

### Angle Modulation

Modulation process is analog modulation process but non linear modulation process. In this we change the total phase angle of  $c(t)$  according to  $m(t)$  by keeping amplitude constant.

§ Advantages of angle modulation over amplitude modulation:

- i) S/N Ratio at Rx      S: Signal Power, N: Noise Power.
- ii) Higher  $B_T$ .

Angle modulation can be classified as:

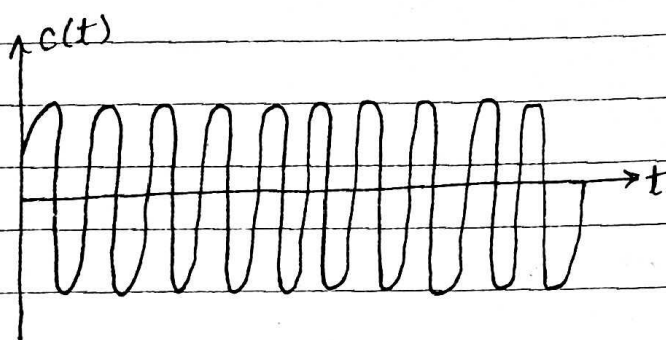
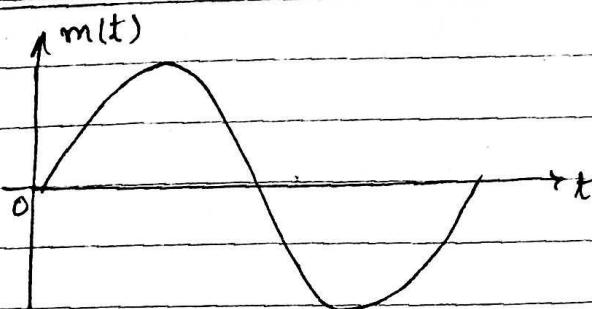
- i) Frequency modulation
- ii) Phase modulation

$$\omega_i = \frac{d}{dt} \theta(t)$$

$$\omega_i = \omega_c + \frac{d}{dt} \phi(t) = \text{Frequency deviation}$$

Frequency modulation is a process in which we change the instantaneous frequency of carrier signal according to the amplitude of the message signal.

The amount by which frequency of  $c(t)$  is varied to its unmodulated value is called frequency deviation.



The frequency deviation ( $\delta$ ):

$$\delta = k V_m f_c$$

where,

$V_m$  = amplitude of  $m(t)$

$f_c$  = frequency of carrier signal.

The instantaneous frequency of F.M.:

$$f_i = f_c (1 \pm k V_m \cos \omega_m t)$$

$$m(t) = V_m \cos \omega_m t$$

$$c(t) = V_c \cos \omega_c t$$

If  $\cos \omega_m t = 1$  then,

$$f_i = f_c (1 \pm k V_m)$$

$$f_i = f_c \pm KV_m f_c$$

If we consider the +ve side :

$$f_H = f_{\max} = f_c + KV_m f_c \\ = f_c + \delta$$

$\delta =$  allowed deviation

If we consider the -ve side :

$$f_L = f_{\min} = f_c - KV_m f_c \\ = f_c - \delta$$

$$\therefore \delta = \frac{f_H - f_L}{2}$$

Modulation Index for F.M. wave :

$$m_f = \frac{\delta}{f_m} = \frac{\text{Frequency deviation}}{\text{Highest freq. component present in } m(t)}$$

Physical significance of  $m$  : How much frequency changes according to amplitude of message signal.

Wave eq<sup>n</sup> of F.M. :

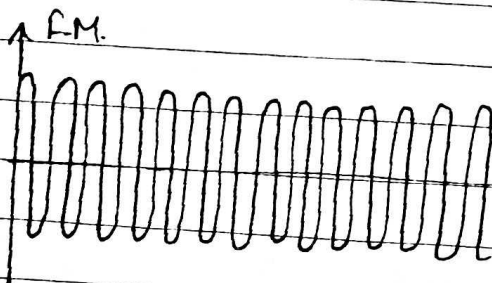
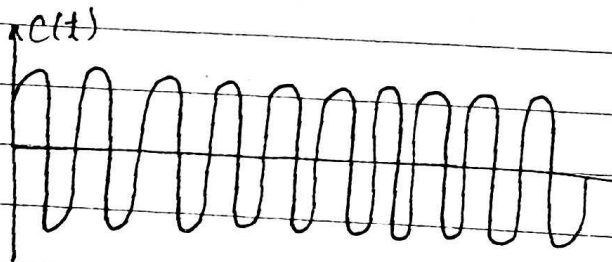
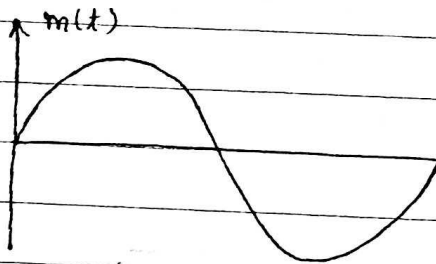
$$s(t) = A_c \sin \theta$$

$$\theta = \int \omega_i dt$$

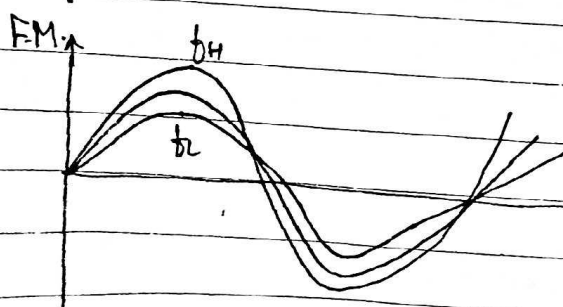
$$\theta = \int \omega_c (1 \pm KV_m \cos \omega_m t) dt$$

$$\begin{aligned}
 \theta &= \omega_c t \pm \frac{\omega_c k V_m \sin \omega_m t}{\omega_m} \\
 &= \omega_c t \pm \frac{2\pi f_c t}{\omega_m} \frac{k V_m \sin \omega_m t}{2\pi f_m} \\
 &= \omega_c t \pm \frac{k V_m f_c \sin \omega_m t}{f_m} \\
 &= \omega_c t \pm \left( \frac{\delta}{f_m} \right) \sin \omega_m t \\
 &= \omega_c t \pm m_f \sin \omega_m t
 \end{aligned}$$

$$s(t) = A_c \sin [\omega_c t \pm m_f \sin \omega_m t]$$



theoretical



Practical

$$\delta = \frac{b_H - b_L}{2}$$