

Mechanical system

Mechanical systems are of two types,

- (i) Translational mechanical system and
- (ii) Rotational mechanical system.

The motion takes place along a straight line is known as translational motion.

The rotational motion of a body can be defined as the motion of a body about a fixed axis.

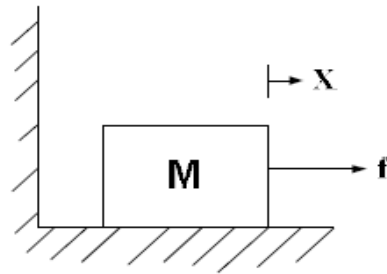
Translational mechanical system

There are three basic elements in a translational mechanical system,

- (a) Mass
- (b) spring
- (c) Damper

Mass: A mass is denoted by M . If a force f is applied on it and it displays distance x , then

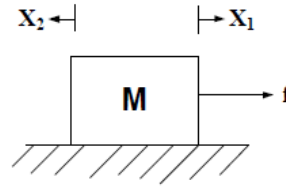
$$f = M \frac{d^2x}{dt^2}$$



Force applied on a mass with displacement in one direction

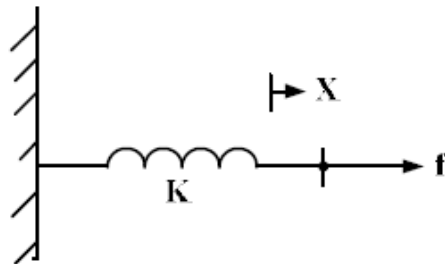
If a force f is applied on a **mass M** and it displays distance x_1 in the direction of f and distance x_2 in the opposite direction, then

$$f = M \left(\frac{d^2 x_1}{dt^2} - \frac{d^2 x_2}{dt^2} \right)$$



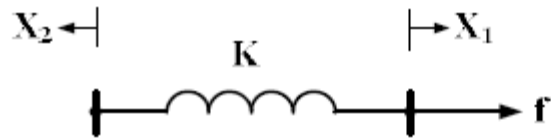
Force applied on a mass with displacement two directions

(b) **Spring:** A spring is denoted by K. If a force f is applied on it and it displays distance x , then $f = Kx$ as shown



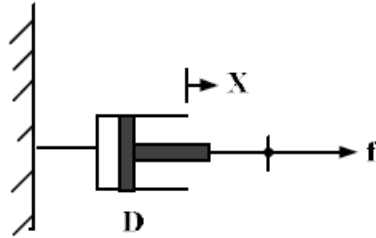
Force applied on a spring with displacement in one direction

If a force f is applied on a spring K and it displays distance x_1 in the direction of f and distance x_2 in the opposite direction, then $f = K(x_1 - x_2)$ as shown in Fig



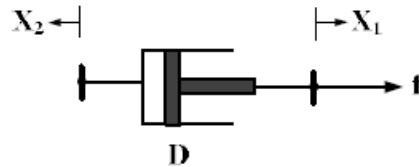
Force applied on a spring with displacement in two directions

Damper: A damper is denoted by D . If a force f is applied on it and it displays distance x , then $f = D \frac{dx}{dt}$ as shown in Fig.



Force applied on a damper with displacement in one direction

If a force f is applied on a damper D and it displays distance x_1 in the direction of f and distance x_2 in the opposite direction, then $f = D \left(\frac{dx_1}{dt} - \frac{dx_2}{dt} \right)$ as shown in Fig.



Rotational mechanical system

There are three basic elements in a Rotational mechanical system, i.e. (a) inertia, (b) spring and (c) damper.

- (a) **Inertia:** A body with an inertia is denoted by J . If a torque T is applied on it and it displays distance θ , then $T = J \frac{d^2\theta}{dt^2}$. If a torque T is applied on a body with inertia J and it displays distance θ_1 in the direction of T and distance θ_2 in the opposite direction, then $T = J \left(\frac{d^2\theta_1}{dt^2} - \frac{d^2\theta_2}{dt^2} \right)$.
- (b) **Spring:** A spring is denoted by K . If a torque T is applied on it and it displays distance θ , then $T = K\theta$. If a torque T is applied on a body with inertia J and it displays distance θ_1 in the direction of T and distance θ_2 in the opposite direction, then $T = K(\theta_1 - \theta_2)$.
- (c) **Damper:** A damper is denoted by D . If a torque T is applied on it and it displays distance θ , then $T = D \frac{d\theta}{dt}$. If a torque T is applied on a body with inertia J and it

displays distance θ_1 in the direction of T and distance θ_2 in the opposite direction, then $T = D \left(\frac{d\theta_1}{dt} - \frac{d\theta_2}{dt} \right)$.

Force-voltage Analogy

Translational	Rotational	Electrical
Force (f)	Torque (T)	Voltage (v)
Mass (M)	Inertia (J)	Inductance (L)
Damper (D)	Damper (D)	Resistance (R)
Spring (K)	Spring (K)	Elastance (1/C)
Displacement (x)	Displacement (Θ)	Charge (q)
Velocity (u) = \dot{x}	Velocity (u) = $\dot{\theta}$	Current (i) = \dot{q}

Force-current analogy

Translational	Rotational	Electrical
Force (f)	Torque (T)	Current (i)
Mass (M)	Inertia (J)	Capacitance (C)
Damper (D)	Damper (D)	Conductance (1/R)
Spring (K)	Spring (K)	Reciprocal of Inductance (1/L)
Displacement (x)	Displacement (Θ)	Flux linkage (ψ)
Velocity (u) = \dot{x}	Velocity (u) = $\dot{\theta}$	Voltage (v) = $\dot{\psi}$