

# Introduction

- The mobile radio channel places **fundamental limitations** on the **performance** of a wireless communication system
- The wireless transmission path may be
  - Line of Sight (LOS)
  - Non line of Sight (NLOS)
- Radio channels are **random** and **time varying**
- Modeling radio channels have been one of the **difficult** parts of mobile radio design and is done in **statistical manner**
- When electrons move, they create **EM waves** that can propagate through space.
- By using **antennas** we can transmit and receive these EM wave
- Microwave ,Infrared visible light and **radio waves** can be used.

# Properties of Radio Waves

- Are **easy to generate**
- Can **travel long distances**
- Can **penetrate buildings**
- May be used for both **indoor** and **outdoor** coverage
- Are **omni-directional**-can travel in all directions
- Can be narrowly **focused** at high frequencies(>100MHz) using parabolic antenna

# Properties of Radio Waves

- Frequency dependence
  - Behave more like light at high frequencies
    - Difficulty in passing obstacle
    - Follow direct paths
    - Absorbed by rain
  - Behave more like radio at lower frequencies
    - Can pass obstacles
    - Power falls off sharply with distance from source
- Subject to interference from other radio waves

# Propagation Models

- The statistical modeling is usually done based on **data measurements** made specifically for
    - the intended communication system
    - the intended spectrum
  - They are tools used for:
    - Predicting the **average signal strength** at a given distance from the transmitter
    - Estimating the **variability of the signal strength** in close spatial proximity to a particular locations
-



# Propagation Models

- Large Scale Propagation Model:
    - Predict the **mean signal strength** for an arbitrary transmitter-receiver(T-R) separation
    - Estimate radio coverage of a transmitter
    - Characterize signal strength over large T-R separation distances(several 100's to 1000's meters)
-

# Free Space Propagation Model

- For clear LOS between T-R
  - Ex: satellite & microwave communications
- Assumes that received power decays as a function of T-R distance separation raised to some power.

- Given by Friis free space eqn: 
$$P_r(d) = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2 L}$$

'L' is the system loss factor

L > 1 indicates loss due to transmission line attenuation, filter losses & antenna losses

L = 1 indicates no loss in the system hardware

- Gain of antenna is related to its effective aperture  $A_e$  by

$$G = 4 \pi A_e / \lambda^2$$

# Free Space Propagation Model

- Effective Aperture  $A_e$  is related to physical size of antenna.

$$\lambda = c/f.$$

- $c$  is speed of light,
- $P_t$  and  $P_r$  must be in same units
- $G_t$  and  $G_r$  are dimensionless
  
- An isotropic radiator, **an ideal radiator** which radiates power with unit gain uniformly in all directions, and is **often used as reference**
  
- Effective Isotropic Radiated Power (EIRP) is defined as
$$\text{EIRP} = P_t G_t$$
- Represents the **max radiated power** available from a transmitter in **direction of maximum antenna gain**, as compared to an isotropic radiator

# Free Space Propagation Model

- In practice Effective Radiated Power (ERP) is used instead of (EIRP)
- Effective Radiated Power (ERP) is radiated power compared to half wave dipole antennas
- Since dipole antenna has gain of 1.64(2.15 dB)  
$$\text{ERP} = \text{EIRP} - 2.15(\text{dB})$$
- the ERP will be **2.15dB smaller** than the EIRP for same Transmission medium



# Free Space Propagation Model

- Path Loss (PL) represents signal attenuation and is defined as difference between the effective transmitted power and received power

$$\begin{aligned} \text{Path loss } PL(\text{dB}) &= 10 \log [P_t/P_r] \\ &= -10 \log \{G_t G_r \lambda^2 / (4\pi)^2 d^2\} \end{aligned}$$

- Without antenna gains (with unit antenna gains)

$$PL = -10 \log \{ \lambda^2 / (4\pi)^2 d^2 \}$$

- Friis free space model is valid predictor for  $P_r$  for values of  $d$  which are in the far-field of transmitting antenna

# Free Space Propagation Model

- The far field or Fraunhofer region that is beyond far field distance  $d_f$  given as :

$$d_f = 2D^2/\lambda$$

- $D$  is the **largest physical linear dimension** of the transmitter antenna
- Additionally,  $d_f \gg D$  and  $d_f \gg \lambda$
- The Friis free space equation **does not hold for  $d=0$**
- Large Scale Propagation models **use a close-in distance,  $d_o$** , as received power reference point, **chosen such that  $d_o \geq d_f$**
- Received power in free space at a distance greater than  $d_o$

$$Pr(d) = Pr(d_o) (d_o/d)^2 \quad d > d_o > d_f$$

*Pr with reference to 1 mW is represented as*

$$Pr(d) = 10 \log(Pr(d_o)/0.001 W) + 20 \log(d_o/d)$$

*Electrostatic, inductive and radiated fields are launched, due to flow of current from antenna.*

*Regions far away from transmitter electrostatic and inductive fields become negligible and only radiated field components are considered.*

# Example

- What will be the far-field distance for a Base station antenna with
- Largest dimension  $D=0.5\text{m}$
- Frequency of operation  $f_c=900\text{MHz}, 1800\text{MHz}$
- For 900MHz
- $\lambda = 3 \cdot 10^8 / (900 \cdot 10^6) = 0.33\text{m}$
- $d_f = 2D^2 / \lambda = 2(0.5)^2 / 0.33 = 1.5\text{m}$

## Example

- If a transmitter produces 50 watts of power, express the transmit power in units of (a) dBm, and (b) dBW. If 50 watts is applied to a unity gain antenna with a 900 MHz carrier frequency, find the received power in dBm at a free space distance of 100 m from the antenna, What is  $P_r$  (10 km)? Assume unity gain for the receiver antenna.



# solution

Given:

Transmitter power,  $P_t = 50$  W.

Carrier frequency,  $f_c = 900$  MHz

Using equation (3.9),

(a) Transmitter power,

$$\begin{aligned}P_t (\text{dBm}) &= 10 \log [P_t (\text{mW}) / (1 \text{ mW})] \\ &= 10 \log [50 \times 10^3] = 47.0 \text{ dBm}.\end{aligned}$$

(b) Transmitter power,

$$\begin{aligned}P_t (\text{dBW}) &= 10 \log [P_t (\text{W}) / (1 \text{ W})] \\ &= 10 \log [50] = 17.0 \text{ dBW}.\end{aligned}$$

The received power can be determined using equation (3.1).

$$P_r = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2 L} = \frac{50 (1) (1) (1/3)^2}{(4\pi)^2 (100)^2 (1)} = 3.5 \times 10^{-5} \text{ W} = 3.5 \times 10^{-3} \text{ mW}$$

$$P_r (\text{dBm}) = 10 \log P_r (\text{mW}) = 10 \log (3.5 \times 10^{-3} \text{ mW}) = -24.5 \text{ dBm}.$$

The received power at 10 km can be expressed in terms of dBm using equation (3.9), where  $d_0 = 100$  m and  $d = 10$  km

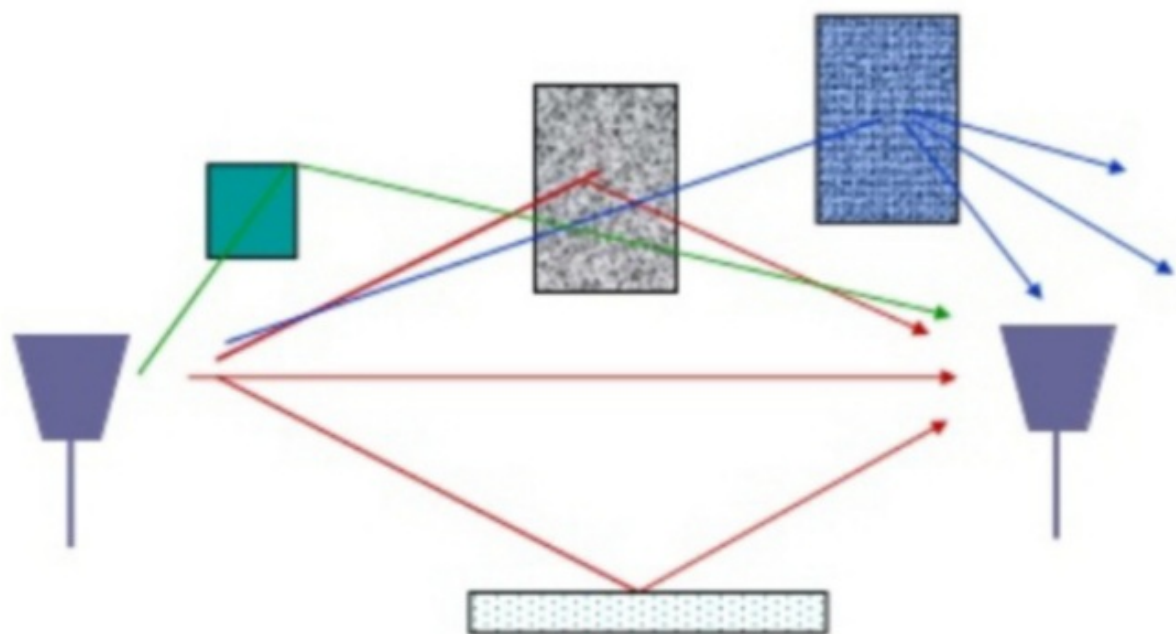
$$\begin{aligned}P_r (10 \text{ km}) &= P_r (100) + 20 \log \left[ \frac{100}{10000} \right] = -24.5 \text{ dBm} - 40 \text{ dB} \\ &= -64.5 \text{ dBm}.\end{aligned}$$



# Propagation Mechanisms

- Three basic propagation mechanism which impact **propagation in mobile radio** communication system are:

- Reflection
- Diffraction
- Scattering



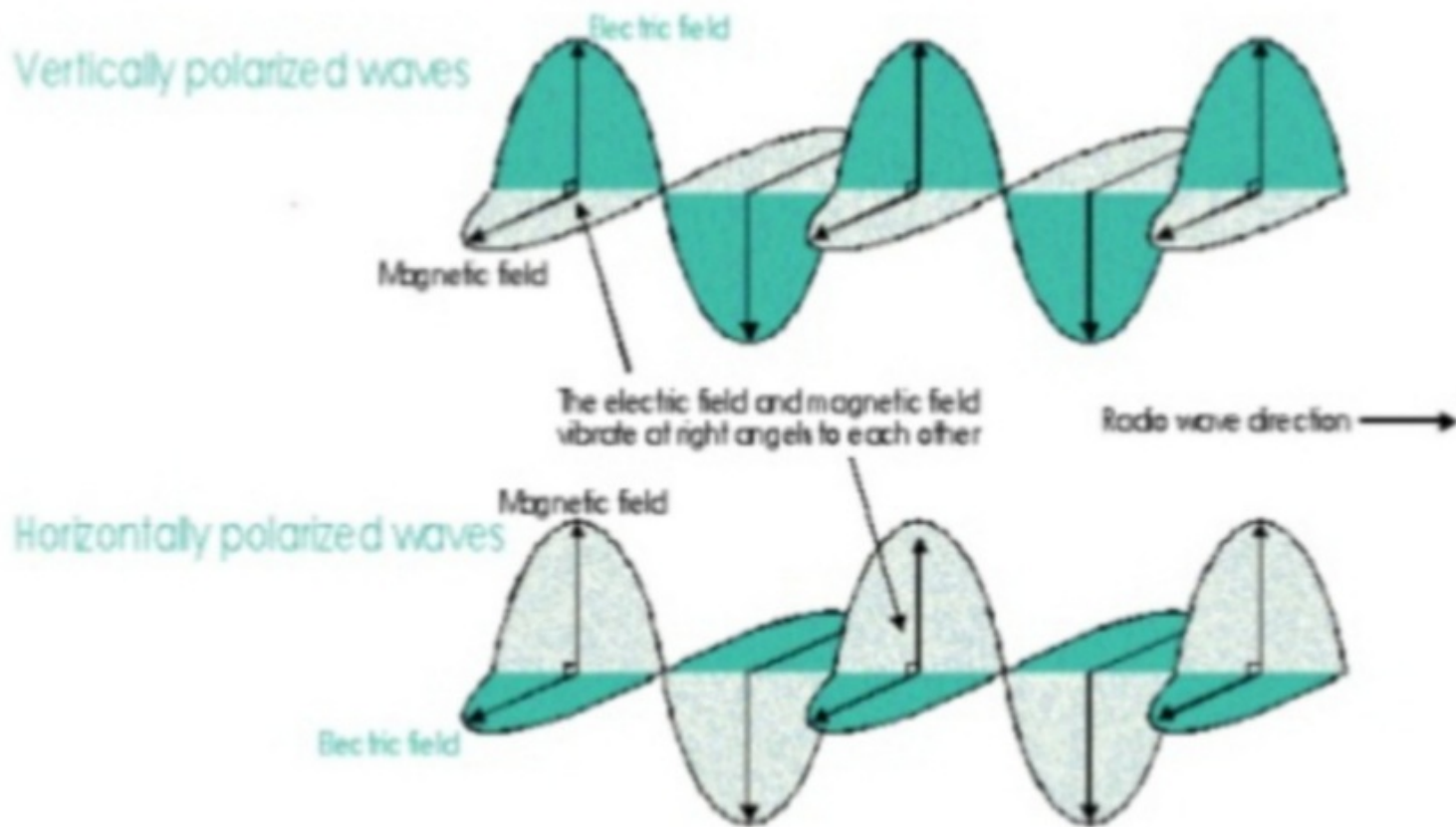
# Propagation Mechanisms

- Reflection occurs when a propagating electromagnetic wave impinges on an object which **has very large dimensions** as compared to **wavelength** e.g. surface of earth , buildings, walls
- Diffraction occurs when the radio path between the transmitter and receiver is **obstructed** by a surface that has sharp irregularities(edges)
  - Explains how radio signals can travel urban and rural environments without a line of sight path
- Scattering occurs when medium has objects that are **smaller or comparable** to the wavelength (small objects, irregularities on channel, foliage, street signs etc)

# Reflection

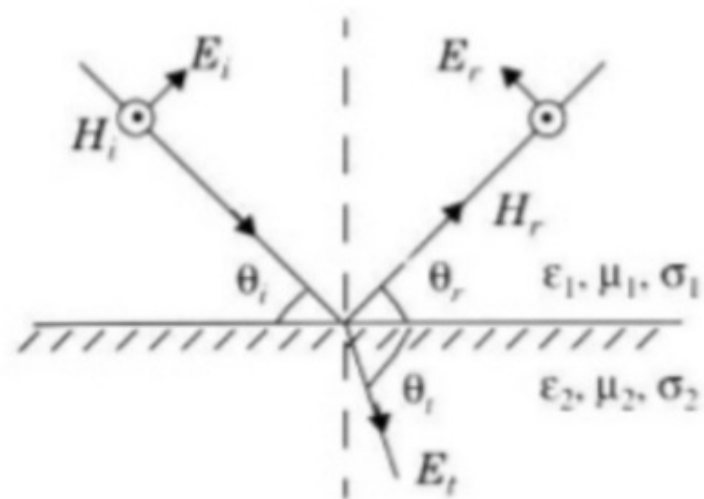
- Occurs when a radio wave propagating in one medium impinges upon another medium having **different electrical properties**
- If radio wave is incident on a **perfect dielectric**
  - Part of energy is reflected back
  - Part of energy is transmitted
- In addition to the **change of direction**, the **interaction** between the wave and boundary causes the **energy to be split between** reflected and transmitted waves
- The amplitudes of the reflected and transmitted waves are given relative to the incident wave amplitude by **Fresnel reflection coefficients**

# Vertical and Horizontal polarization

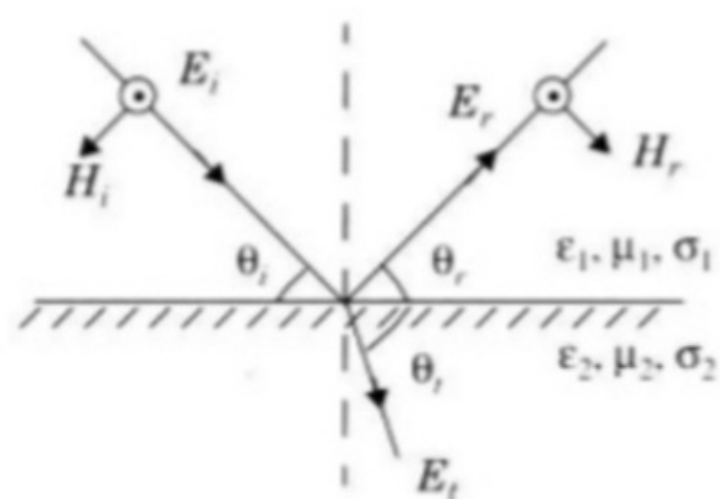




# Reflection- Dielectrics



(a) E-field in the plane of incidence



(b) E-field normal to the plane of incidence

**Figure 4.4** Geometry for calculating the reflection coefficients between two dielectrics.



# Reflection

- $\Gamma_{\parallel} = \frac{E_r}{E_i} = \frac{\eta_2 \sin \theta_t - \eta_1 \sin \theta_i}{\eta_1 \sin \theta_t + \eta_1 \sin \theta_i}$  (Parallel E-field polarization)
- $\Gamma_{\perp} = \frac{E_r}{E_i} = \frac{\eta_2 \sin \theta_i - \eta_1 \sin \theta_t}{\eta_1 \sin \theta_i + \eta_1 \sin \theta_t}$  (Perpendicular E-field polarization)
- These expressions express **ratio of reflected electric fields to the incident electric field** and depend on **impedance of media and on angles**
- $\eta$  is the intrinsic impedance given by  $\sqrt{(\mu/\epsilon)}$
- $\mu$ =permeability,  $\epsilon$ =permittivity

# Reflection-Perfect Conductor

- If incident on a perfect conductor the entire EM energy is reflected back
- Here we have  $\theta_r = \theta_i$
- $E_i = E_r$  (E-field in plane of incidence)
- $E_i = -E_r$  (E field normal to plane of incidence)
- $\Gamma(\text{parallel}) = 1$
- $\Gamma(\text{perpendicular}) = -1$

## Reflection - Brewster Angle

- It is the angle at which no reflection occur in the medium of origin. It occurs when the incident angle  $\theta_B$  is such that the reflection coefficient  $\Gamma(\text{parallel})$  is equal to zero.
- It is given in terms of  $\theta_B$  as given below

$$\text{Sin}(\theta_B) = \sqrt{\frac{\epsilon_1}{\epsilon_1 + \epsilon_2}}$$

- When first medium is a free space and second medium has an relative permittivity of  $\epsilon_r$  then

$$\text{Sin}(\theta_B) = \frac{\sqrt{\epsilon_r - 1}}{\sqrt{e_r^2 - 1}}$$

- Brewster angle only occur for parallel polarization

# Ground Reflection(Two Ray) Model

- In mobile radio channel, **single direct path** between base station and mobile and is **seldom** only physical means for propagation
- Free space model as a stand alone is inaccurate
- Two ray ground reflection model is useful
  - Based on geometric optics
  - Considers both direct and ground reflected path
- Reasonably accurate for predicting large scale signal strength over several kms that use tall tower height
- Assumption: The height of Transmitter >50 meters

# Ground Reflection(Two Ray) Model

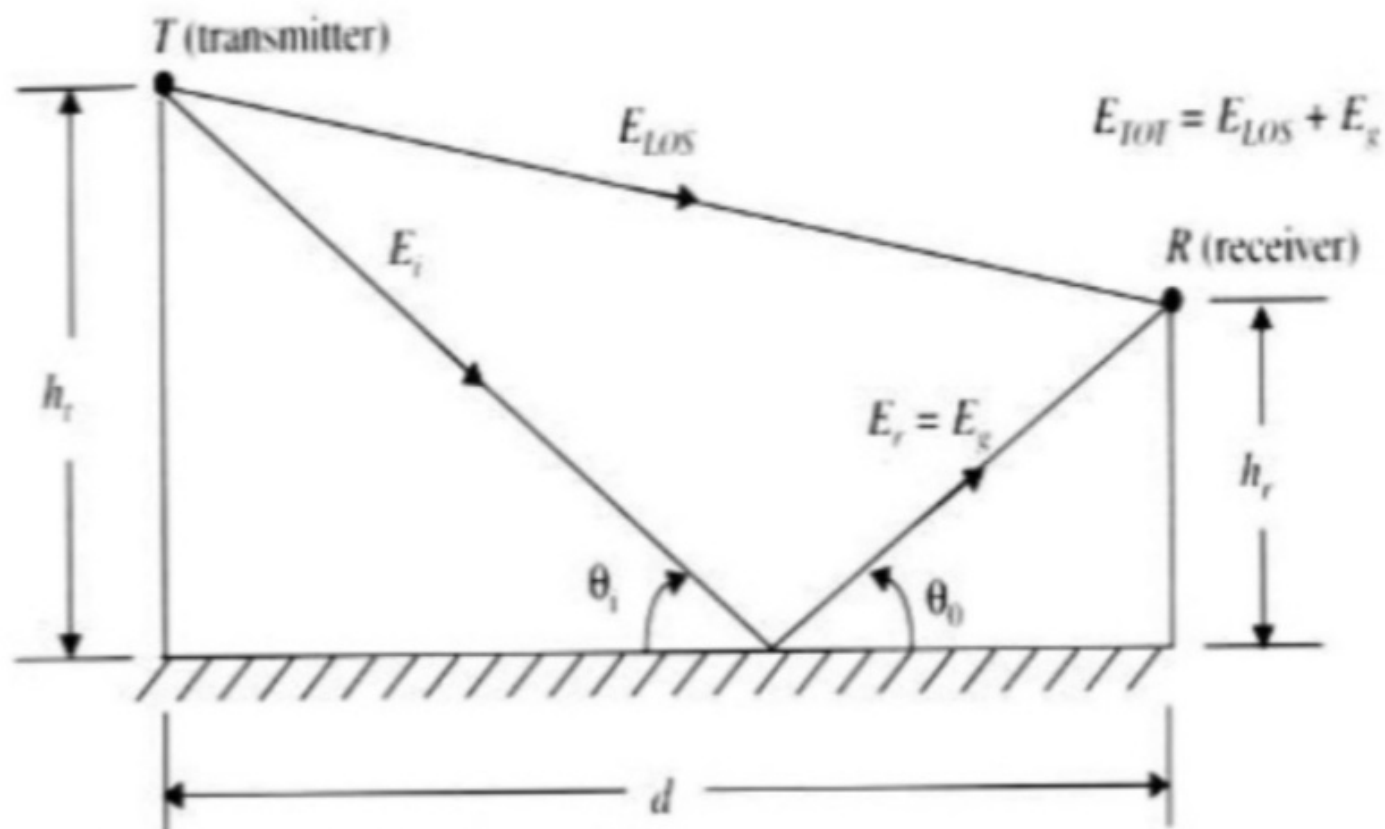


Figure 4.7 Two-ray ground reflection model.



# Ground Reflection(Two Ray) Model

$$\bar{E}_{TOT} = \bar{E}_{LOS} + \bar{E}_g$$

let  $E_0$  be  $|\bar{E}|$  at reference point  $d_0$  then

$$\bar{E}(d, t) = \left( \frac{E_0 d_0}{d} \right) \cos \left( \omega_c \left( t - \frac{d}{c} \right) \right) \quad d > d_0$$

$$E_{LOS}(d', t) = \frac{E_0 d_0}{d'} \cos \left( \omega_c \left( t - \frac{d'}{c} \right) \right) \quad E_g(d'', t) = \Gamma \frac{E_0 d_0}{d''} \cos \left( \omega_c \left( t - \frac{d''}{c} \right) \right)$$

$$\bar{E}_{TOT}(d, t) = \left( \frac{E_0 d_0}{d'} \right) \cos \left( \omega_c \left( t - \frac{d'}{c} \right) \right) + \Gamma \left( \frac{E_0 d_0}{d''} \right) \cos \left( \omega_c \left( t - \frac{d''}{c} \right) \right)$$

$$E_{TOT}(d, t) = \frac{E_0 d_0}{d'} \cos \left( \omega_c \left( t - \frac{d'}{c} \right) \right) + (-1) \frac{E_0 d_0}{d''} \cos \left( \omega_c \left( t - \frac{d''}{c} \right) \right)$$

# Ground Reflection(Two Ray) Model

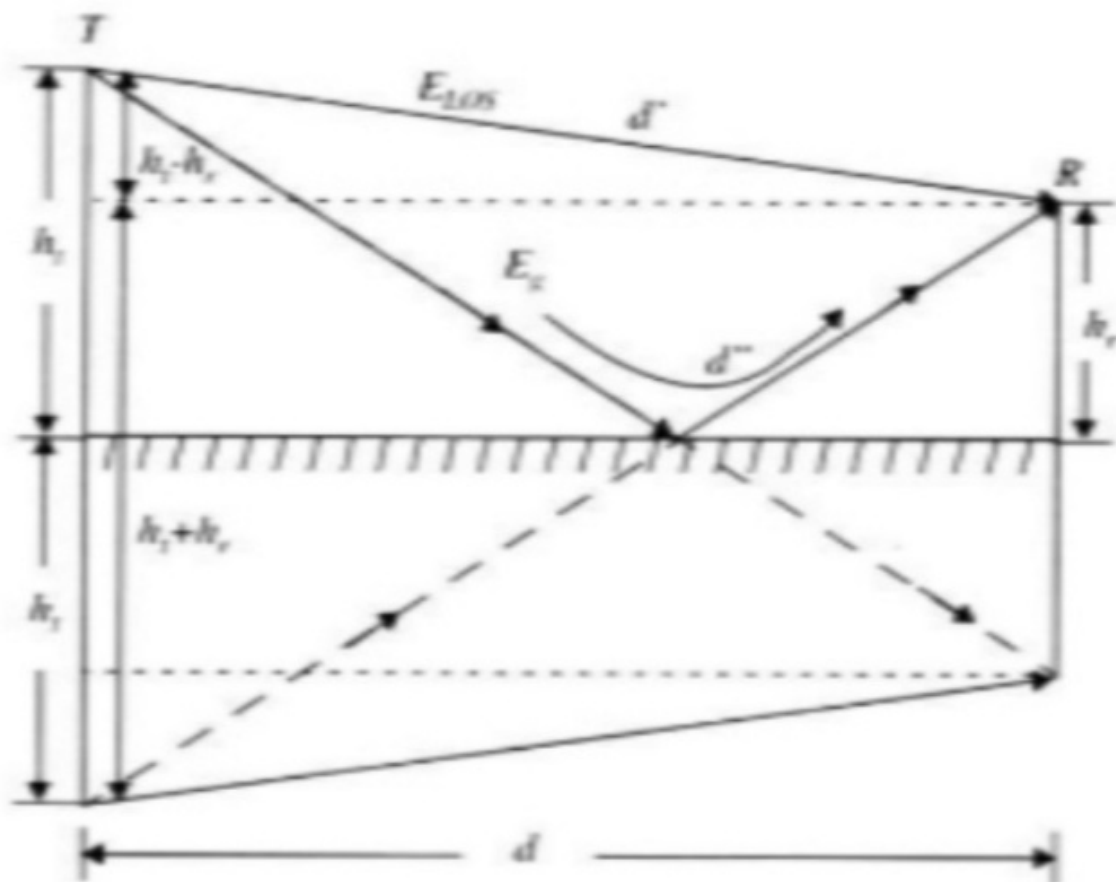


Figure 4.8 The method of images is used to find the path difference between the line-of-sight and the ground reflected paths.

## Path Difference

$$\begin{aligned}\Delta &= d'' - d' = \sqrt{(h_t + h_r)^2 + d^2} - \sqrt{(h_t - h_r)^2 + d^2} \\ &= d \sqrt{\left( \left( \frac{h_t + h_r}{d} \right)^2 + 1 \right)} - d \sqrt{\left( \left( \frac{h_t - h_r}{d} \right)^2 + 1 \right)} \\ &\approx d \left( 1 + \frac{1}{2} \left( \frac{h_t + h_r}{d} \right)^2 \right) - d \left( 1 + \frac{1}{2} \left( \frac{h_t - h_r}{d} \right)^2 \right) \\ &\approx \frac{1}{2d} \left( (h_t + h_r)^2 - (h_t - h_r)^2 \right) \\ &\approx \frac{1}{2d} \left( (h_t^2 + 2h_t h_r + h_r^2) - (h_t^2 - 2h_t h_r + h_r^2) \right) \\ &\approx \frac{2h_t h_r}{d}\end{aligned}$$

# Phase difference

$$\theta_{\Delta} \text{ radians} = \frac{2\pi\Delta}{\lambda} = \frac{2\pi\Delta}{\left(\frac{c}{f_c}\right)} = \frac{\omega_c \Delta}{c}$$

$$|E_{TOT}(t)| = 2 \frac{E_0 d_0}{d} \sin\left(\frac{\theta_{\Delta}}{2}\right)$$

$$\frac{\theta_{\Delta}}{2} \approx \frac{2\pi h_r h_t}{\lambda d} < 0.3 \text{ rad}$$

$$E_{TOT}(t) \approx 2 \frac{E_0 d_0}{d} \frac{2\pi h_r h_t}{\lambda d} \approx \frac{k}{d^2} \text{ V/m}$$

$$P_r = P_t G_t G_r \frac{h_t^2 h_r^2}{d^4}$$

# Diffraction

- Diffraction is the **bending of** wave fronts around obstacles.
- Diffraction allows radio signals to propagate behind obstructions and is thus one of the factors why we receive signals at locations where there is **no line-of-sight** from base stations
- Although the received field strength decreases rapidly as a receiver moves deeper into an obstructed (shadowed) region, the diffraction field still exists and often has sufficient signal strength to produce a useful signal.



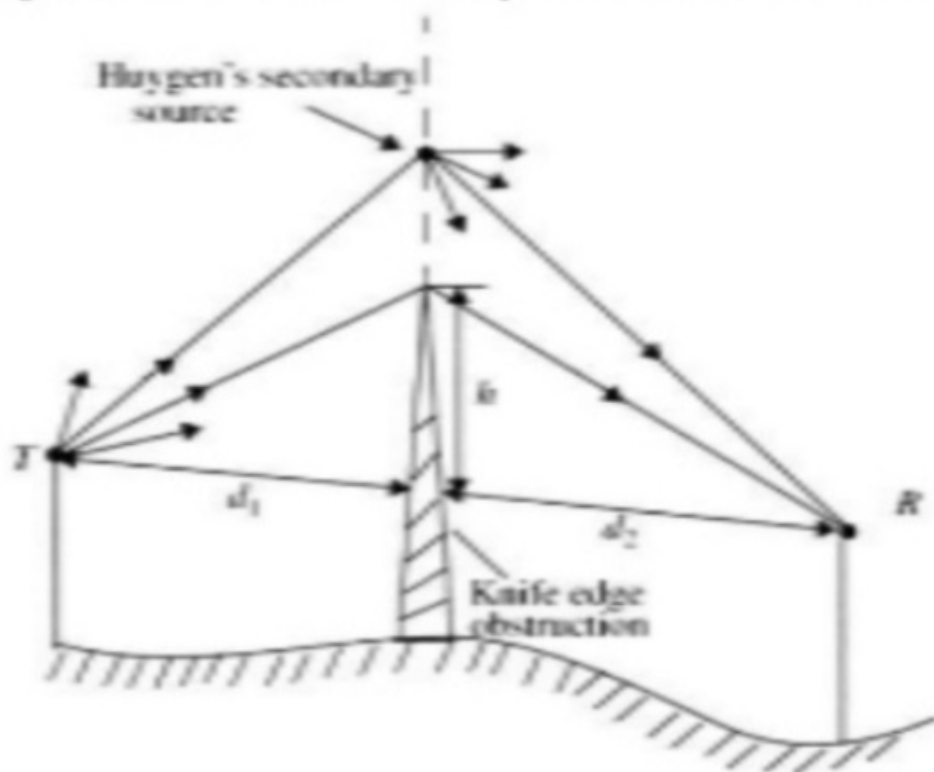


# Knife-edge Diffraction Model

- **Estimating** the signal attenuation caused by **diffraction** of radio waves **over hills and buildings** is essential in predicting the **field strength** in a given service area.
- As a starting point, the **limiting case of propagation over a knife edge** gives good insight into the order of magnitude diffraction loss.
- When shadowing is **caused by a single object** such as a building, the attenuation caused by diffraction **can be estimated by treating the obstruction as a diffracting knife edge**

# Knife-edge Diffraction Model

Consider a receiver at point  $R$  located in the shadowed region. The field strength at point  $R$  is a vector sum of the fields due to all of the secondary Huygens sources in the plane above the knife edge.



**Figure 4.13** Illustration of knife-edge diffraction geometry. The receiver  $R$  is located in the shadow region.