

\* Direct Recombination of Electrons and Holes:- Filtrations of conduction band

recombine with Holes in the valance band either directly or indirectly. In the direct recombination electrons falling from the conduction band to empty states (holes) in the valance band. The energy lost by an electron in making the transition is given up as a photon. Direct recombination is spontaneous.

The probability of recombining of an electron and a hole is constant in time.

$$\frac{d[n(t)]}{dt} = \underbrace{\alpha_1 n_i^2}_{\text{rate of generation, (Thermal generation)}} - \underbrace{\alpha_2 n(t) p(t)}_{\text{rate of recombination}} \quad \dots \quad (i)$$

rate of change of conduction band electrons

We know that.

$$\begin{aligned} \text{Rate of recombination } &\propto n(t) p(t) \\ &= \alpha_2 n(t) p(t) \end{aligned}$$

where  $\alpha_2$  = Recombination Coefficient.

Let assume Excess EHP is at  $t=0$ . Initial electron - Hole concentrations  $\Delta n$  and  $\Delta p$  are equal.

The instantaneous concentrations of excess carriers =  $\delta n(t), \delta p(t)$ .

Now we can write equation (i) in the terms of equilibrium values  $n_0$  and  $p_0$  and excess carrier concentrations  $\delta n(t) = \delta p(t)$ .

$$\begin{aligned} \frac{d[\delta n(t)]}{dt} &= \alpha_1 n_i^2 - \alpha_2 [n_0 + \delta n(t)] [p_0 + \delta p(t)] \\ &= - \alpha_2 [(n_0 + p_0) \delta n(t)] + \delta n^2(t) \\ &= - \alpha_2 [(n_0 + p_0) \delta n(t) + \delta n^2(t)] \quad \dots \quad (ii) \end{aligned}$$

The equation (ii) is nonlinear and it is difficult to solve it. We simplified for the case of Low-level Injection.  $\delta n^2$ .

If excess carrier concentrations small then we neglect  $\delta n^2$ .  
If material is extrinsic then we can neglect the term representing equilibrium minority carriers.

Suppose P type then  $P_0 \gg n_0$ .

$$\therefore \frac{d(\delta n(t))}{dt} = -\alpha_r P_0 \delta n(t)$$

The solution of this equation is an exponential decay from the original excess carrier concentration  $\Delta n$ .

$$\begin{aligned} \delta n(t) &= \Delta n e^{-\alpha_r P_0 t} \\ &= \Delta n e^{-t/\tau_n} \end{aligned}$$

Where,  $\tau_n = (\alpha_r P_0)^{-1}$ , called decay constant or recombination life time.

$$\begin{aligned} \tau_p &= (\alpha_r n_0)^{-1} \\ \tau_n &= (\alpha_r P_0)^{-1} \end{aligned}$$

Problem:-  $\therefore$  A sample of GaAs is doped with  $10^{15}/\text{cm}^3$  (acceptor)  $10^6/\text{cm}^3$ , the intrinsic carrier concentration of GaAs is  $10^6/\text{cm}^3$ , the minority electron concentration is  $n_0$ . The minority  $10^{14}$  EHP/ $\text{cm}^3$  are created at  $t=0$ , &  $\tau_n = 10^{-8}$  s. find  $\alpha_r$  (Recombination Coefficient).

Solution:-

$$\begin{aligned} P_0 &\approx N_A = 10^{15}/\text{cm}^3 \\ n_i &= 10^6/\text{cm}^3 \\ n_0 &= \frac{n_i^2}{P_0} = \frac{(10^6)^2}{10^{15}} = 10^{-3} \end{aligned}$$

$$P_0 \gg n_0$$

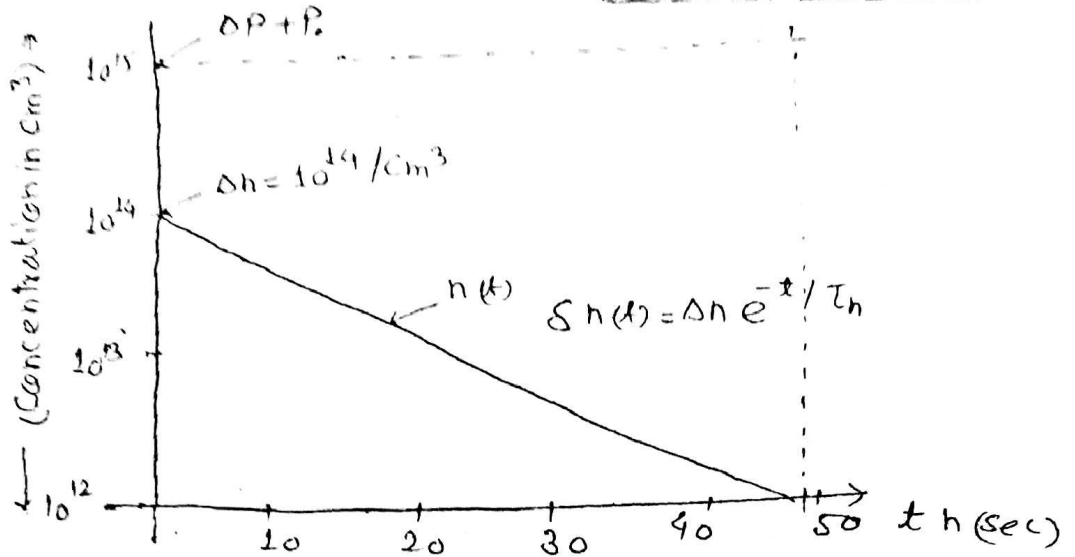
$$\therefore \tau_n = (\alpha_r P_0)^{-1}$$

$$= \frac{1}{10^{12} \text{ Sec} \times 10^{15} / \text{cm}^3}$$

$$= 10^{-7} \text{ cm}^3 / \text{Sec}$$

$$\alpha_1 = 10^{-7} \text{ cm}^3 / \text{Sec}$$

The exponential decay of  $\delta n(t)$  is linear in Grats.

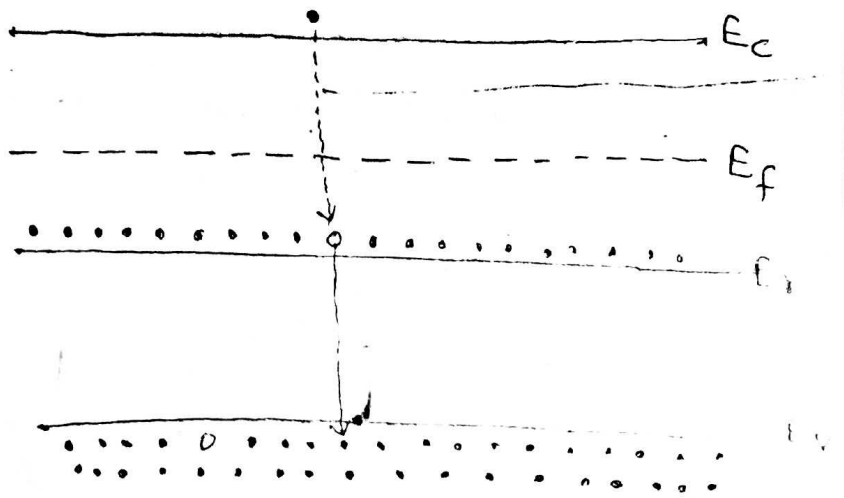


\* Indirect Recombination or Trapping \* - The figure shows - Indirect Recombination

$E_r$  is recombination level which is below  $E_f$  at equilibrium and filled with electrons. When excess electrons and holes are created in this material each EHP recombines at  $E_r$  in two steps -

- Hole Capture and
- Electron Capture,

Since the recombination centres are filled at equilibrium, the first event in the recombination process is Hole Capture. This process is equivalent to an electron of valence band falling at  $E_r$ , leaving behind an empty state in the recombination level.



and leaving behind an empty state in the recombination level. Thus in Hole Capture, energy is given to heat to the lattice.

Falling of electron from  $E_v$  to  $E_c$  valence band  $\rightarrow$  Hole capture  
Conduction band electron falling to  $E_v$   $\rightarrow$  Electron capture,

49.

electron capture must follow the Hole capture means if Hole capture occurs the electron capture will occur. Energy is leaving as a heat in both steps.

When both events occur then recombination centre is back to its original state (filled with an electron) but an EHP is missing. Thus one recombination has taken place and the centre is ready to participate in another recombination event by capturing of a hole.

Unequal time required for capturing of each type of carrier. It means the electron capture does not follow hole capture immediately after hole capture.

When a carrier is trapped temporarily at a centre and then is reexcited without recombination taking place, the process is called temporarily trapping.

The effects of recombination and trapping can be measured by an photoconductive decay experiment. The conductivity of the sample during decay is -

$$\sigma(t) = q [n(t) \mu_n + p(t) \mu_p]$$

$\rightarrow$  Electron capture,

$\rightarrow$  Recombination level, or, trapping centre or, defect level.

$\rightarrow$  Hole capture

Steady state Carrier Generation :-

The steady state carrier and holes concentrations are given in the terms of Fermi levels. The Fermi level  $E_f$  is meaningful only when no excess carriers are present. We can write steady state electron and holes concentrations as expressions in the equilibrium by defining quasi-Fermi levels  $F_n$  and  $F_p$  for electrons and holes.

$$\left. \begin{aligned} n &= n_i e^{(E_f - E_i)/kT} \\ p &= n_i e^{(E_i - E_f)/kT} \end{aligned} \right\}$$

"

The thermal generation of EHPs -

$$g(T) = g_i \quad \text{- for intrinsic semiconductor,}$$

$$g(T) = \alpha_i n_i^2 = \alpha_r n_0 p_0 \quad \text{----- (i)}$$

where,  $\alpha_r$  = recombination coefficient.

$n_i$  = Intrinsic carrier concentration.

$n_0, p_0$  = electron, Hole concentrations at thermal equilibrium.

a light is shown on the sample, an optical generation rate  $g_{op}$  will be added to the thermal generation -

$$g(T) + g_{op} = \alpha_r np$$

$$= \alpha_r (n_0 + \delta n)(p_0 + \delta p) \quad \text{----- (ii)}$$

here,  $n_0$  and  $p_0$  are equilibrium concentrations and.

$\delta n, \delta p$  are departures, for no trapping  $\delta n = \delta p$ .

using becomes

$$g(T) + g_{op} = \alpha_r [n_0 p_0 + \delta n(n_0 + p_0) + \delta n^2]$$

$$\cancel{g(T) + g_{op}} = \alpha_r n_0 p_0 + \alpha_r \delta n(n_0 + p_0) + \alpha_r \delta n^2$$

$$g_{op} = \alpha_r (n_0 + p_0) \delta n$$

$$g_{op} = \frac{\delta n}{\tau_n}$$

$\delta n^2$  is neglected for Low level Injection.

Hence excess carrier concentration written as -

$$\delta n = \delta p = g_{op} \tau_n$$

The photoconductivity:

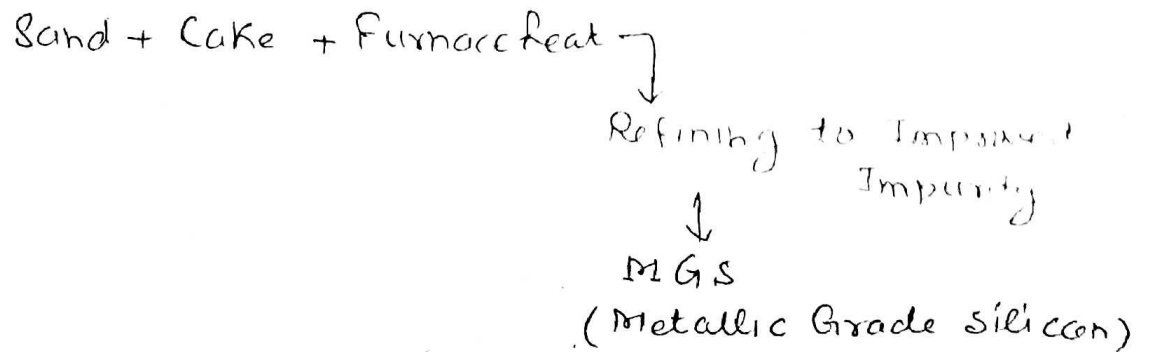
$$\sigma = q g_{op} (\tau_n \mu_n + \tau_p \mu_p)$$

Similar to conductivity of semiconductor.

\* Fabrication of Junctions:- Mainly following techniques are used for fabrication of junctions:-

- 1. Grown junctions,
- 2. Alloyed junctions
- 3. Diffused junctions
- 4. Ion Implantation
- 5. Epitaxial junctions

⇒ Grown junctions :- Grown junctions are fabricated by using crystal growth process. In this process a single crystal of silicon is obtained. As we already know that silicon achieved from sand. under following steps-



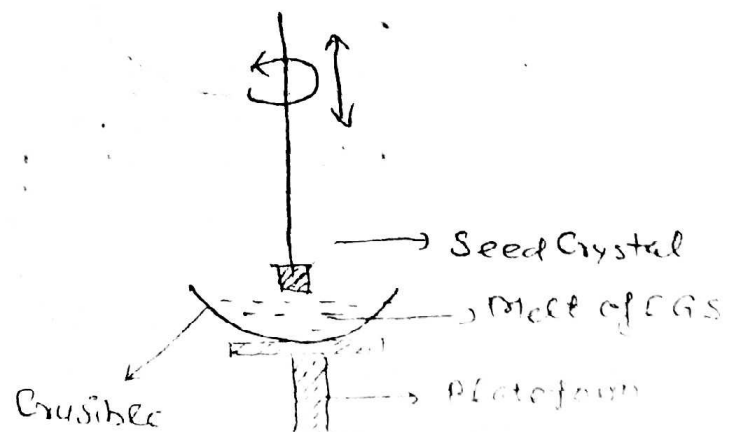
This metallic grade silicon is impure and polycrystalline.

Metallic Grade Silicon under treatment → Electron Grade Silicon (EGS)  
Pure material  
But polycrystalline

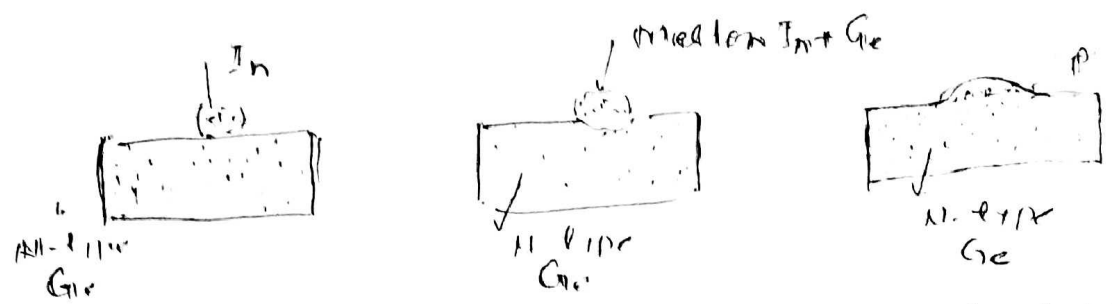
CZ process:- CZ process is used for converting this EGS into single crystal silicon.

Required amount of Impurity is added for N type & P type semiconductor.

Firstly Boron is added and growth process is stop and then further phosphorus is added.



Alloyed junctions : Alloyed junctions are fabricated by using alloying technique. In this technique a metal is alloyed with a semiconductor with the opposite type of dopant.

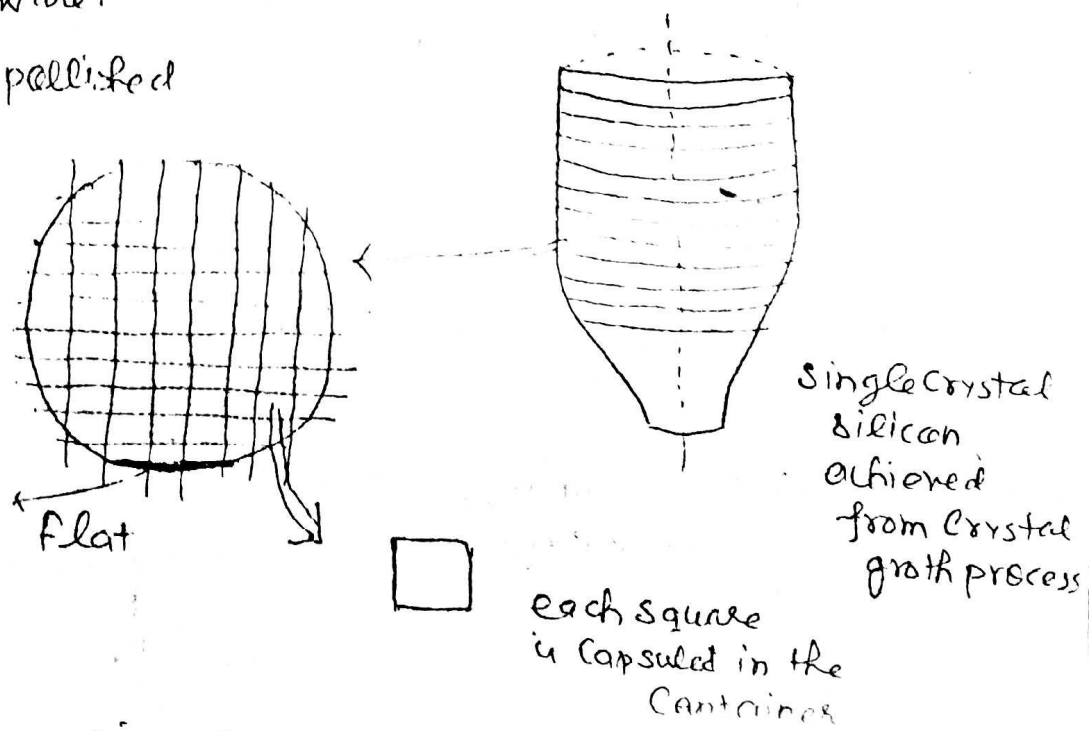


(a) Pellet of In in contact with n-type Ge, (b) Molten phase of In & Ge mixture during heating (c) Cross section view of alloyed junction.

This process was used in the 1950 to produce diode and transistors. For example in the figure above, a sample of Ge was heated with a pellet of In on it.

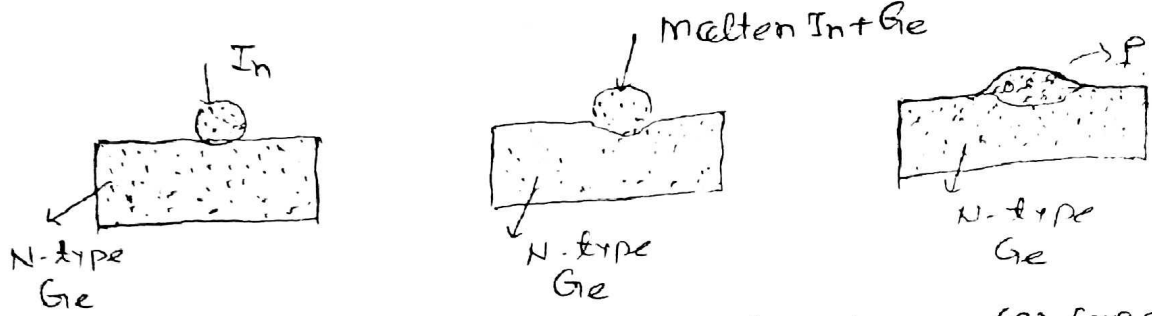
Diffused junctions :- Diffused junctions are fabricated for IC technology purpose. In the IC-fabrication technology - After CZ process a single crystal silicon is obtained in the form of cylinder as shown in the figure. we cut it in equal shape parts. Each part is circular and called Si-wafer.

New wafer is polished and doped



To make diffused junctions photolithography process is used. photolithography process is a selective diffusion process to control junction geometry.

Allayed junctions :- Allayed junctions by using allaying technique. In this technique a metal is allayed on a semiconductor with the opposite type of dopant.



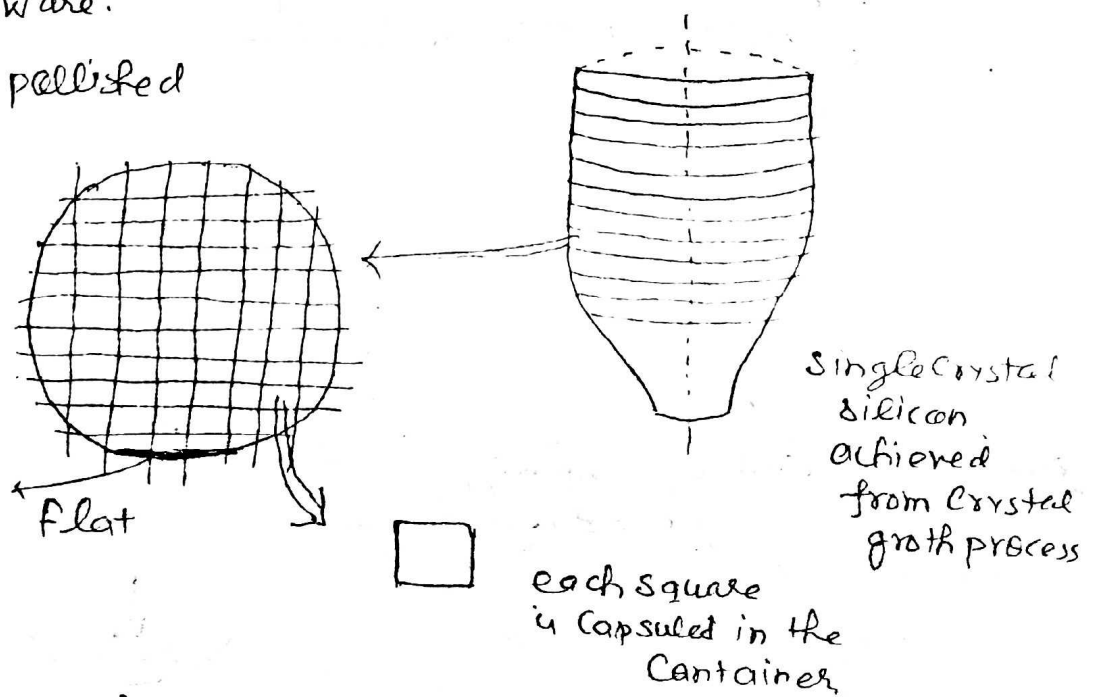
(a) Pellet of In in contact with n type Ge, (b) Molten phase of In & Ge mixture during heating, (c) cross section view of allayed junction.

This process was used in the 1950 to produce diode and transistors. For example in the figure above, a sample of Ge can be heated with a pellet of In on it.

➔ Diffused junctions :- Diffused junctions are fabricated for IC technology purpose. In the IC-fabrication technology.

- After CZ process a single crystal silicon is obtained in the form of cylinder as shown in the figure. we cut it in equal shape parts. Each part is circular and called Si-ware.

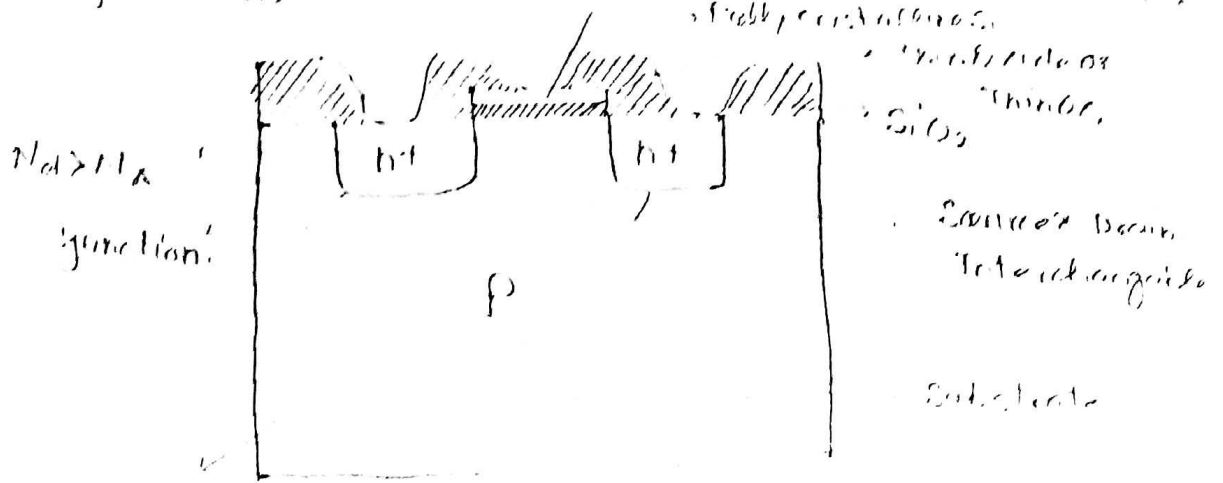
New wafer is polished and d and



To make diffused junctions photolithography process is used. photolithography process is a selective diffusion process to control junction geometry.



Figure shows structure of n-mos where junctions are diffused junctions. 57



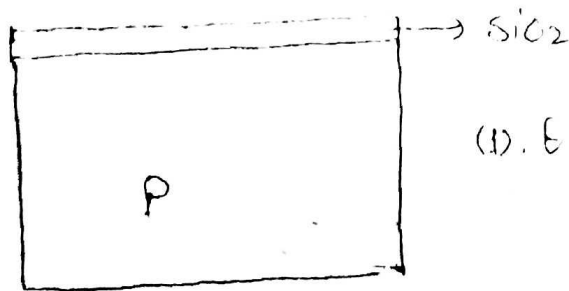
In this region  $N_A > 10^{18}$

Structure of n-mos:-

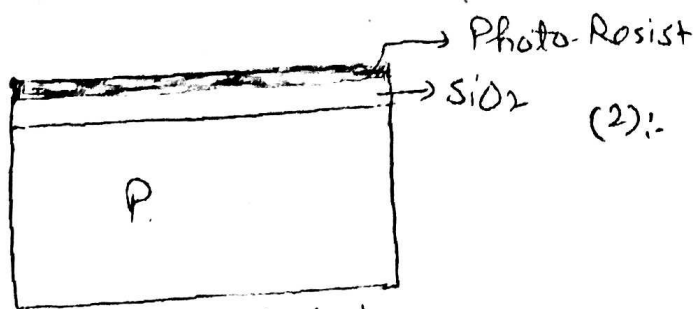
(actually cross-section view of n-mos)

while 3 dimensional view of n-mos looks as usual.

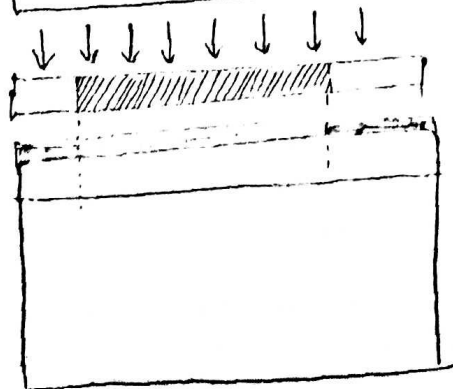
Making a n-mos following steps are used-



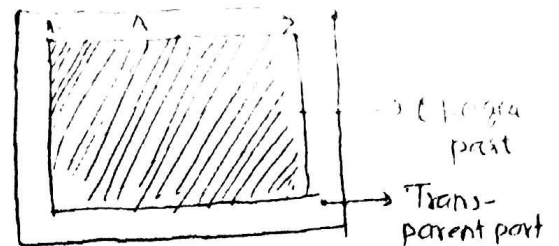
(1). Etched Si sample



(2):- Apply a Layer of Photoresist.



(3) :- Expose PR through Photomask A.



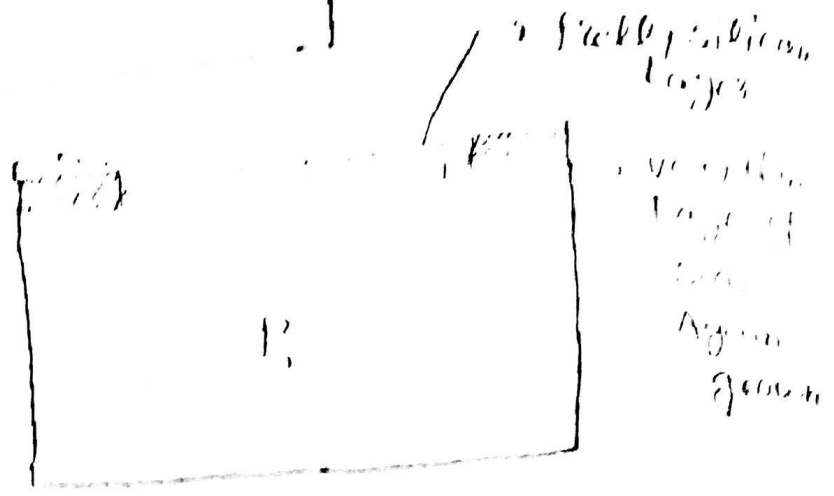
Glass Photomask

→ (Top view of Glass photomask)

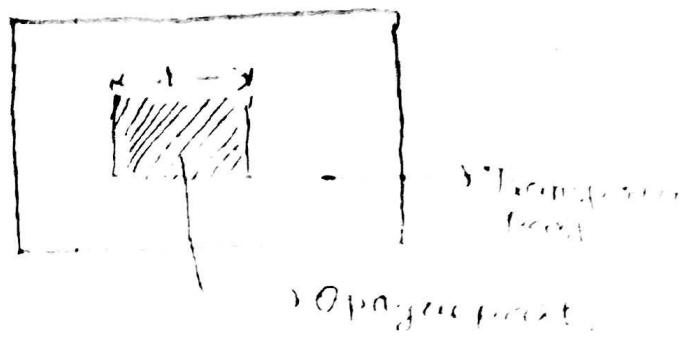
4. opening of  
the window  
- for diffusion.



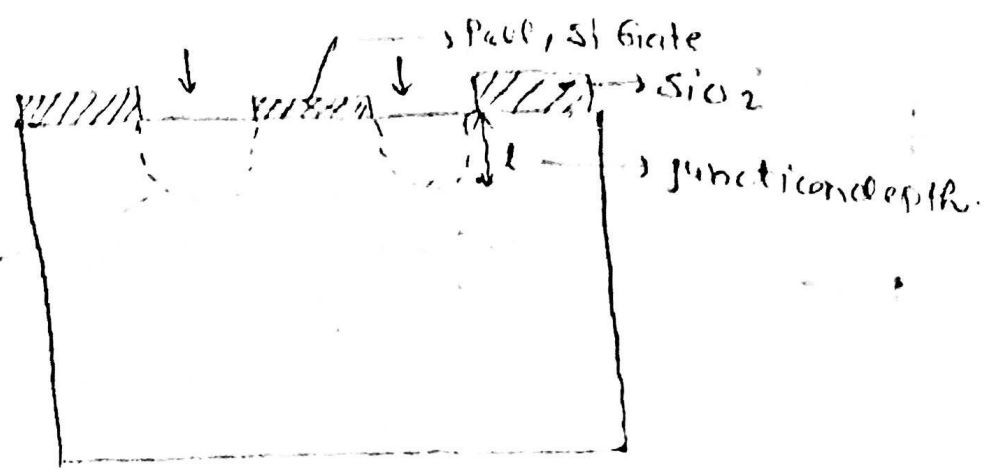
5. polly silicon  
is coated using  
chemical vapour  
deposition.  
Polly silicon is Gate  
Layer.



6. After forming gate.  
Again making mask  
and repeat all  
previous steps again



7.

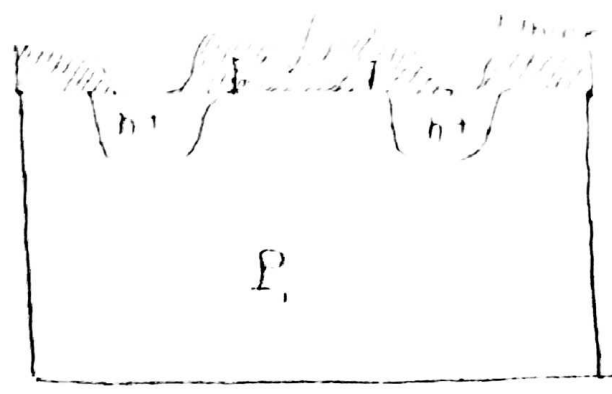


Area for  
N diffusion

Now these two windows I, J are ready to make  
N region.

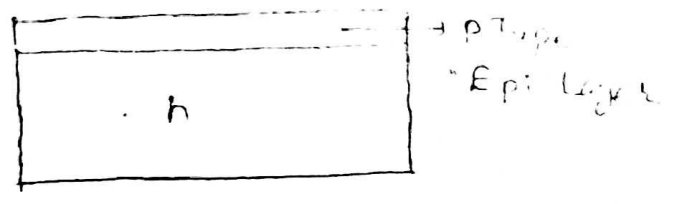
The depth of junction depends upon following parameters →  
Diffusion time,  
Pressure, and other parameters.

→ For making N regions, Ion implantation is  
used.



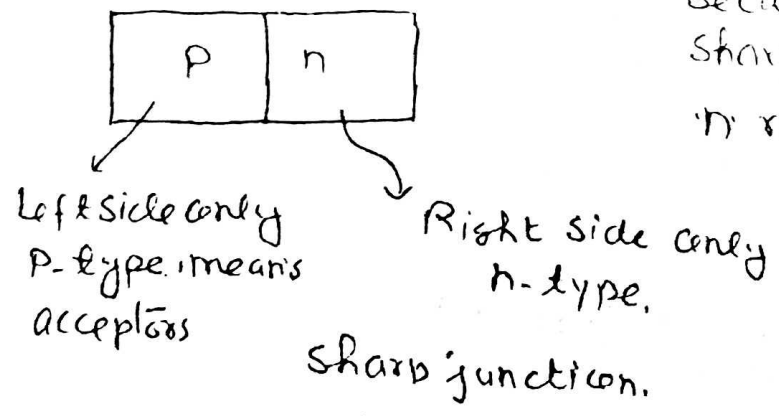
Depletion type, n-MOS.

> Epitaxial Junctions: Epitaxial junctions are formed by using epitaxy process. In the epitaxy process a layer is deposited by using chemical vapour deposition process. The epitaxial layer some times called 'epi' layer.



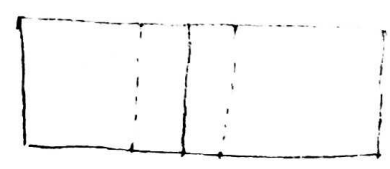
Epitaxial junctions & Aligned junctions are modeled as  $\Rightarrow$  step junction

$\Downarrow$   
Because there is sharp 'p' region and 'n' region.



On other hand, diffused junctions are called  $\Rightarrow$  Graded junctions because.

$N_A - N_D$  varies across the junction.

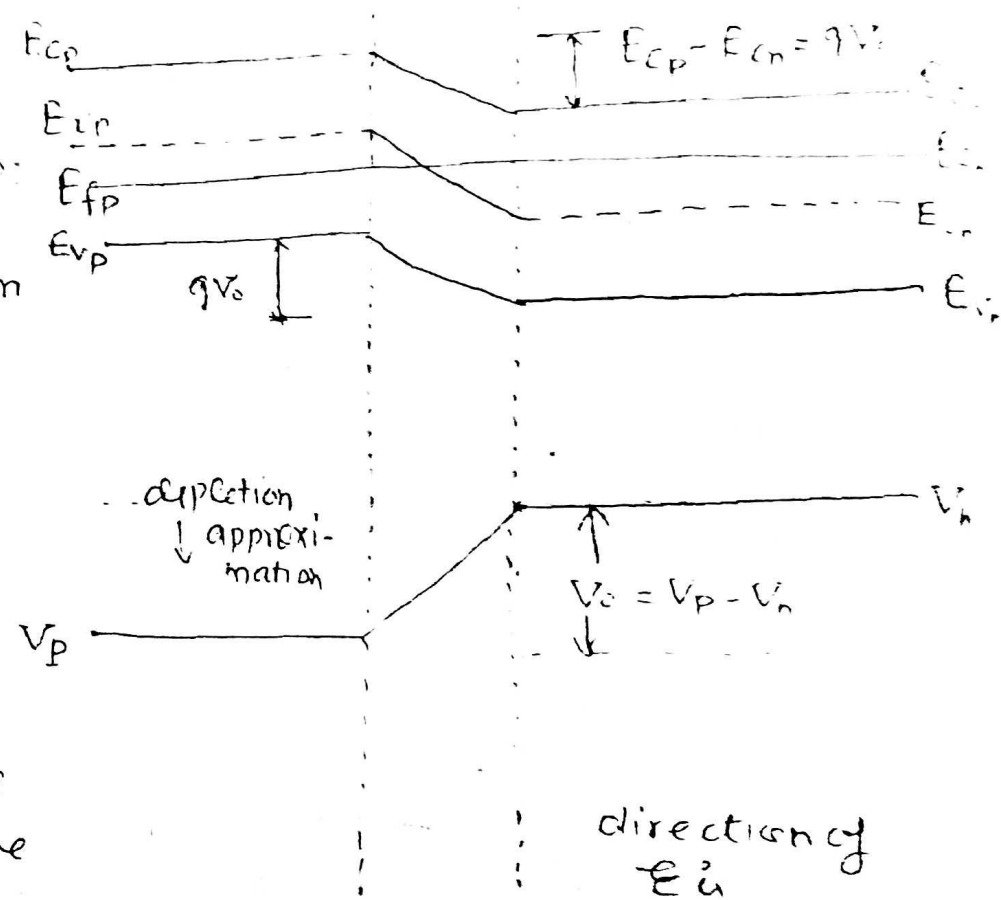
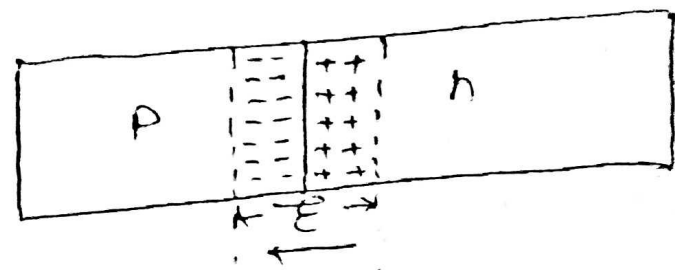


$N_A - N_D$  varies across the junction.

P-n Junction:- As a common general n-type and p-type then junction formed at Equilibrium. Equilibrium means no biasing at Equilibrium Fermi level at same energy level through the device.

As junction is formed diffusion of charge carriers starts in opposite region.

Due to diffusion depletion region is developed. Due to development of transition region an field  $E$  acting at junction. The direction of field is + to -ve. side.



The potential curve shows gradient in the Intrinsic level,

$V_p$  = Occure due to diffused Acceptor.

$V_n$  = Occure due to diffused donor.

& 
$$V_0 = V_p - V_n$$

$V_0$  = Called Contact potential

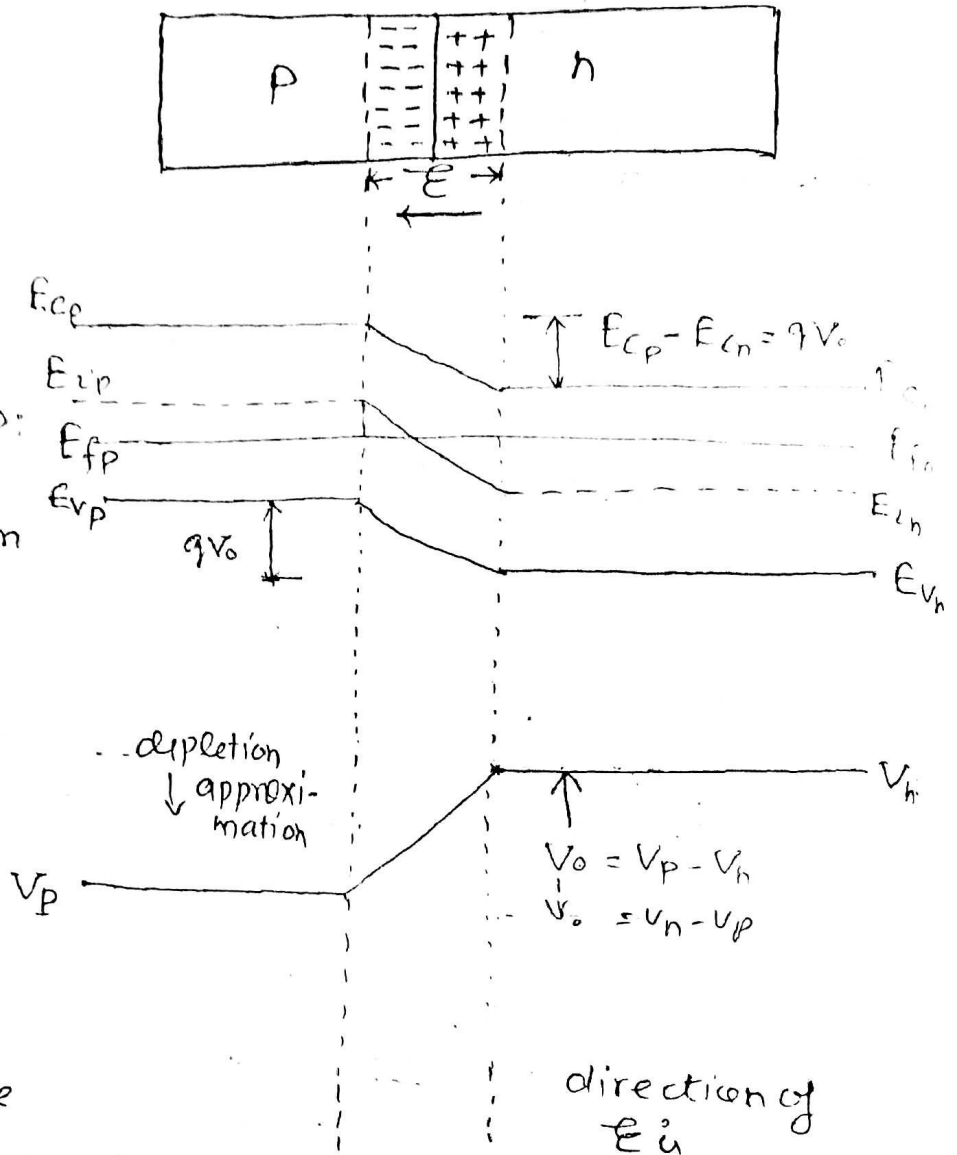
Following four terms are Occure at Equilibrium —

→ 1. Hole diffusion.

→ 2. Hole drift

• P-n Junction:- Let us consider junction is step type, when joined p-type and n-type then junction is formed at Equilibrium. Equilibrium means no biasing. At Equilibrium Fermi level at same energy level through the device.

As junction is formed diffusion of charge carriers starts in opposite region. Due to diffusion, depletion region or transition region is developed. Due to development of transition region an field  $E$  acting at junction. The direction of field is + to -ve. side.



The potential curve shows gradient in the intrinsic level.

$V_p$  = Occure due to diffused Acceptor.

$V_n$  = Occure due to diffused donor.

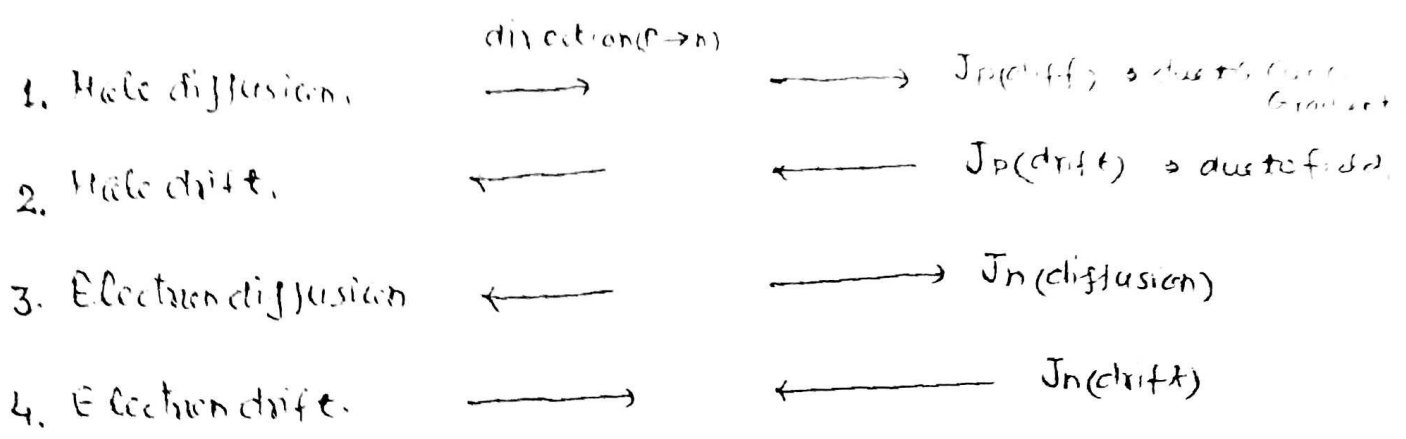
& 
$$V_0 = V_p - V_n$$

$V_0$  = Called Contact potential

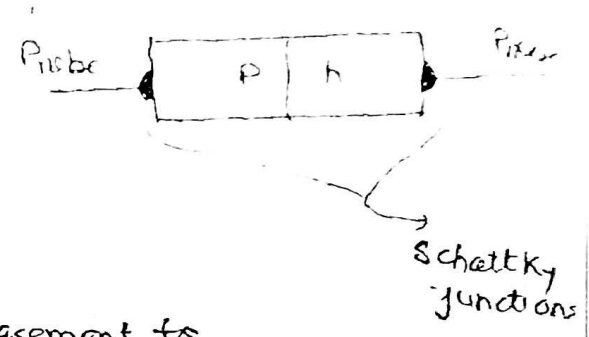
Following four terms are Occure at Equilibrium —

→ 1. Hole diffusion.

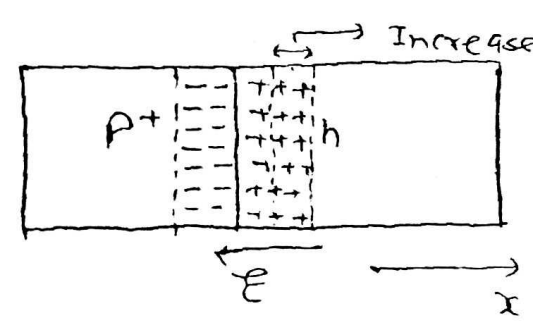
$$\left. \begin{aligned} J_p(\text{drift}) + J_p(\text{diffusion}) &= 0 \\ J_n(\text{drift}) + J_n(\text{diffusion}) &= 0 \end{aligned} \right\} \text{at Equilibrium}$$



Note: 1 The contact potential  $V_0$  can not be measured because when we connected prods then Schottky junctions are formed at the ends.



Note: 2



balancing concentration in p+ region.

Now-

$$E = - \frac{dV(x)}{dx}$$

field is opposite to direction of x.

⇒ Now we consider Hole current density at equilibrium-

$$J_p(x) = q \left[ \underbrace{\mu_p P(x)}_{\text{drift}} E(x) - \underbrace{D_p \frac{dP(x)}{dx}}_{\text{diffusion}} \right] = 0$$

$$\text{or } \mu_p P(x) E(x) = D_p \frac{dP(x)}{dx}$$

$$\frac{\mu_p}{D_p} E(x) = \frac{1}{P(x)} \frac{dP(x)}{dx}$$

$$\left. \begin{aligned} E(x) &= - \frac{dV(x)}{dx} \\ \frac{\mu_p}{D_p} \cdot \frac{q}{kT} \cdot \frac{dV(x)}{dx} &= \frac{1}{P(x)} \frac{dP(x)}{dx} \\ - \frac{q}{kT} \int_{V_p}^{V_n} dV &= \int_{P_p}^{P_n} \frac{1}{P} dP \end{aligned} \right\}$$

Hence equation (i) becomes -

$$\frac{q}{kT} = - \frac{dV(x)}{dx} = \frac{1}{P(x)} \frac{dP(x)}{dx} \quad \text{--- (ii)}$$

Now integrating equation (ii) under the limits

$$- \frac{q}{kT} \int_{V_p}^{V_n} dV(x) = \int_{P_p}^{P_n} \frac{1}{P} dP$$

where,  $P_p$  = concentration in p-region.

$P_n$  = concentration in n-region.

$$- \frac{q}{kT} (V_n - V_p) = \log P_n - \log P_p$$

$$= \log \frac{P_n}{P_p}$$

$$\therefore - \frac{q}{kT} (V_n - V_p) = \log \frac{P_n}{P_p}$$

$$\frac{q}{kT} (V_n - V_p) = \log \frac{P_p}{P_n}$$

$$\frac{q}{kT} V_0 = \log \frac{P_p}{P_n}$$

$$\therefore \boxed{V_0 = \frac{kT}{q} \log \frac{P_p}{P_n}} \quad \text{--- (iii)}$$

$P_p$  = concentration in p-region =  $N_a$

$P_n = n_i^2 / N_d$  = concentration in n-region.

$$\Rightarrow V_0 = \frac{kT}{q} \log \frac{N_a}{n_i^2 / N_d}$$

$$= \frac{kT}{q} \log \frac{N_a N_d}{n_i^2}$$

$$\Rightarrow \boxed{V_0 = \frac{kT}{q} \log \frac{N_a N_d}{n_i^2}} \quad \text{--- (iv)}$$