

Domain and range of a relation :-

Let $R = \{(x, y) : x \in A, y \in B \text{ and } xRy\}$ be a relation from A to B . Then the set of first co-ordinate of every element of R is called domain of R and denote by Domain of R , $(\text{Dom}(R))$ and the set of second co-ordinate of its every element is called Range of R and denoted by $\text{Ran}(R)$.

Ques - Let $A = \{2, 4, 6\}$ and $B = \{1, 4, 5, 6\}$ then find the relation from A to B defined by "is less than or equal to". Find out the domain and range of the relation.

Solu - $A \times B = \{(2, 1), (2, 4), (2, 5), (2, 6), (4, 1), (4, 4), (4, 5), (4, 6), (6, 1), (6, 4), (6, 5), (6, 6)\}$

Hence $R = \{(2, 5), (2, 6), (2, 4), (4, 4), (4, 5), (4, 6), (6, 6)\}$

$$\text{Dom}(R) = \{2, 4, 6\}$$

$$\text{Ran}(R) = \{4, 5, 6\}$$

Complement of a relation -

Consider a relation R from set A to B .

The complement of relation R denoted by \bar{R} or R' is a relation from A to B such that

$$R' = \{(a, b) : (a, b) \notin R\}$$

Ques - Let R be a relation from X to Y , where $X = \{1, 2, 3\}$ and $Y = \{8, 9\}$ and $R = \{(1, 8), (1, 9), (2, 8), (3, 9)\}$. Find the complement of relation R .

Solu - $X \times Y = \{(1, 8), (1, 9), (2, 8), (2, 9), (3, 8), (3, 9)\}$

$$R' = \{(2, 9), (3, 8)\} \Rightarrow \text{qit element uti } R \text{ ni ni } \bar{R}$$

Inverse relation - Let R be a relation from a set A to B ,

The inverse of relation R denoted by R^{-1} is a relation from B to A such that $bR^{-1}a$ iff aRb .

$$R^{-1} = \{(b, a) : (a, b) \in R\}$$

Thus, to find R^{-1} we write in reverse order all ordered pairs belonging to R .

ex - Let $A = \{1, 2, 3\}$ and relation (R) is \leq on A .
Determine its inverse.

sol - $A = \{1, 2, 3\}$

$$R = \{(1, 1), (2, 2), (3, 3), (1, 2), (1, 3), (2, 3)\}$$

$$R^{-1} = \{(1, 1), (2, 2), (3, 3), (3, 2), (3, 1), (2, 1)\}$$