

HAMMING N/W

DATE: / /

input :- orange $P_1 = \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix}$, $P_2 = \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}$ Apple $P = \begin{bmatrix} P_1 \\ P_2 \end{bmatrix}$

* Feed forward layer \rightarrow performs correlation or inner product, b/w each prototype patterns & the input patterns.

$$W^1 = \begin{bmatrix} P_1^T \\ P_2^T \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 \\ 1 & 1 & -1 \end{bmatrix}$$

& feedforward layers uses a linear transfer function, & each element of the bias vector is equal to R, (R is the no. of elements in input vector)

$$b^1 = \begin{bmatrix} R \\ R \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \end{bmatrix}$$

Output of the feed forward layer is

$$a^1 = W^1 p + b^1 = \begin{bmatrix} P_1^T \\ P_2^T \end{bmatrix} \cdot p + \begin{bmatrix} R \\ R \end{bmatrix} = \begin{bmatrix} P_1^T p + 3 \\ P_2^T p + 3 \end{bmatrix}$$

* Recurrent layer \rightarrow ("competitive" layer).

Neuron in this layer are initialised with the outputs of the feedforward layer, The neurons compete with each other to determine a winner.

$$a^{(2)}(0) = a^{(1)} \quad \text{initial condition.}$$

Linear for positive value & zero for negative

$$a^2(t+1) = \text{poslin}(w^2 a^2(t))$$

(superscript here indicate the layer no. not a power of 2)

&

$$w^2 = \begin{bmatrix} 1 & -\epsilon \\ -\epsilon & 1 \end{bmatrix}$$

$\epsilon \rightarrow$ some no. less than $1/(s-1)$

$s \rightarrow$ no. of neurons in recurrent layer.

Ex \rightarrow $p = \begin{bmatrix} -1 \\ -1 \\ -1 \end{bmatrix}$, $a^1 = \begin{bmatrix} +1 & -1 & -1 \\ 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} -1 \\ -1 \\ -1 \end{bmatrix} + \begin{bmatrix} 3 \\ 3 \end{bmatrix} = \begin{bmatrix} 4 \\ 2 \end{bmatrix}$

which is initial condition for the recurrent layer

$$w^{(2)} = \begin{bmatrix} 1 & -0.5 \\ -0.5 & 0 \end{bmatrix}, \epsilon = 1/2$$

$$a^2(1) = \text{poslin}(w^2 a^2(0)) = \text{poslin}\left(\begin{bmatrix} 3 \\ 0 \end{bmatrix}\right) = \begin{bmatrix} 3 \\ 0 \end{bmatrix}$$

second iteration:

$$a^2(2) = \begin{bmatrix} 3 \\ 0 \end{bmatrix}$$

Since the o/p of successive iterations produce the same result, the network has converged.