

Date: 25/10/23

## Lecture - 28

### -: Energy Balance:-

#### Topics

Thermophysics

Energy

External

Kinetic  
(motion)  
Potential

(position, compression,  
elongation, surface energy  
flow (PV) energy)

Enthalpy,  $H = U + PV$

$$\Delta H = \Delta U + \Delta(PV) = \Delta U + P\Delta V + V\Delta P$$

Flow work  $\approx \Delta(PV)$

Internal (U)

Internal

Kinetic (motion)  
Potential

Translational  
Rotational  
Vibrational

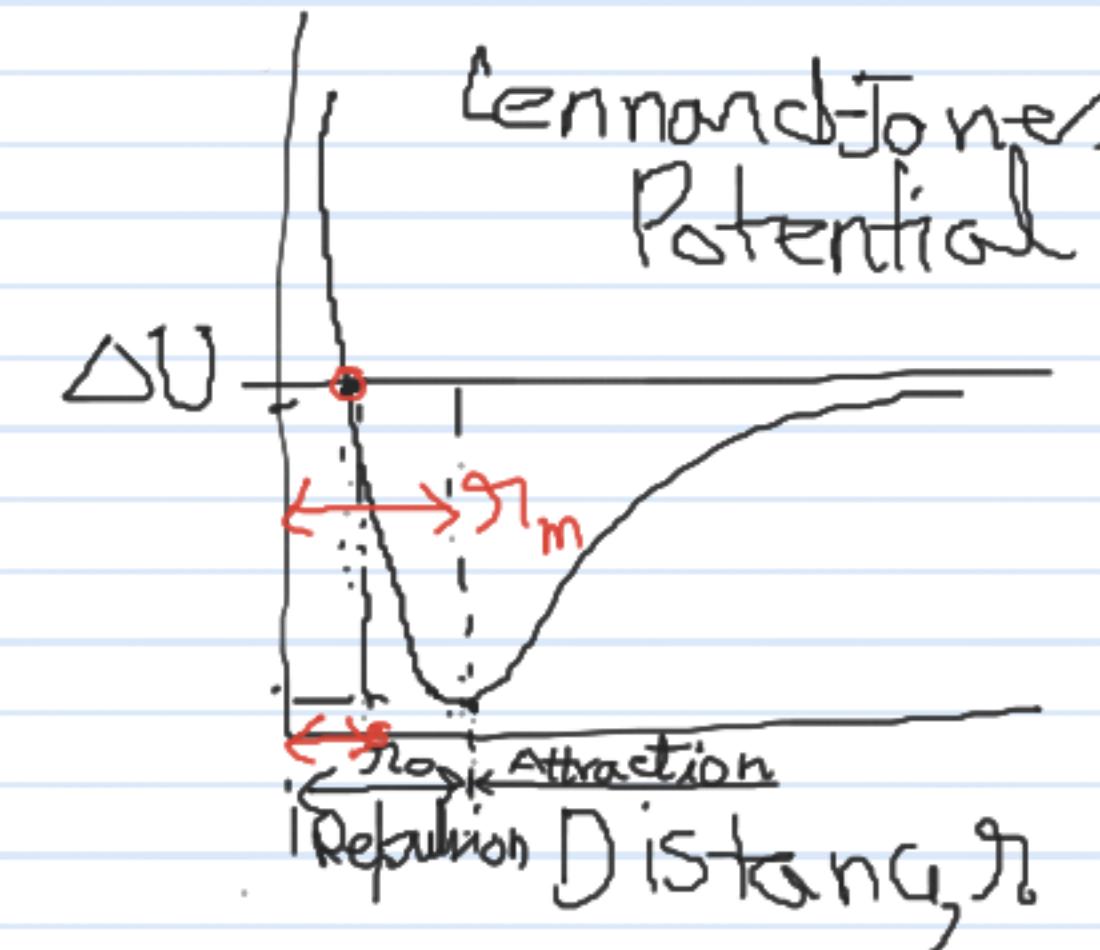
Thermochimistry

Heat of reactions

(Heat of formation, combustion,

= 0 at absolute zero T

Lennard-Jones Potential



25/10/23 L-28 contd...

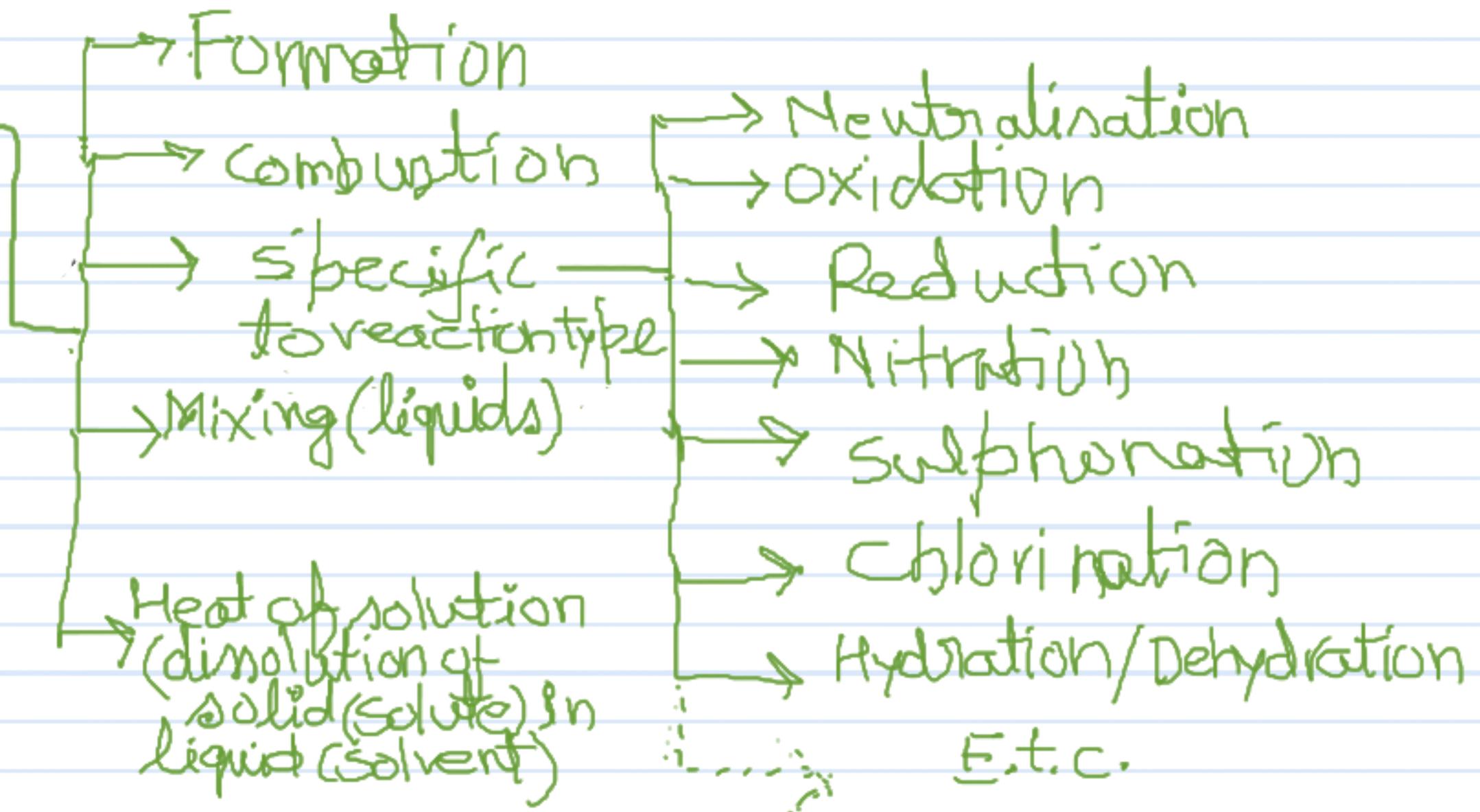
## Topics of Study

Thermophysics — sensible heat and heat capacity, heat of phase change → evaporation/condensation  
Heat of unit operations — absorption, adsorption, crystallisation etc → melting/freezing, sublimation

## Thermochemistry

Enthalpy change / Heat of  
(Heat of unit process)

$$\Delta H_{rxn}$$

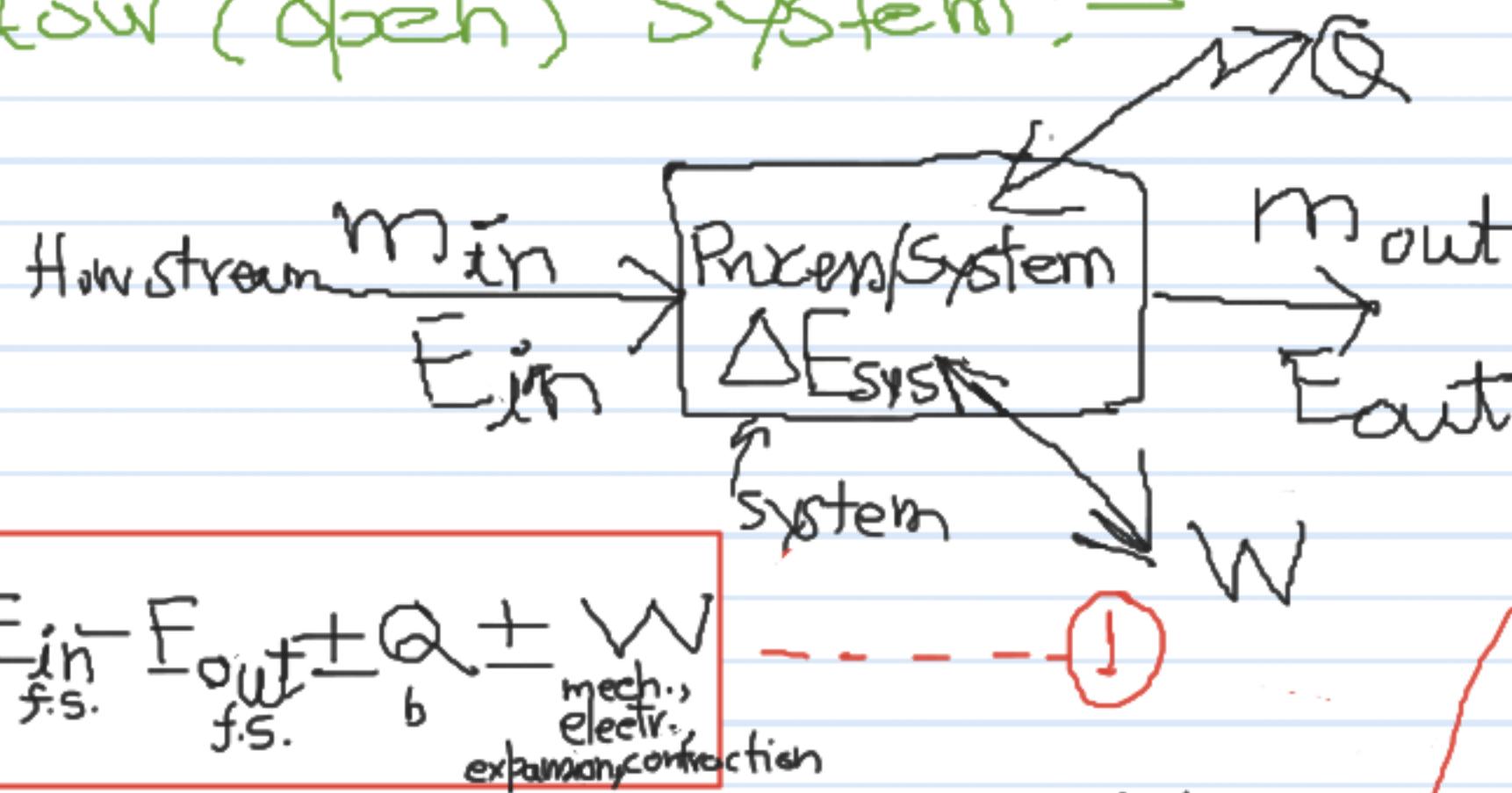


Date: 26/10/23

## Lecture - 29 Thermophysics

Law of Energy Conservation / I Law of Thermodynamics

⇒ General Energy Balance for close (non-flow) and flow (open) System :-



$Q, W$  are form of transport of energy

$$E = \frac{1}{2}mu^2$$

$$E_{PE} = PV + mgz$$

$$\text{pressure energy} = \frac{P \cdot m}{\rho}$$

Flow stream:  $E_{f.s.} = E_{int} + E_{ext} = U + E_{KE} + E_{PE} + E_{flow} = H + \frac{1}{2}u^2 + gz$

( $E_{in}$  and  $E_{out}$ )

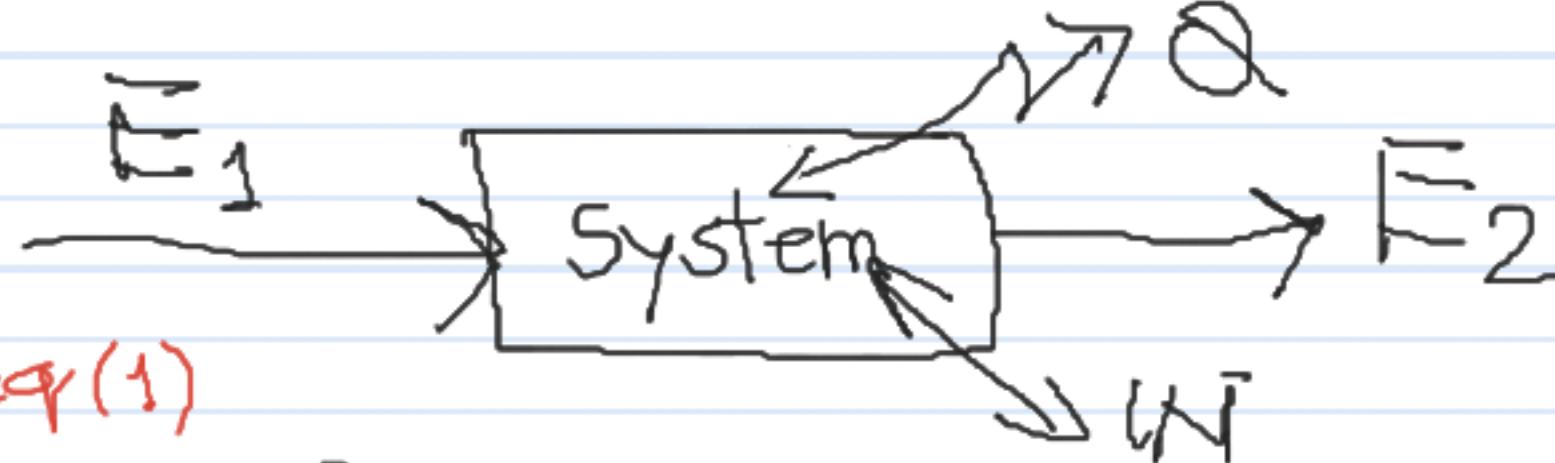
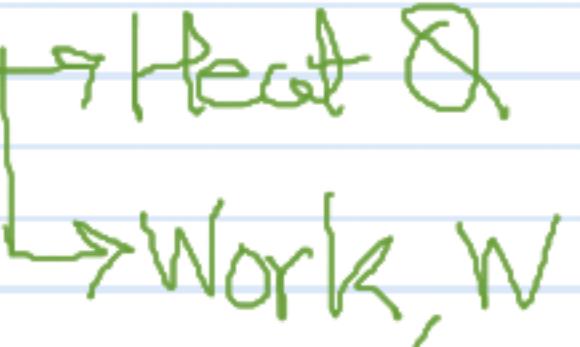
System:  $E_{sys} = [U + \frac{1}{2}mu^2 + mgz]_{sys}$

Steady Process:  $\Delta E_{sys} = 0$  (energy of system)

$= U + \frac{1}{2}u^2 + gz + PV$  (for unit mass,  $m=1$ )

$P/\rho$  -

26/10/23 L-29 contd... Energies transferred to/from the system via boundary



where  $Q = mc\Delta T$   
and

Steady flow processes

from eq(1)

$$\bar{E}_1 + Q + W = \bar{E}_2$$

$$\bar{E}_2 - \bar{E}_1 = \Delta \bar{E}_{f.s.} = \pm Q + W \quad \text{usually } \Delta \bar{E}_{f.s.} = \Delta H_{f.s.} \quad (\text{since kinetic & potential energy changes are negligible})$$

Unsteady nonflow/closed system

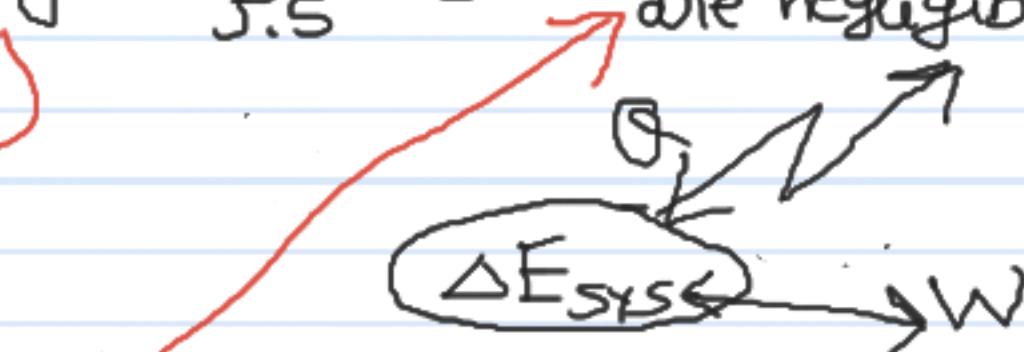
$$\bar{E}_{f.s.} = 0 \text{ and}$$

From eq.(1)

$$\Delta \bar{E}_{sys} = \pm Q + W \quad \text{usually } \Delta \bar{E}_{sys} = \Delta U_{sys}$$

or

$$\Delta U_{sys} = \pm Q + W \quad \dots \dots \dots \quad (3)$$



$$\Delta KE = \Delta gz = 0$$

(Subscript 1 and 2 represent states of system) + into system  
→ Sign of  $Q$  &  $W$  - out from system

27/10/23

## Lecture-30

I Law of Thermodynamics:

Steady flow:  $\Delta H_{f.s.} = \pm Q \pm W$

Unsteady non-flow:  $\Delta E_{sys} = \Delta U_{sys}$

$$\Delta U_{sys} = \pm Q \pm W$$

Usually for chemical process  $W = 0$

therefore  $\Delta H_{f.s.} = \pm Q$  (for steady flow system)

and  $\Delta U_{sys} = \pm Q$  (for batch/non flow  
(unsteady state system))

Date: 27/10/23 L-30 contd....

Definitions:-

Heat capacity:  $C = \frac{Q}{\Delta T}$ , Specific heat  $s = \frac{Q}{m \Delta T}$

For solids & liquids (incompressible materials) only one C is defined whereas gases have heat capacity at constant pressure,  $C_p$  and constant volume,  $C_v$

For ideal gas  $C_p - C_v = R$   $(C_p > C_v)$

Sensible Heat (change in temperature is observed)

$$\text{Q}_{\text{Sensible}} = m C \underline{\Delta T}$$

Latent heat (Phase change/state of aggregation changes)

$$\text{Q}_{\text{Latent}} = m \underline{\lambda}$$

Date: 28/10/23

## Lecture-31

Heat capacity of gases:

$$C = \frac{\partial Q}{\partial T} \Rightarrow C_p = \frac{\partial Q_p}{\partial T} \text{ and } C_v = \frac{\partial Q_v}{\partial T}$$

I Law:  $dU = \partial Q + \partial W$

$$dU = \partial Q - PdV$$

$$dU = \partial Q_p - PdV \Rightarrow \partial Q_p = \underline{dU + PdV}$$

We know,  $H = U + PV$

$$\therefore dH = dU + PdV + VdP$$

at constant  $P$ ,  $dH_p = \boxed{dU + PdV}$  ( $dP = 0$ )

$$\boxed{dH_p = \partial Q_p}$$

$$C_p = \frac{\partial Q_p}{\partial T} = \left( \frac{dH}{dT} \right)_p$$

Date 28/10/23

Lecture-31 contd. . .

## Heat capacities of gas

$$Q = m C \Delta T$$

I Law :  $dU = \partial Q - PdV$

at constant volume:  $dU = \partial Q_v$  (since  $dV=0$ )

$$C_V = \frac{\partial Q_V}{\partial T} = \left( \frac{dU}{dT} \right)_V$$

It can be shown that for ideal (monatomic) gases

$$C_P - C_V = R \rightarrow \text{Universal gas constant}$$

For ideal gas  $U$  is function of only  $T$ . Also  $C_P = a + bT + cT^2$

Mean heat capacity  $C_{P,\text{mean}} = \frac{\int_{T_1}^{T_2} C_P dT}{T_2 - T_1}$

$$C_{P,\text{mean}} = a + \frac{b}{2}(T_2 + T_1) + \frac{c}{3}(T_2^2 + 2T_1T_2 + T_1^2)$$

$$C_P = 2.5 + 4 \times 10^{-3}T - 1.4 \times 10^{-4}T^2$$

$$C_{P,\text{mean}} = ?$$

$50-100^\circ C$   
 $323K - 373K$

Date: 30/10/23

## Lecture-32

Heat capacities of monatomic gases (He, Ar, Kr, Xe, Ne, Re)

Internal energy is only composed of kinetic energy of translation

of molecules :  $U = \frac{3}{2} RT$

$$C_V = \frac{\partial U}{\partial T} = \frac{3}{2} R = 3 \text{ g-cal/g-mol K}$$

$$R \approx 2 \text{ g-cal/g-mol K}$$

$$C_P = R + C_V = 2 + 3 = 5 \text{ g-cal/g-mol K}$$

$$\frac{C_P}{C_V} = \gamma = \frac{5}{3} = 1.67$$

Data on heat capacity is given in texts (eg. Table 18, Fig 60, page 253)

Thumb rule:  $C_P$  of water  $\approx 2 C_P$  of steam  $\approx 4 C_P$  of air

$$C_{P,\text{mean}} = \frac{\int_{T_1}^{T_2} C_P dT}{T_2 - T_1}$$

(Refer Table 19, Hoggan, Watson Text)

Fig 62 and 63

## Properties of Water and Air

Density

Water

1000 kg/m<sup>3</sup>

Air

1.23 g/L

Heat capacity

1 cal/g K

0.24 cal/g K

Viscosity

1 cP

$1 \times 10^{-3}$  cP

Mol. wt.

18

29