

1. The following data were gathered for the steady state creep rate of polycrystalline Al_2O_3 . All grain sizes are $10\mu m$ except * which are $30\mu m$.

	Temp °C	Stress MPa	strain rate $10^{-4}/hr.$
	1400	10	0.3
	1400	10	0.011*
	1425	10	0.8
	1450	10	1.6
	1475	10	3.0
①	1500	1	0.5
②	1500	2	1.1
③	1500	5	2.6
④	1500	10	5.1
	1500	10	0.19*
	1550	15	8.0
	1525	10	11.0
	1575	10	54.6
	1600	10	121.5
	1600	10	13.5*

for steady state creep determine

- the stress exponent.
- the activation energy
- the grain size exponent
- the creep mechanism.

For steady state creep rate

$$\dot{\epsilon} = \frac{ADGb}{KT} \left(\frac{b}{d}\right)^m \left(\frac{\sigma}{G}\right)^n$$

(a) at same temp & same grain size

$$\frac{\dot{\epsilon}_1}{\dot{\epsilon}_2} = \left(\frac{\sigma_1}{\sigma_2}\right)^n$$

Consider ① ② ③ ④ set of values

① ②

$$\frac{0.5}{1.1} = \left(\frac{1}{2}\right)^n \quad n = 1.1$$

② ③

$$\frac{1.1}{2.6} = \left(\frac{2}{5}\right)^n \quad n = 0.94 \quad \Rightarrow n = 1$$

③ ④

$$\frac{2.6}{5.1} = \left(\frac{5}{10}\right)^n \quad n = 0.97$$

(b)

$$\Delta H = \frac{R \ln \left(\frac{\dot{\epsilon}_1}{\dot{\epsilon}_2}\right)}{\frac{1}{T_2} - \frac{1}{T_1}}$$

Consider the data for const stress, & same grain size

T °C	$\dot{\epsilon}$ hr ⁻¹	grain size ~ 10 μ m	stress ~ 10 MPa
1400	0.3×10^{-4}		
1500	5.1×10^{-4}		

$$\Delta H = \frac{8.314 \ln \left(\frac{0.3 \times 10^{-4}}{5.1 \times 10^{-4}}\right)}{\frac{1}{1773} - \frac{1}{1673}} = \frac{-23.56}{-3.37 \times 10^{-5}} = 6.99 \times 10^5 \text{ J}$$

$^{\circ}\text{C}$	
1400	$0.011 \times 10^{-4} / \text{hr}$
1600	$13.5 \times 10^{-4} / \text{hr}$

$$\Delta H = \frac{0.314 \ln \left(\frac{0.011}{13.5} \right)}{\frac{1}{1873} - \frac{1}{1673}} = \frac{\cancel{6.77 \times 10^{-3}} - 59.1}{-6.39 \times 10^{-5}} = 9.26 \times 10^5 \text{ J}$$

$T^{\circ}\text{C}$	$\dot{E} / \text{hr} \times 10^{-4}$
1400	0.3
1425	0.8
1450	1.6
1475	3
1500	5.1
1525	11.0
1575	54.6
1600	121.5

$$\dot{E} = A \exp \left(-\frac{\Delta H}{RT} \right)$$

$$\ln \dot{E} = \ln A - \frac{\Delta H}{RT}$$

$$-\ln \dot{E} = \frac{\Delta H}{R} \left(\frac{1}{T} \right) - \ln A$$

make a plot $(-\ln \dot{E})$ vs. $\frac{1}{T}$

$$\text{slope} = \frac{\Delta H}{R}$$

from slope get ΔH