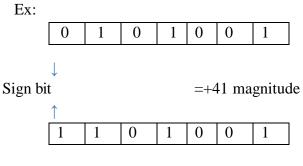
## **Representation of signed no.s binary arithmetic in computers:**

- Two ways of rep signed no.s
  - 1. Sign Magnitude form
  - 2. Complemented form
- Two complimented forms
  - 1. 1's compliment form
  - 2. 2's compliment form

Advantage of performing subtraction by the compliment method is reduction in the hardware.( instead of addition & subtraction only adding ckt's are needed.)

i.e, subtraction is also performed by adders only.

Instead of subtracting one no. from other the compliment of the subtrahend is added to minuend. In sign magnitude form, an additional bit called the sign bit is placed in front of the no. If the sign bit is 0, the no. is +ve, If it is a 1, the no is \_ve.



= -41

Note: manipulation is necessary to add a +ve no to a -ve no

# Representation of signed no.s using 2's or 1's complement method:

If the no. is +ve, the magnitude is rep in its true binary form & a sign bit 0 is placed in front of the MSB.I f the no is \_ve , the magnitude is rep in its 2's or 1's compliment form & a sign bit 1 is placed in front of the MSB.

-
Hv.
LA.

Given no.	Sign mag form	2's comp form	1's comp form
01101	+13	+13	+13
010111	+23	+23	+23
10111	-7	-7	-8
1101010	-42	-22	-21

#### Special case in 2's comp representation:

Whenever a signed no. has a 1 in the sign bit & all 0's for the magnitude bits, the decimal equivalent is  $-2^n$ , where n is the no of bits in the magnitude . Ex: 1000=-8 & 10000=-16

### **Characteristics of 2's compliment no.s:**

Properties:

- 1. There is one unique zero
- 2. 2's comp of 0 is 0

1100

1011

1010

1001

1000

- 3. The leftmost bit can't be used to express a quantity . it is a 0 no. is +ve.
- 4. For an n-bit word which includes the sign bit there are  $(2^{n-1}-1)$  +ve integers,  $2^{n-1}$  –ve integers & one 0, for a total of  $2^n$  uniquestates.
- 5. Significant information is containd in the 1's of the +ve no.s & 0's of the \_ve no.s
- 6. A \_ve no. may be converted into a +ve no. by finding its 2's comp.

Decimal	Sign 2's comp form	Sign 1's comp form	Sign mag form
+7	0111	0111	0111
+6	0110	0110	0110
+5	0101	0101	0101
+4	0100	0100	0100
+3	0011	0011	0011
+2	0010	0010	0010
+1	0011	0011	0011
+0	0000	0000	0000
			·
-0		1111	1000
-1	1111	1110	1001
-2	1110	1101	1010
-3	1101	1100	1011

1011

1010

1001

1000

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1100

1101

1110

1111

--

## Signed binary numbers:

-4

-5

-6 -7

8

## Methods of obtaining 2's comp of a no:

- In 3 ways
  - 1. By obtaining the 1's comp of the given no. (by changing all 0's to 1's & 1's to 0's) & then adding 1.
  - 2. By subtracting the given n bit no N from  $2^n$
  - 3. Starting at the LSB, copying down each bit upto & including the first 1 bit encountered, and complimenting the remaining bits.
  - Ex: Express -45 in 8 bit 2's comp form

+45 in 8 bit form is 00101101

I method:

1's comp of 00101101 & the add 1 00101101 11010010 +1

\_\_\_\_\_

11010011

is 2's comp form

II method:

Subtract the given no. N from  $2^n$ 

$$2^{n} = 100000000$$
  
Subtract 45= -00101101  
+1

11010011

is 2's comp

**III** method:

Original no: 00101101 Copy up to First 1 bit 1 Compliment remaining : 1101001

bits

11010011

Ex:

-73.75 in 12 bit 2'compform I method

01001001.1100 10110110.0011 +1

10110110.0100 is 2's II method:  $2^8 = 10000000.0000$ Sub 73.75=-01001001.1100

 10110110.0100 is 2's comp

 III method :

 Orginalno
 :

 01001001.1100

 Copy up to 1'st bit
 100

 Comp the remaining bits:
 10110110.0

#### 10110110.0100

#### **2's compliment Arithmetic:**

• The 2's comp system is used to rep -ve no.s using modulus arithmetic . The word length of a computer is fixed. i.e, if a 4 bit no. is added to another 4 bit no . the result will be only of 4 bits. Carry if any , from the fourth bit will overflow called the Modulus arithmetic.

Ex:1100+1111=1011

• In the 2's compl subtraction, add the 2's comp of the subtrahend to the minuend. If there is a carry out, ignore it, look at the sign bit I,e, MSB of the sum term .If the MSB is a 0, the result is positive.& it is in true binary form. If the MSB is a ` ( carry in or no carry at all) the result is negative.& is in its 2's comp form. Take its 2's comp to find its magnitude in binary.

Ex:Subtract 14 from 46 using 8 bit 2's comp arithmetic:

+14 -14	= 00001110 = 11110010	2's comp
+46 -14	= 00101110 =+11110010	2's comp form of -14

### -32 (1)00100000 ignore carry

Ignore carry, The MSB is 0. so the result is +ve. & is in normal binary form. So the result is +00100000=+32.

**EX:** Add -75 to +26 using 8 bit 2's comp arithmetic

+75 -75	= 01001011 =10110101	2's comp
+26 -75	= 00011010 =+10110101	2's comp form of -75
-49	11001111	No carry

No carry, MSB is a 1, result is ve & is in 2's comp. The magnitude is 2's comp of 11001111. i.e, 00110001 = 49. so result is -49

Ex: add -45.75 to +87.5 using 12 bit arithmetic

+87.5 = 01010111.1000-45.75 = +11010010.0100

-41.75 (1)00101001.1100 ignore carry MSB is 0, result is +ve. =+41.75

### 1's compliment of n number:

- It is obtained by simply complimenting each bit of the no,.& also, 1's comp of a no, is subtracting each bit of the no. form 1. This complemented value rep the ve of the original no. One of the difficulties of using 1's comp is its rep o f zero. Both 00000000 & its 1's comp 11111111 rep zero.
- The 00000000 called +ve zero& 11111111 called -ve zero.
- Ex: -99 & -77.25 in 8 bit 1's comp

+99	=	01100011
-99	=	10011100

+77.25 = 01001101.0100-77.25 = 10110010.1011

#### 1's compliment arithmetic:

In 1's comp subtraction, add the 1's comp of the subtrahend to the minuend. If there is a carryout, bring the carry around & add it to the LSB called the **end around carry**. Look at the sign bit (MSB). If this is a 0, the result is +ve & is in true binary. If the MSB is a 1 ( carry or no carry ), the result is -ve & is in its is comp form. Take its 1's comp to get the magnitude inn binary.

Ex: Subtract 14 from 25 using 8 bit 1's EX: ADD -25 to +14

25	=	00011001	+14	= 00001110
-45	=	11110001	-25	=+11100110
. 11		(1)00001010	11	11110100
+11		(1)00001010	-11	11110100
	+1			
			No ca	arry MSB=1
	_	00001011		result=-ve=-11 <sub>10</sub>
MSE	B is a 0 s	so result is +ve (binary)		

 $=+11_{10}$ 

## **Binary codes**

Binary codes are codes which are represented in binary system with modification from the original ones.

- □ Weighted Binary codes
- $\Box$  Non Weighted Codes

Weighted binary codes are those which obey the positional weighting principles, each position of the number represents a specific weight. The binary counting sequence is an example.

Decimal	BCD 8421	Excess-3	84-2-1	2421	5211	Bi-Quinary 5043210		5	0	4	3	2	1	0
0	0000	0011	0000	0000	0000	0100001	0		Х					Х
1	0001	0100	0111	0001	0001	0100010	1		Х				Х	
2	0010	0101	0110	0010	0011	0100100	2		Х			Х		
3	0011	0110	0101	0011	0101	0101000	3		Х		Х			
4	0100	0111	0100	0100	0111	0110000	4		Х	Х				
5	0101	1000	1011	1011	1000	1000001	5	Х						Х
6	0110	1001	1010	1100	1010	1000010	6	Х					Х	
7	0111	1010	1001	1101	1100	1000100	7	Х				Х		
8	1000	1011	1000	1110	1110	1001000	8	Х			Х			
9	1001	1111	1111	1111	1111	1010000	9	Х		Х				

## **Reflective Code**

A code is said to be reflective when code for 9 is complement for the code for 0, and

so is for 8 and 1 codes, 7 and 2, 6 and 3, 5 and 4. Codes 2421, 5211, and excess-3 are reflective, whereas the 8421 code is not.

### **Sequential Codes**

A code is said to be sequential when two subsequent codes, seen as numbers in binary representation, differ by one. This greatly aids mathematical manipulation of data. The 8421 and Excess-3 codes are sequential, whereas the 2421 and 5211 codes are not.

#### Non weighted codes

Non weighted codes are codes that are not positionally weighted. That is, each position within the binary number is not assigned a fixed value. Ex: Excess-3 code

#### **Excess-3 Code**

Excess-3 is a non weighted code used to express decimal numbers. The code derives its name from the fact that each binary code is the corresponding 8421 code plus 0011(3).

### **Gray Code**

The gray code belongs to a class of codes called minimum change codes, in which only one bit in the code changes when moving from one code to the next. The Gray code is non-weighted code, as the position of bit does not contain any weight. The gray code is a reflective digital code which has the special property that any two subsequent numbers codes differ by only one bit. This is also called a unit-distance code. In digital Gray code has got a special place.

Decimal Number	Binary Code	Gray Code	Decimal Number	Binary Code	Gray Code
0	0000	0000	8	1000	1100
1	0001	0001	9	1001	1101
2	0010	0011	10	1010	1111
3	0011	0010	11	1011	1110
4	0100	0110	12	1100	1010
5	0101	0111	13	1101	1011
6	0110	0101	14	1110	1001
7	0111	0100	15	1111	1000