Hydrostatic stress tensor

Objective: To learn how to find the hydrostatic stress tensor at a given point.

Suppose at a point stress tensor
$$\sigma = \begin{bmatrix} \sigma_x & \tau_{xy} & \tau_{xz} \\ \tau_{xy} & \sigma_y & \tau_{yz} \\ \tau_{xz} & \tau_{yz} & \sigma_z \end{bmatrix}$$

Evaluate
$$\bar{\sigma} = \frac{\sigma_x + \sigma_y + \sigma_z}{3}$$

Hydrostatic stress tensor

$$\sigma_{Hyd} = \begin{bmatrix} \overline{\sigma} & 0 & 0 \\ 0 & \overline{\sigma} & 0 \\ 0 & 0 & \overline{\sigma} \end{bmatrix}$$

O Physical significance of hydrostatic stress tensor:

Hydrostatic stress tensor is responsible for volumetric change in infinitesimal at point P. It doesn't change with stress transformation.