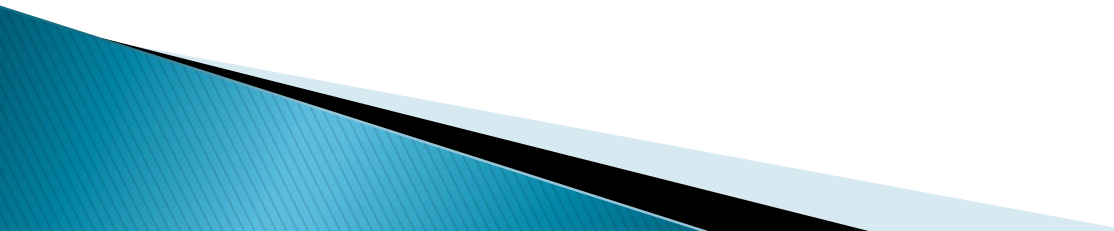
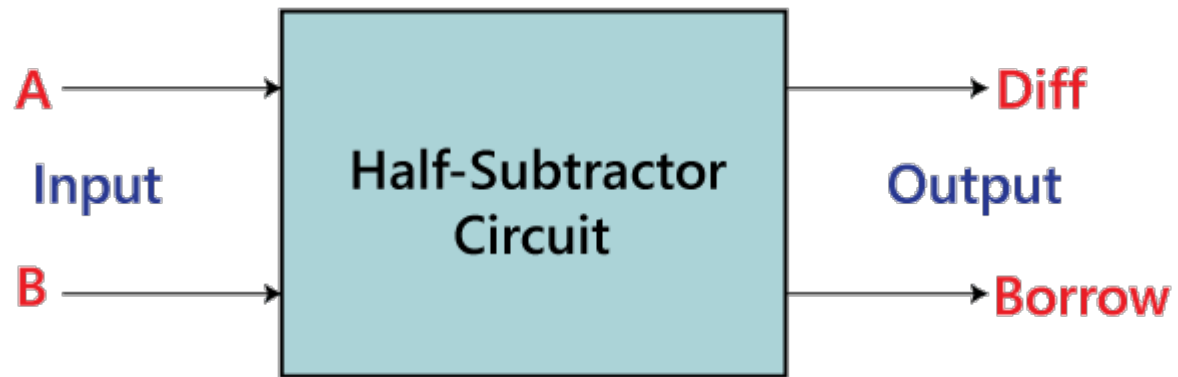


HALF SUBTRACTOR



- ▶ **Half Subtractor is a combinational logic circuit.**
 - ▶ **It is used for the purpose of subtracting two single bit numbers.**
 - ▶ **It contains 2 inputs and 2 outputs (difference and borrow).**
- 

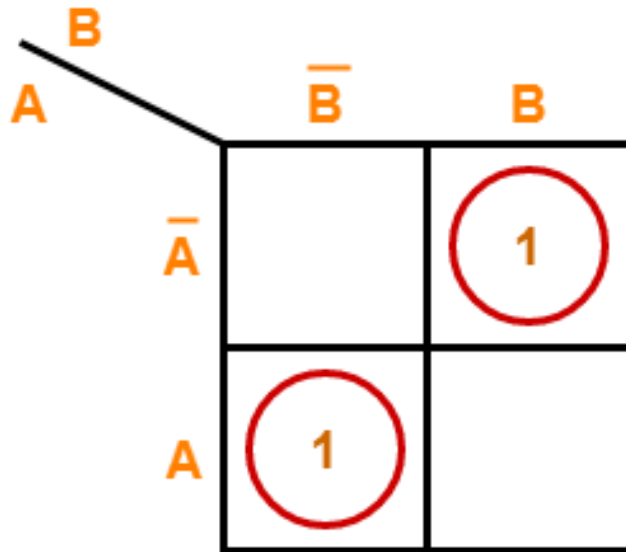


Truth Table

INPUTS		OUTPUTS	
A	B	D (Difference)	B (Borrow)
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

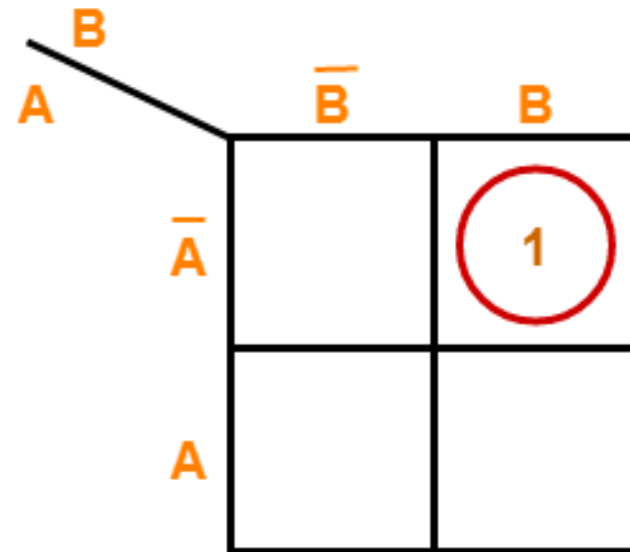
K-maps

For D:



$$D = A \oplus B$$

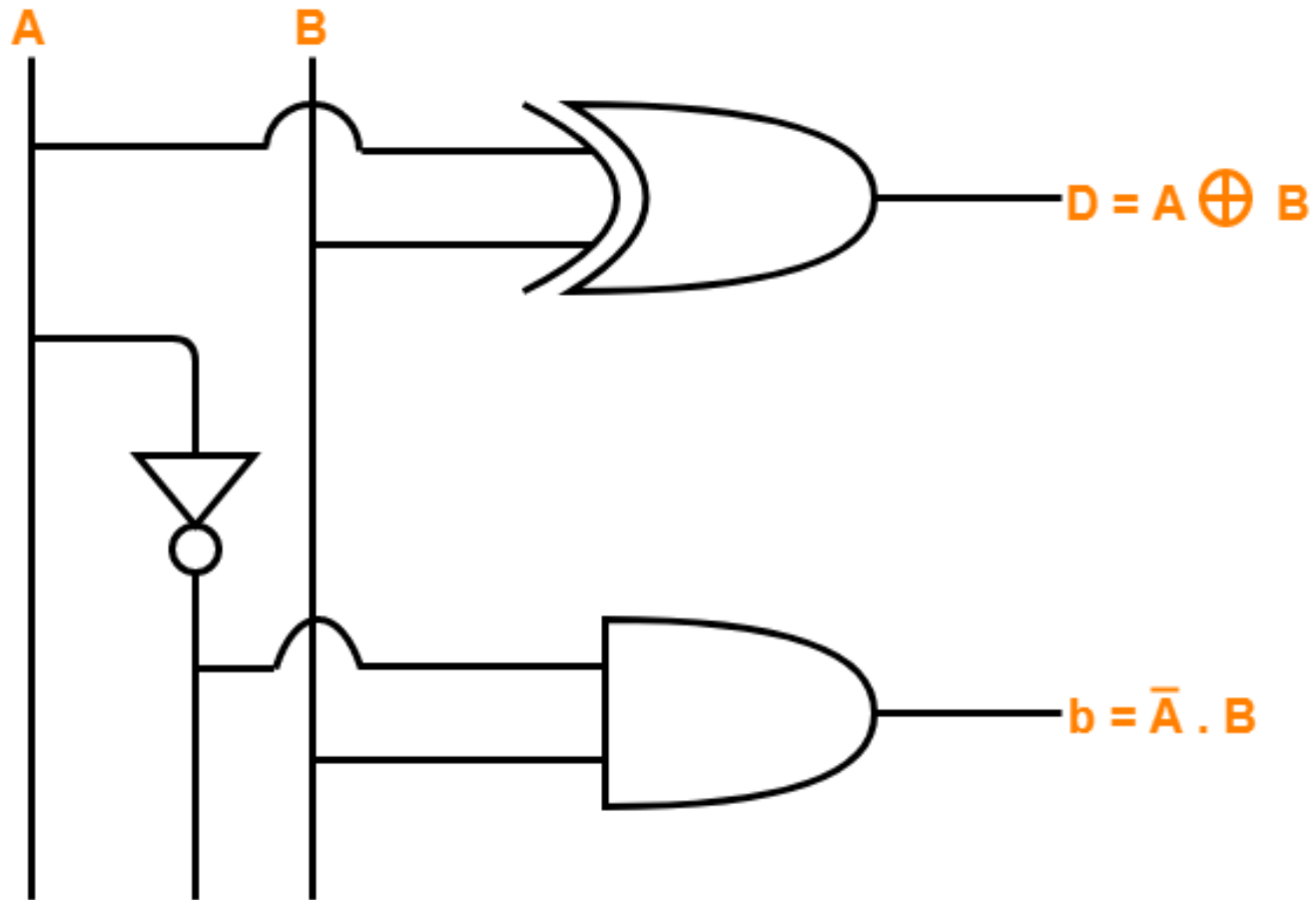
For b:



$$b = \bar{A}.B$$

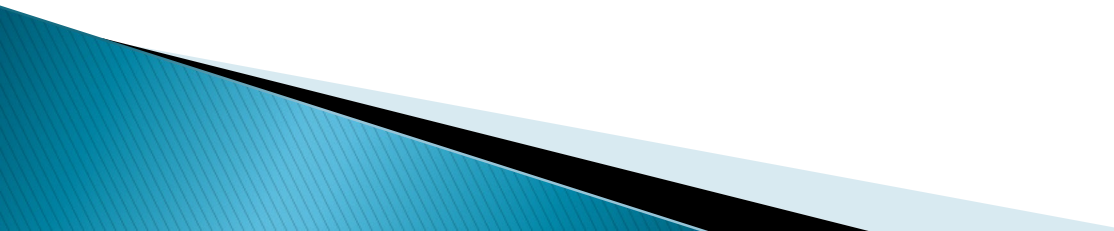
K Maps

Logic Diagram

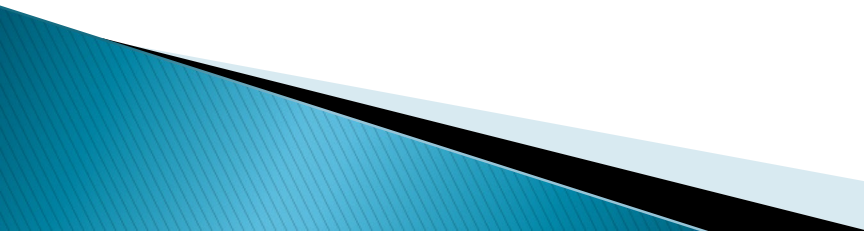


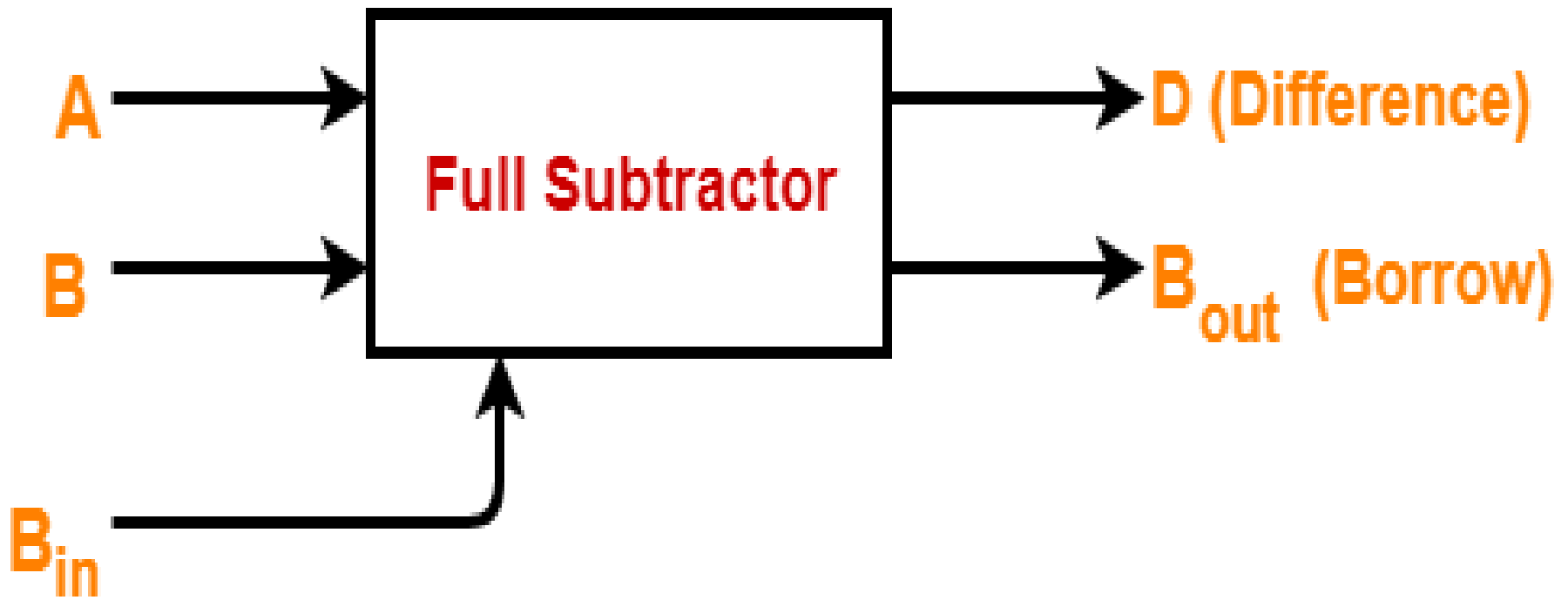
Half Subtractor Logic Diagram

Limitation of Half Subtractor

- ▶ Half subtractors do not take into account “Borrow-in” from the previous circuit.
 - ▶ This is a major drawback of half subtractors.
 - ▶ This is because real time scenarios involve subtracting the multiple number of bits which can not be accomplished using half subtractors.
 - ▶ To overcome this drawback, Full Subtractor comes into play
- 

Full subtractor

- ▶ **Full Subtractor is a combinational logic circuit.**
 - ▶ **It is used for the purpose of subtracting two single bit numbers.**
 - ▶ **It also takes into consideration borrow of the lower significant stage.**
 - ▶ **Thus, full subtractor has the ability to perform the subtraction of three bits.**
 - ▶ **Full subtractor contains 3 inputs and 2 outputs (Difference and Borrow) as shown-**
- 



Block Diagram of Full Subtractor

Truth Table

INPUTS			OUTPUTS	
A	B	B _{in}	B _{out} (borrow)	D(difference)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

K-maps

For D:

A		BB_{in}	$\bar{B}\bar{B}_{in}$	$\bar{B}B_{in}$	BB_{in}	$B\bar{B}_{in}$
		\bar{A}		1		1
\bar{A}	A	1		1		

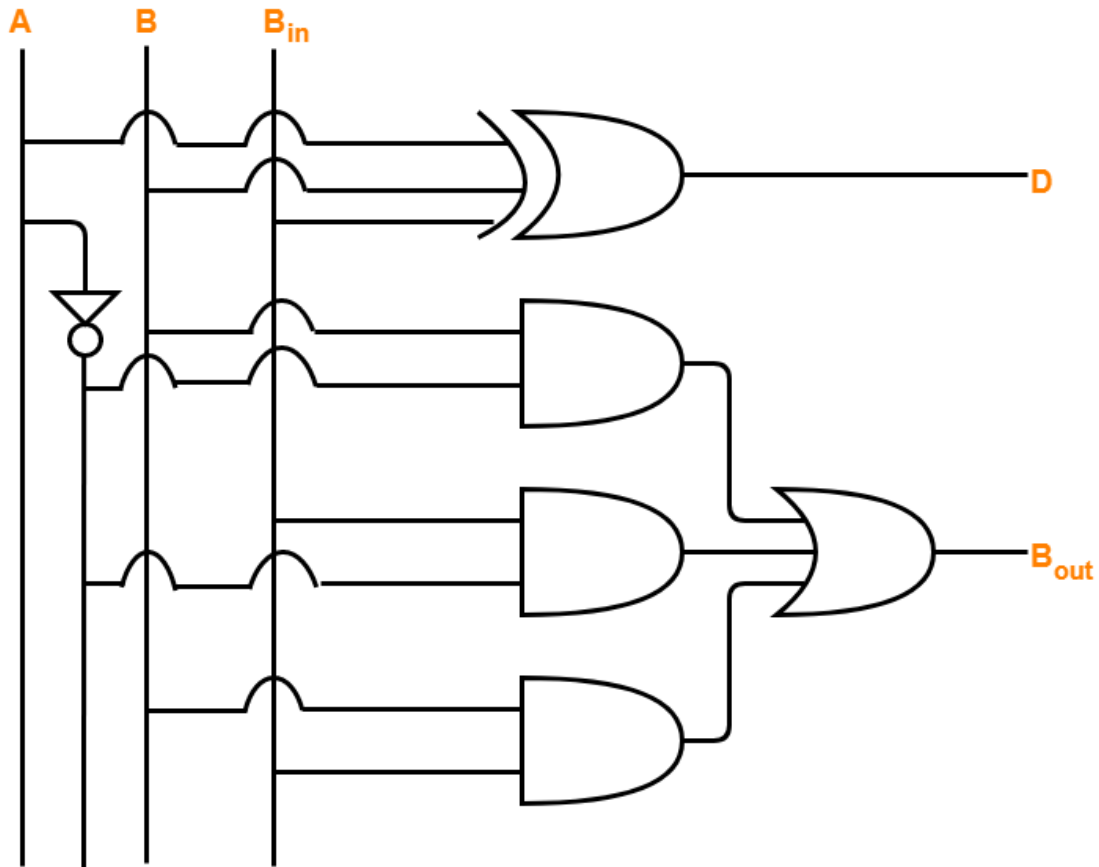
$$D = A \oplus B \oplus B_{in}$$

For B_{in} :

A		BB_{in}	$\bar{B}\bar{B}_{in}$	$\bar{B}B_{in}$	BB_{in}	$B\bar{B}_{in}$
		\bar{A}		1	1	1
\bar{A}	A			1		

$$B_{out} = \bar{A}B + (\bar{A} + B)B_{in}$$

Logic diagram



Full Subtractor Logic Diagram