uses an [Op-Amp](#) in inverting configuration in its amplifier section while the tank circuit remains similar to that in the case of Figure 1. This kind of circuit functions almost analogous to that of the one explained earlier. However, here the gain of the oscillator can be adjusted individually just by using the feedback resistor  $R_f$ , as the gain of the [inverting amplifier](#) is given as  $-R_f / R_1$ . From this, it can be noted that, in this case, the gain of the circuit is less dependent on the circuit elements of the tank circuit.

Typically, the operating frequency of the **Colpitts oscillators** ranges from 20 KHz to 300 MHz. However they can even be used for microwave applications as their capacitors provide low reactance path for the high-frequency signals. This results in better frequency stability as well as a better sinusoidal output waveform. Moreover, they are also extensively used as surface acoustical wave (SAW) resonators, [sensors](#) and in mobile and communication systems.

# Clapp Oscillator:

*Clapp oscillator* is a variation of [Colpitts oscillator](#) in which an additional capacitor ( $C_3$ ) is added into the tank circuit to be in series with the [inductor](#) in it, as shown by Figure 1.

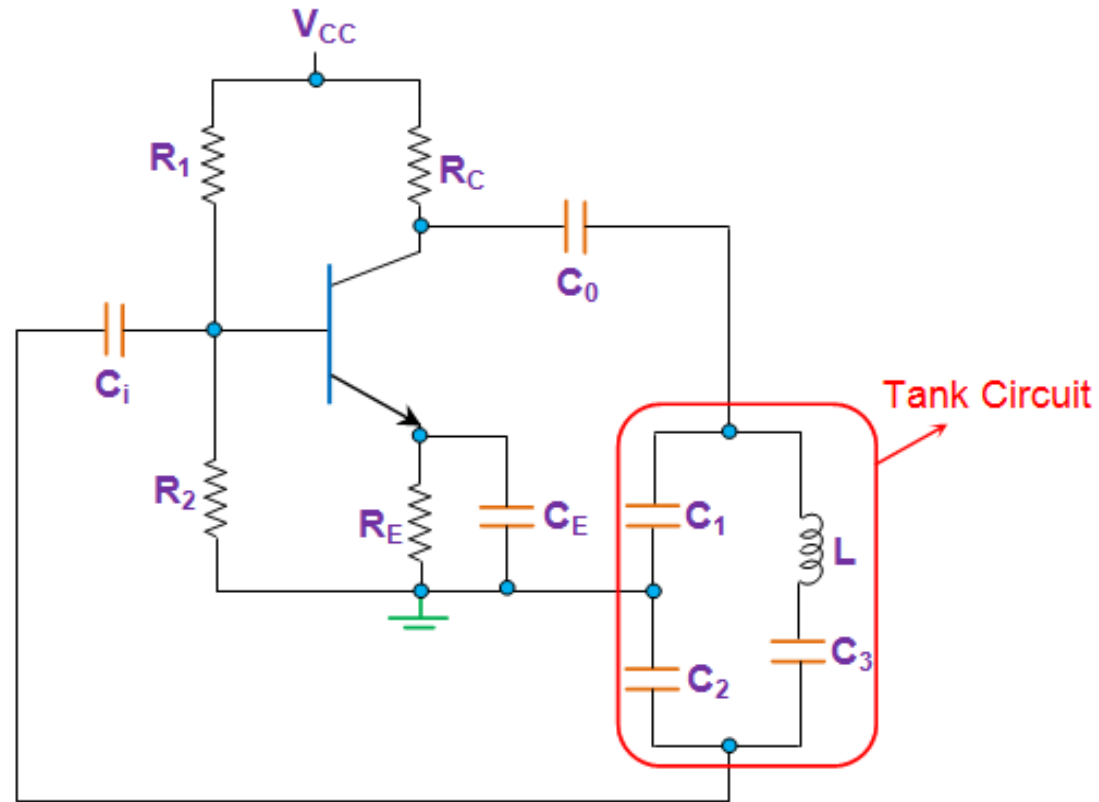


Figure 1 Clapp Oscillator

Apart from the presence of an extra capacitor, all other components and their connections remain similar to that in the case of Colpitts oscillator.

Hence, the working of this circuit is almost identical to that of the Colpitts, where the feedback ratio governs the generation and sustainability of the oscillations. However the frequency of oscillation in the case of **Clapp oscillator** is given by

$$f = \frac{1}{2\pi \sqrt{L \left( \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \right)}}$$

Usually the value of  $C_3$  is chosen to be much smaller than the other two capacitors. This is because, at higher frequencies, smaller the  $C_3$ , larger will be the inductor, which eases the implementation as well as reduces the influence of stray inductance. Nevertheless, the value of  $C_3$  is to be chosen with utmost care. This is because, if it is chosen to be very small, then the oscillations will not be generated as the L-C branch will fail to have a net inductive reactance. However, here it is to be noted that when  $C_3$  is chosen to be smaller in comparison with  $C_1$  and  $C_2$ , the net capacitance governing the circuit will be more dependent on it.

Thus the equation for the frequency can be approximated as

$$f = \frac{1}{2\pi\sqrt{LC_3}}$$

Further, the presence of this extra capacitance will make the **Clapp oscillator** preferable over Colpitts when there is a need to vary the frequency as is the case with **Variable Frequency Oscillator (VCO)**. The reason behind this can be explained as follows.

In the case of Colpitts oscillator, the capacitors  $C_1$  and  $C_2$  need to be varied in order to vary its frequency of operation. However during this process, even the feedback ratio of the oscillator changes which in turn affects its output waveform. One solution to this problem is to make both  $C_1$  and  $C_2$  to be fixed in nature while achieve the variation in frequency using a separate variable capacitor. As could be guessed, this is what the  $C_3$  does in the case of **Clapp oscillator**, which in turn makes it more stable over Colpitts in terms of frequency. The frequency stability of the circuit can be even more increased by enclosing the entire circuit in a chamber with constant temperature and by using a Zener diode to ensure constant supply voltage.

In addition, it is to be noted that the values of the capacitors  $C_1$  and  $C_2$  are prone to the effect of stray capacitances unlike that of  $C_3$ . This means that the resonant frequency of the circuit would be affected by the stray capacitances if one had a circuit with just  $C_1$  and  $C_2$ , as in the case of Colpitts oscillator. However if there is  $C_3$  in the circuit, then the changes in the values of  $C_1$  and  $C_2$  would not vary the resonant frequency much, as the dominant term would then be  $C_3$ .

Next, it is seen that the **Clapp oscillators** are comparatively compact as they employ a relatively small [capacitor](#) to tune the oscillator over a wide frequency band. This is because, here, even a slight change in the value of the capacitance varies the frequency of the circuit upto a great extent. Further they exhibit high Q-factor with a high L/C ratio and lesser circulating [current](#) in comparison with [Colpitts oscillators](#). Lastly it is to be noted that these [oscillators](#) are highly reliable and are hence preferred inspite of having a limited range of frequency of operation.

# Crystal Oscillators:

Crystal Oscillators can be designed by connecting the crystal into the circuit such that it offers low impedance when operated in series-resonant mode (Figure 2a) and high impedance when operated in anti-resonant or parallel resonant mode (Figure 2b).

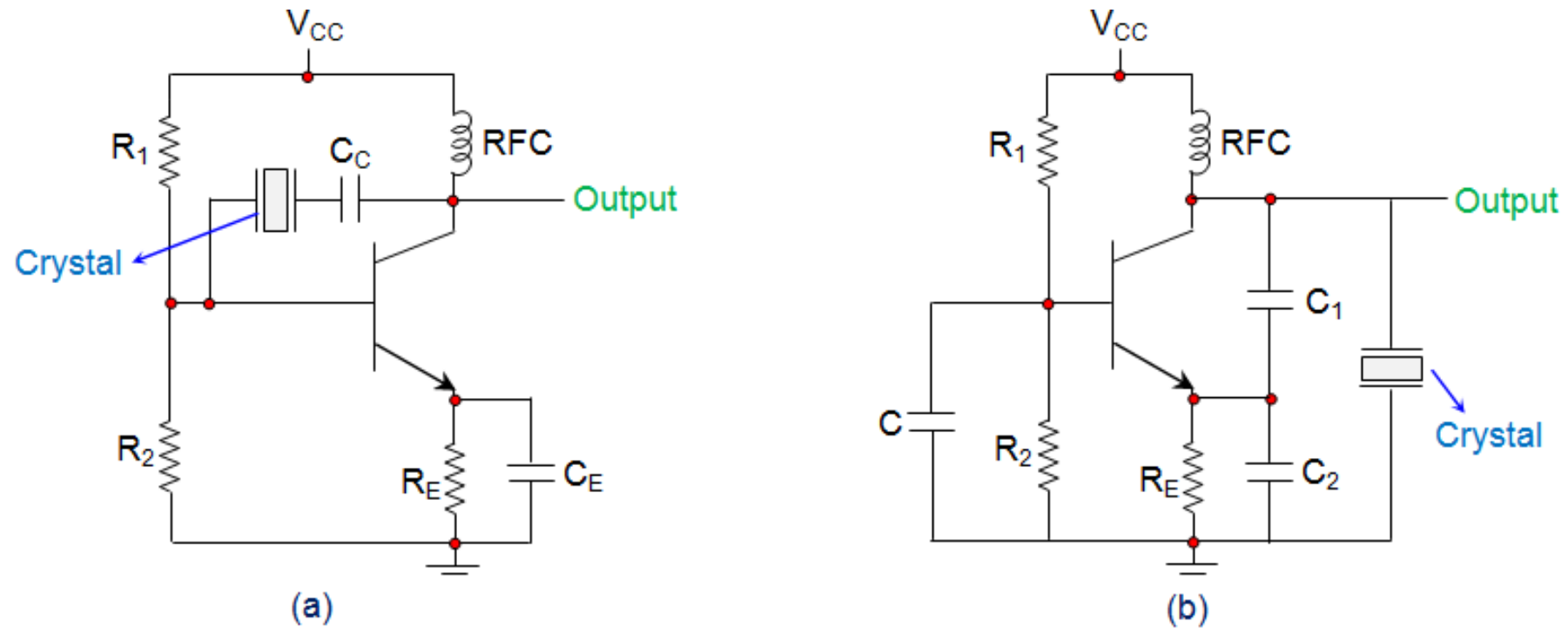


Figure 2 Crystal Oscillator Operating in (a) Series Resonance (b) Parallel Resonance



In the circuits shown, the [resistors](#)  $R_1$  and  $R_2$  form the [voltage divider](#) network while the emitter resistor  $R_E$  stabilizes the circuit. Further,  $C_E$  (Figure 2a) acts as an AC bypass capacitor while the coupling capacitor  $C_C$  (Figure 2a) is used to block DC signal propagation between the collector and the base terminals. Next, the capacitors  $C_1$  and  $C_2$  form the capacitive voltage divider network in the case of Figure 2b. In addition, there is also a Radio Frequency Coil (RFC) in the circuits (both in Figure 2a and 2b) which offers dual advantage as it provides even the DC bias as well as frees the circuit-output from being affected by the AC signal on the power lines.

**On supplying the power to the [oscillator](#), the amplitude of the oscillations in the circuit increases until a point is reached wherein the nonlinearities in the amplifier reduce the loop gain to unity. Next, on reaching the steady-state, the crystal in the feedback loop highly influences the frequency of the operating circuit. Further, here, the frequency will self-adjust so as to facilitate the crystal to present a reactance to the circuit such that the Barkhausen phase requirement is fulfilled.**

**In general, the frequency of the crystal oscillators will be fixed to be the crystal's fundamental or characteristic frequency which will be decided by the physical size and shape of the crystal.** However, if the crystal is non-parallel or of non-uniform thickness, then it might resonate at multiple frequencies, resulting in harmonics. Further, the crystal oscillators can be tuned to either even or odd harmonic of the fundamental frequency, which are called Harmonic and Overtone Oscillators, respectively. An example for this is the case where the parallel resonance frequency of the crystal is decreased or increased by adding a capacitor or an inductor across the crystal, respectively.

The typical operating range of the crystal oscillators is from **40 KHz to 100 MHz** wherein the low frequency oscillators are designed using OpAmps while the high frequency-ones are designed using the [transistors](#) ([BJTs](#) or [FETs](#)). **The frequency of oscillations generated by the circuit is decided by the series resonant frequency of the crystal and will be unaffected by the variations in supply [voltage](#), transistor parameters, etc. As a result, crystal oscillators exhibit high Q-factor with excellent frequency stability, making them most suitable for high-frequency applications.** However care should be taken so as to drive the crystal with optimum power only. This is because, if too much of power is delivered to the crystal, then the parasitic resonances might be excited in the crystal which leads to unstable resonant frequency. Further even its output waveform might be distorted due to the degradation in its phase noise performance. Moreover it can even result in the destruction of the device (crystal) due to overheat.

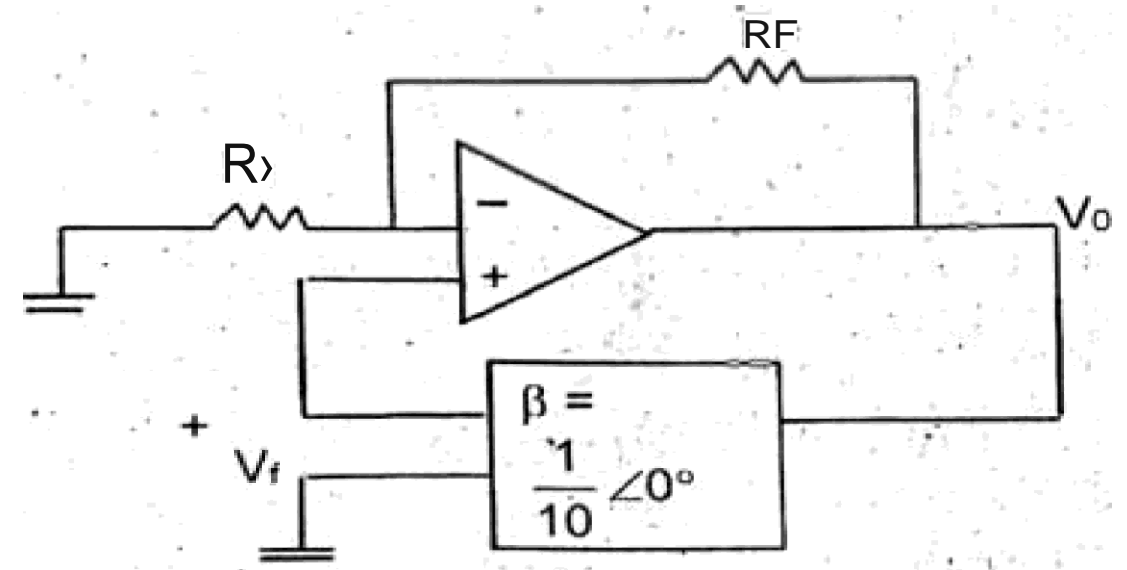
## Applications:

**Crystal oscillators** are compact in size and are of low cost due to which they are extensively used in electronic warfare systems, communication systems, guidance systems, microprocessors, microcontrollers, space tracking systems, measuring instruments, medical devices, computers, digital systems, instrumentation, phase locked loop systems, modems, [sensors](#), disk drives, marine systems, telecommunications, engine controlling systems, clocks, Global Positioning Systems (GPS), cable television systems, video cameras, toys, video games, radio systems, cellular phones, timers, etc.

# **GATE Questions with Solutions**

Relation

between  $R_1$  and  $R_F$  for sustained Oscillations if  $\phi = 180^\circ$  for the following circuit?

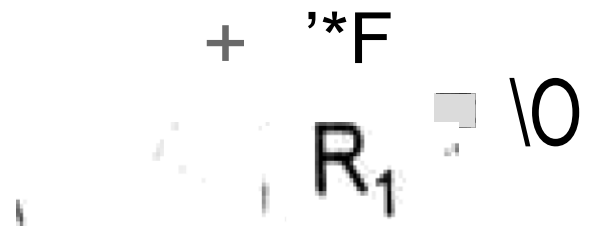


- (A)  $R_F = 4R_1$
- (B)  $R_F = 10R_1$
- (C)  $R_F = 2R_1$
- (D)  $R_F = 9R_1$

$$g_{tj}, q = 1 + \frac{R_F}{R_1}$$

$$A_g = 1$$

$$\Rightarrow \left[ 1 + \frac{R_F}{R_1} \right] \frac{1}{iV} 10^D \approx 1 \approx 0 \bullet$$



$$R_F = 9R_1$$

Choice (D)



A Colpitts oscillator has a coil with an inductance of 50  $\mu\text{H}$  and is tuned by a capacitor 400 pF across amplifier input & 200 pF across the output. Then the frequency of oscillation & the minimum gain for maintaining oscillations?

- (A) 1.95 MHz, 3 (B) 1.95 MHz, 2  
(C) 2.9 MHz, 2 (D) 2.9 MHz, 2

101. /Or colpitts OSCillatOf

$$f_0 = \frac{1}{2\pi L C_{eq}}, \quad C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

$$C_{eq} = \frac{400 \times 20}{600} = 133.33 \text{ pF}$$

$$f_0 = \frac{1}{2\pi \times 50 \times 133.33 \times 10^{-18}}$$

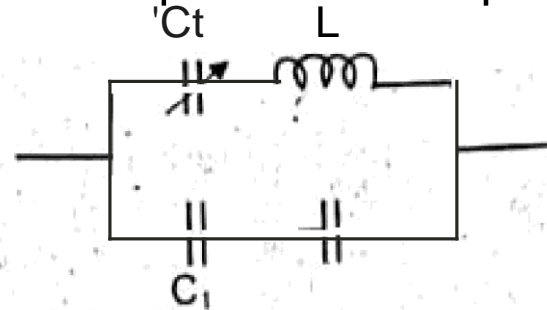
1.95, MHz

For maintaining oscillations.  $A\beta = 1$

$$A_{loop} = A_{v0} \cdot \frac{2}{C_1} = 1$$

$$A_{v0} = \frac{C_i}{C_t} = \frac{400}{200} = 2 \quad \text{Choice (B)}$$

7.10. A Clapp oscillator has the following circuit components  $C_1 = 500 \text{ pF}$ ,  $C_2 = 500 \text{ pF}$ ,  $L = 50 \text{ }\mu\text{H}$  and  $C_3$  is a variable capacitor. Or



Find out the tuning frequency range?

- (A) 1.98 to 10.34 MHz
- (B) 2.34 to 11.56 MHz
- (C) 3.35 to 12.5 MHz
- (D) 5.34 to 15.4 MHz

Sol.  $f_a = \frac{1}{2\sqrt{LC_{eq}}}$       $\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_3}$

$$C_{eq} = \frac{5000 \times 500 \times 50}{5000 \times 500 + 5000 \times 50 + 500 \times 50}$$

$$= 45.045 \text{ pF for } C_3 = 60 \text{ pF}$$

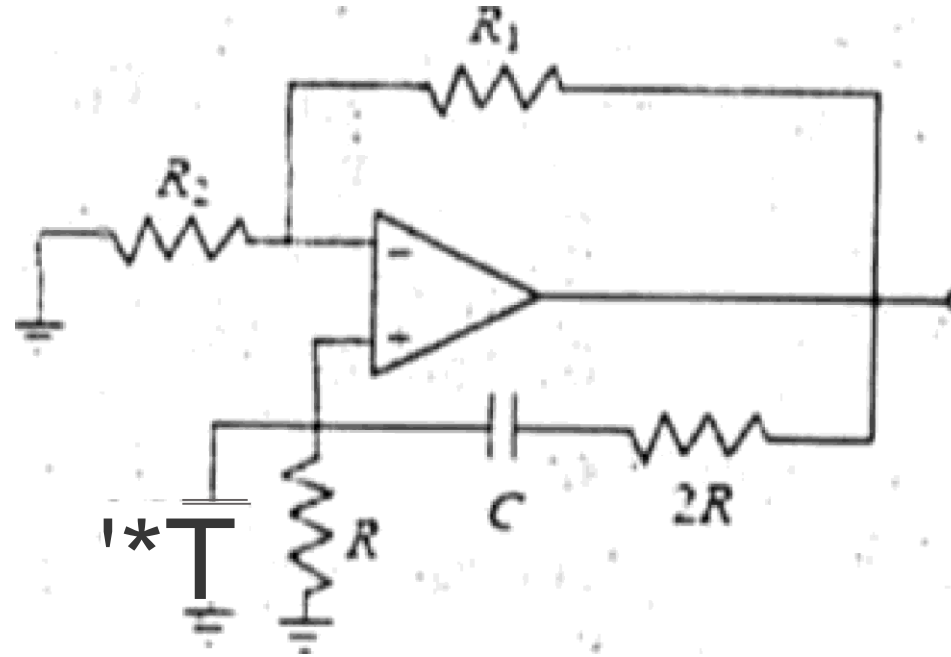
$$f = \frac{1}{2\pi\sqrt{50 \times 45.045 \times 10^{-12}}}$$

$$= 3.35 \text{ MHz}$$

$$C_{eq} = 161.29 \text{ pF for } C_3 = 250 \text{ pF}$$

$$\text{Then } f = 12.5 \text{ MHz} \quad \text{Choice (C)}$$

- 1•11• The circuit shown in the figure has an ideal opamp. The oscillation frequency and the condition to sustain the oscillation, respectively are



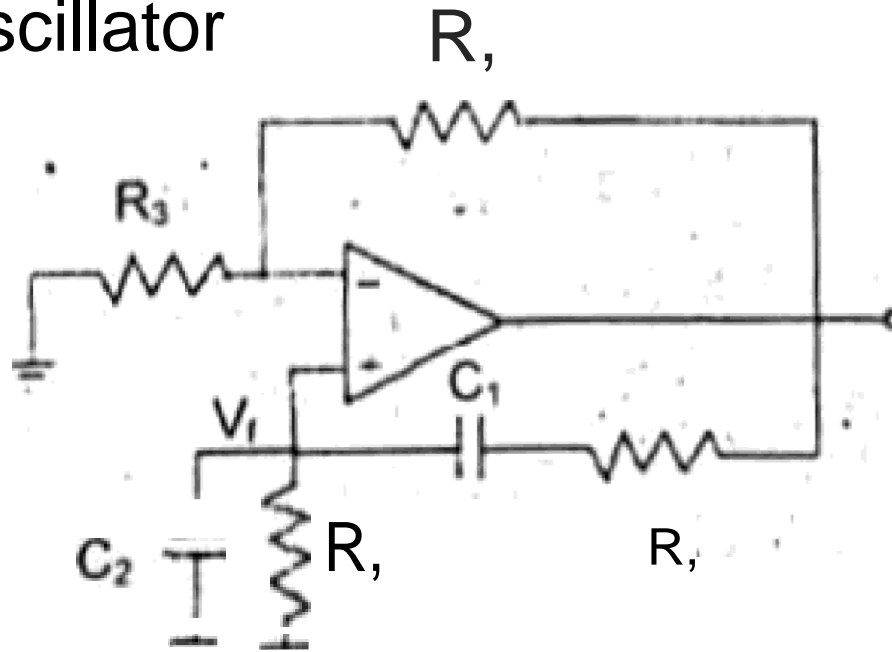
$$(A) \frac{1}{CR} \text{ and } H, - e,$$

$$\overline{ce}^{\prime o} = 4Rz$$

$$\frac{1}{2CR} \text{ and } H, - H,$$

$$\underline{\underline{1}} \text{ and } R \rangle =, 4R2$$

Sol. The given circuit is weiri brigge  
Oscillator



The gain of the op-amp is  $A = 1 + \frac{R_f}{R_g}$  and feedback factor

Let  $Z_1 = R_1 \parallel \frac{1}{sC_1}$  and  $Z_2 = R_2 \parallel \frac{1}{sC_2}$

By substituting all values, we get finally

$$B = \frac{j\omega R}{1 + j\omega(R_1 C_1 + R_2 C_2 + R_2 C_1) - \omega^2 R_1 R_2 C_1 C_2}$$

But B is real quantity so equate

$$1 - \omega^2 R_1 R_2 C_1 C_2 = 0$$

Thus the oscillation,

$$\omega_0 = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}}$$



From the given data

$$R_1 = 2R, R_2 = R$$

$$C_1 = C, C_2 = 2C, \dots \frac{1}{2RC}$$

$$\text{And } B = \frac{R_2 C_1}{1 + R_2 C_1 + R_1 C_1}$$

Sub all values

$$B = \frac{RG}{2RG + RG + RG} = \frac{1}{5}$$

For sustained oscillation  $AP = 1$

$$A = \frac{1}{0} \therefore 1 + \frac{R_f}{R_q} = 5$$

But  $R_f = R_1$  and  $R_q = R_x$

$$\therefore R_1 = 4R_x$$

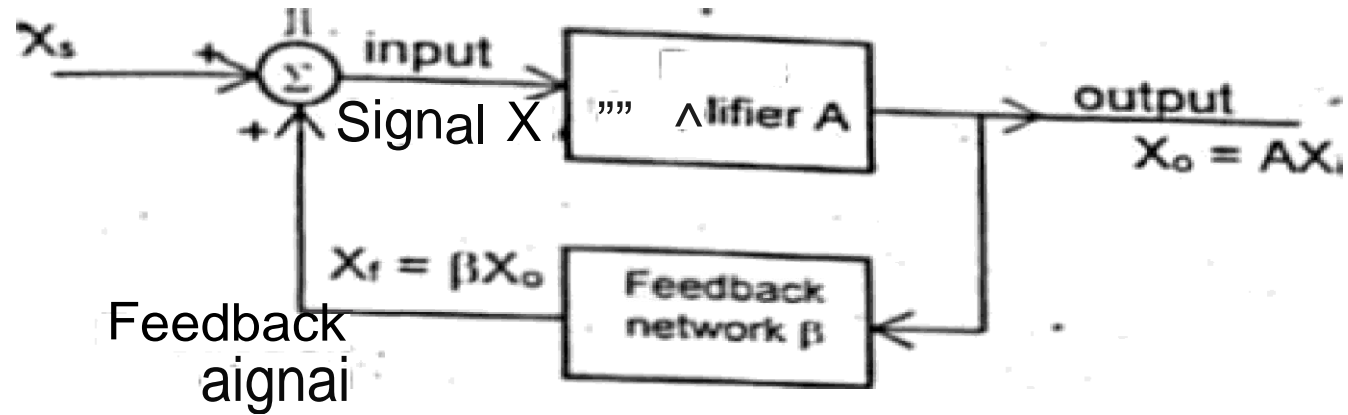
QED (□)

7.12. Show that a feedback amplifier can be made to work as an oscillator



(ESE)

\* 0 • > e f3e \* »!ized positim feedba ck  
ampliifier circuit blo6 diaga jyj iS  
shown below:



we know that  $X_i = p_i + jg_i$

$= -$

$$X_o = AX_{in}$$

$$X_o = A \{ X_s + X_r \}$$

$=$

$$X_o = AX_s + A\beta X_o$$

$$*to = f* \quad App \quad Ax,$$

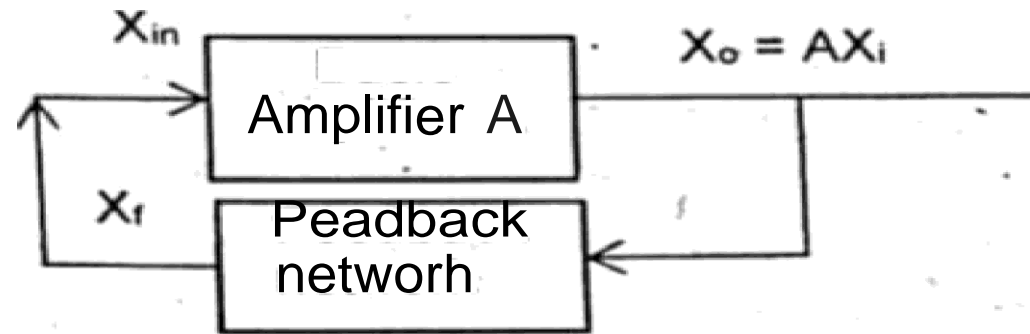
□ overall gain with positive feedback

$$\Rightarrow A_f = \frac{A}{1 - A\beta}$$

If  $A\beta > 1 \Rightarrow j\omega \rightarrow +\infty$

"infinite gain means, with no input there can expect some output in fact in oscillator there is no input signal, it works on another noise signal the circuit sustains it.

Oscillator:-



$$A\beta = 1$$

---

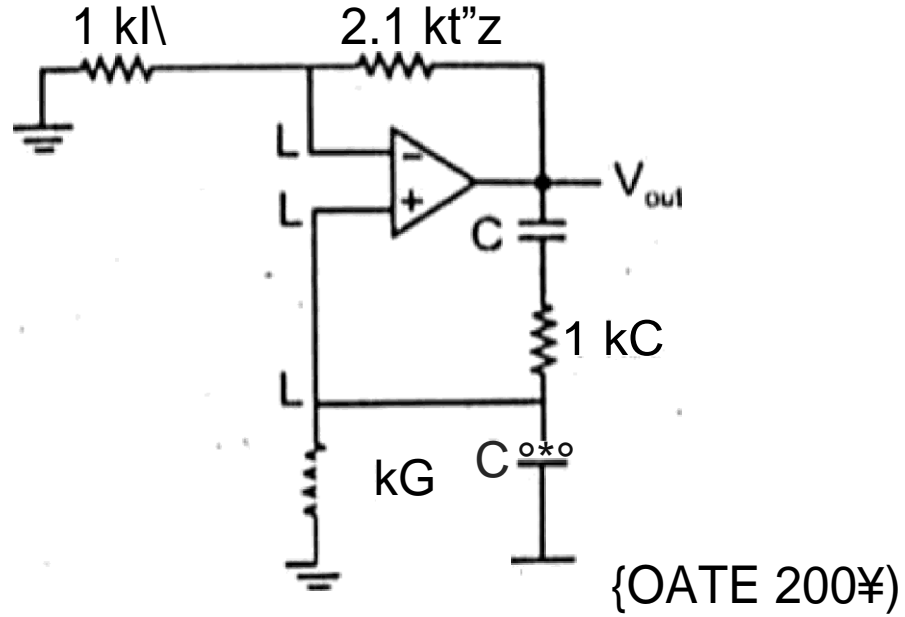
∴ a necessary condition for oscillator circuits is known to be one of the Barkhausen criterion.

Necessary condition for oscillation  
(Or) Barkhausen criterion is satisfied if  $|A\beta| \geq 1$  and  $\angle A\beta = 0^\circ$

- 
- (i) magnitude of loop gain should be equal to 1 i.e.  $|A\beta| = 1$
  - (ii) Loop angle should be made to  $0^\circ$  (or)  $360^\circ$ . i.e.  $\angle A\beta = 0^\circ$  or  $360^\circ$ .

Hence, a feedback Amplifier (positive feedback) can be made to work as an oscillator by following the above two conditions.

3. The value of C required for sinusoidal oscillations of frequency 1 KHz in the circuit of fig. is



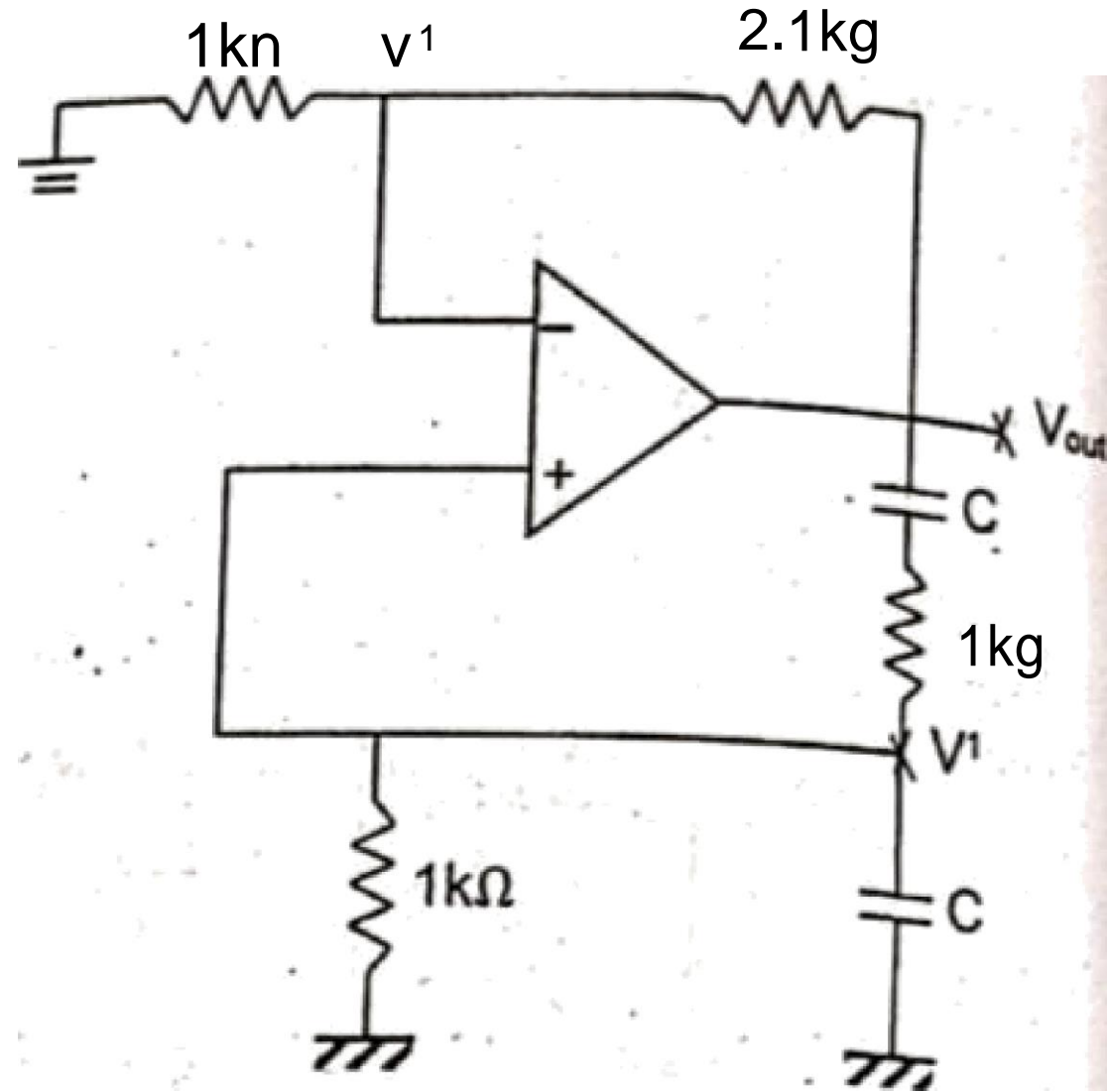
(A)  $\frac{1}{2\pi} \mu\text{F}$

(B)  $2\pi \text{ kF}$

(C)  $\frac{1}{2\pi} \text{ F}$

(D)  $2\pi \text{ srr}$

3.





→ apply XCL at  $V^1$

$$\frac{V^1}{X_C} + \frac{V^1}{R} + \frac{V^1 - V_{out}}{X_C + R} = 0$$

$$\therefore Z^{V^1} \left[ \frac{1}{X_C} + \frac{1}{R} + \frac{1}{X_C + R} \right] - \frac{V_{out}}{X_C + R} = 0$$

$$\frac{V_{out}}{V^1} = \frac{R(X_C + R)}{R(X_C + R) + X_C(X_C + R)}$$

$$= 1 + \frac{X_C^2}{R(X_C + R)} = 3 + \frac{R}{X_C} + \frac{X_C}{R}$$

For  $\phi = 0$  the imaginary part is equal to

zero

$$\frac{R}{X_C} + \frac{X_C}{R} = 0$$

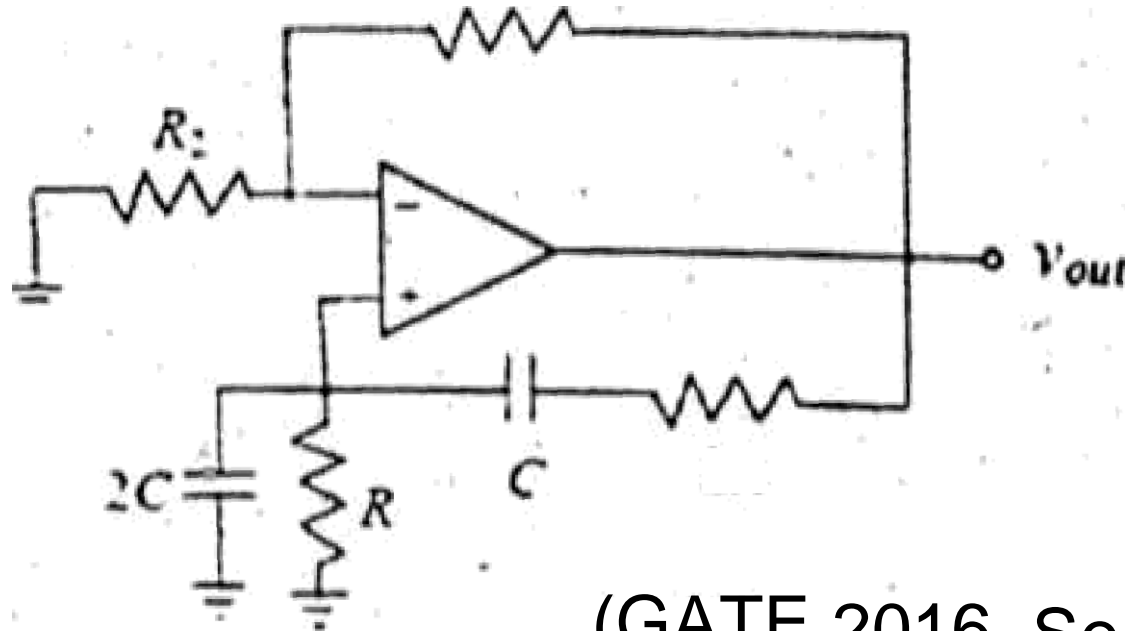
$$\Rightarrow j\omega R = \frac{1}{j\omega C}$$

$$25 \Rightarrow \phi = -\frac{\pi}{2}$$

$$\Rightarrow C = \frac{1}{R\omega} = \frac{1}{10^3 \times 2\pi \times 10^3} = \frac{1}{2\pi} \mu\text{F}$$

Choice (\*)

20. The circuit shown in the figure has an ideal opamp. The oscillation frequency and the condition to sustain the oscillation » respectively are



(GATE 2016, Se1•1\

(A)  $\frac{1}{CR}$  and  $R_1 = R_x$

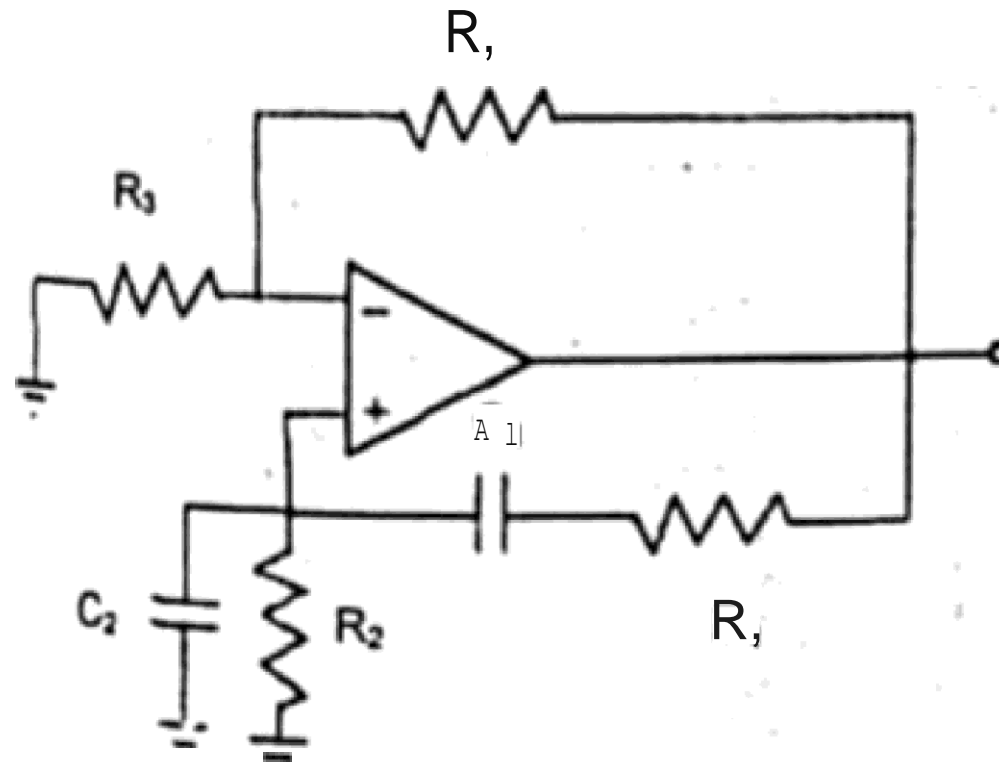
(B)  $\frac{1}{-CR}$  and  $R_i = 4R_x$

(C)  $\frac{1}{2CR}$  and  $R_i = R_x$

(D)  $\frac{1}{2CR}$  and  $R_i = 4R_x$

---

tA. The given circuit is wein bridge Oscillator



the gain of the opamp is

$$A = 1 + \frac{R_f}{R_3} \text{ and feedback factor}$$

$$B = \frac{V_f}{V_o}$$

$$V_f = \frac{R_2}{R_1 + R_2} V_o$$

$$A' = \frac{1}{1 - B} = \frac{1}{1 - \frac{R_2}{R_1 + R_2}}$$

$$V_f = \frac{Z_2 \times V_o}{Z_1 + Z_2}$$

2/2

$$= \frac{1}{1 - \omega^2 R_1 R_2 C_1 C_2}$$

Sub all values in mB we get finally

$$B = \frac{j\omega R_2 C_1}{1 - j\omega(R_1 C_1 + R_2 C_2 + R_2 C_1) - \omega^2 R_1 R_2 C_1 C_2}$$

BUT B is real quantity so equate

$$1 - \omega^2 R_1 R_2 C_1 C_2 = 0$$

Thus the frequency of oscillation,

$$f_o = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

$$= \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

From the given data

$$R_x = 2R,$$

$$R_z = R$$

$$C_x = C,$$

$$C_z = 2C$$

$$\text{And } B = \frac{R_2 C_1}{R_1 C_1 + R_2 C_2 + R_2 C_1}$$

Sub all values

$$B = \frac{RC}{1 + 2RC + 2RC + RC} = \frac{RC}{5RC}$$

For sustained oscillation  $AB = 1$

$$A = \frac{1}{B} \cdot \left(1 + \frac{R_f}{R_y}\right) = 5$$

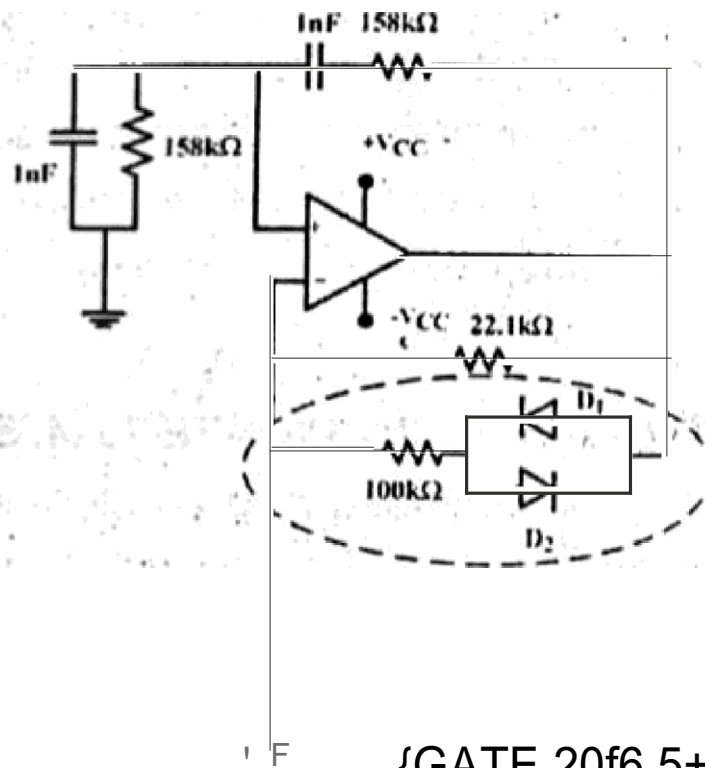
But  $R_i = R_x$  and  $R_a = R_z$

$$\therefore R_s = 4R_z$$

Choice (D)



22. Consider the oscillator circuit shown in the figure. The function of the network consisting of a 100k resistor in series with the two diodes connected back to back is to



{GATE 20f6,5+!•!}

(4) Introduce amplitude stabilization by preventing the op amp from saturating and thus producing a square wave of fixed amplitude

(B) introduce amplitude stabilization by forcing the op amp to swing between positive and negative saturation and thus producing a square wave of fixed amplitude

(C) introduce frequency stabilization by forcing the circuit to oscillate at a specific frequency

(D) Reduce the open loop gain to a value that produces square wave oscillations

22. The given circuit is a wein bridge oscillator, it produces sinusoidal oscillations. The back – to – back diodes introduces amplitude stabilization by preventing the op-amp from saturation.

Choice (A)

