

Least cost method

The Least Cost Method is **another method used to obtain the initial feasible solution for the transportation problem**. Here, the allocation begins with the cell which has the minimum cost. The lower cost cells are chosen over the higher-cost cell with the objective to have the least cost of transportation.

	Warehouse P	Warehouse Q	Warehouse R	Warehouse S	Source
Plant A	5	1	3	3	34
Plant B	3	3	5	4	15
Plant C	6	4	4	3	12
Plant D	4	1	4	2	19
Demand	21	25	17	17	

Step-1: Check given problem is balanced transportation problem or unbalanced transportation problem.

For balanced transportation problem, sum of demand should equal to sum of supply

For given problem,

$$\text{Total Demand} = 21 + 25 + 17 + 17 = 80$$

$$\text{Total Supply} = 34 + 15 + 12 + 19 = 80$$

So balanced transportation problem.

Cost Matrix

5	1	3	3
3	3	5	4
6	4	4	3
4	1	4	2

Find the least cost in cost matrix .

$$C(1, 2) = 1$$

$$C(4, 2) = 1$$

Select any cell out of C(1,2) or C(4,2)

I have selected C(1,2) .

Demand of ware house Q = 25

Supply of plant A = 34

So allocate 25 unit to C(1, 2)

	Warehouse P	Warehouse Q	Warehouse R	Warehouse S	Source
Plant A	5	1 ₍₂₅₎	3	3	34 (9)
Plant B	3	3	5	4	15
Plant C	6	4	4	3	12
Plant D	4	1	4	2	19
Demand	21	25 (0)	17	17	

Next least cost matrix C (4, 4) = 2

Demand of ware house S = 17

Supply of plant D = 19

Allocate 17 unit to C (4, 4)

	Warehouse P	Warehouse Q	Warehouse R	Warehouse S	Source
Plant A	5	1 ₍₂₅₎	3 ₍₉₎	3	34 (9) (0)
Plant B	3	3	5	4	15
Plant C	6	4	4	3	12
Plant D	4	1	4	2 ₍₁₇₎	19 (2)
Demand	21	25 (0)	17 (8)	17 (0)	

Next least cost matrix C (1, 3) and C(2 ,1)

Select any one of them. I have selected C (1, 3)

Demand of warehouse R = 17

Remaining Supply of plant A =9

So allocate 9 unit to cell C (1, 3)

	Warehouse P	Warehouse Q	Warehouse R	Warehouse S	Source
Plant A	5	1 ₍₂₅₎	3 ₍₉₎	3	34 (9) (0)
Plant B	3 ₍₁₅₎	3	5	4	15 (0)
Plant C	6	4	4	3	12
Plant D	4	1	4	2 ₍₁₇₎	19 (2)
Demand	21	25 (0)	17 (8)	17 (0)	

Next least cost cell is C (2,1) = 3

Demand of ware house P = 21

Supply of plant B = 15

Allocate C (2,1) = 15

	Warehouse P	Warehouse Q	Warehouse R	Warehouse S	Source
Plant A	5	1 ₍₂₅₎	3 ₍₉₎	3	34 (9) (0)
Plant B	3 ₍₁₅₎	3	5	4	15 (0)
Plant C	6 ₍₄₎	4	4 ₍₈₎	3	12 (4) (0)
Plant D	4 ₍₂₎	1	4	2 ₍₁₇₎	19 (2) (0)
Demand	21 (6)(4)(0)	25 (0)	17 (8) (0)	17 (0)	

$$\begin{aligned} \text{Cost} &= 1 \times 25 + 3 \times 9 + 3 \times 15 + 6 \times 4 + 4 \times 8 + 4 \times 2 + 2 \times 17 \\ &= 195 \end{aligned}$$